

CS 4644-DL / 7643-A: LECTURE 21

DANFEI XU

- 2D Computer Vision (Continued)
- 3D Vision: Representations and Neural Rendering

Computer Vision Tasks

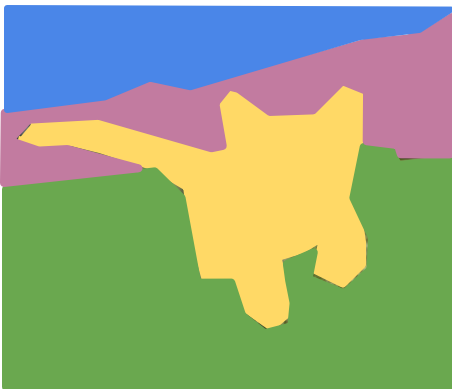
Classification



CAT

No spatial extent

Semantic Segmentation



**GRASS, CAT,
TREE, SKY**

No objects, just pixels

Object Detection



DOG, DOG, CAT

Multiple Object

Instance Segmentation



DOG, DOG, CAT

[This image is CC0 public domain](#)

Semantic Segmentation Idea: Fully Convolutional

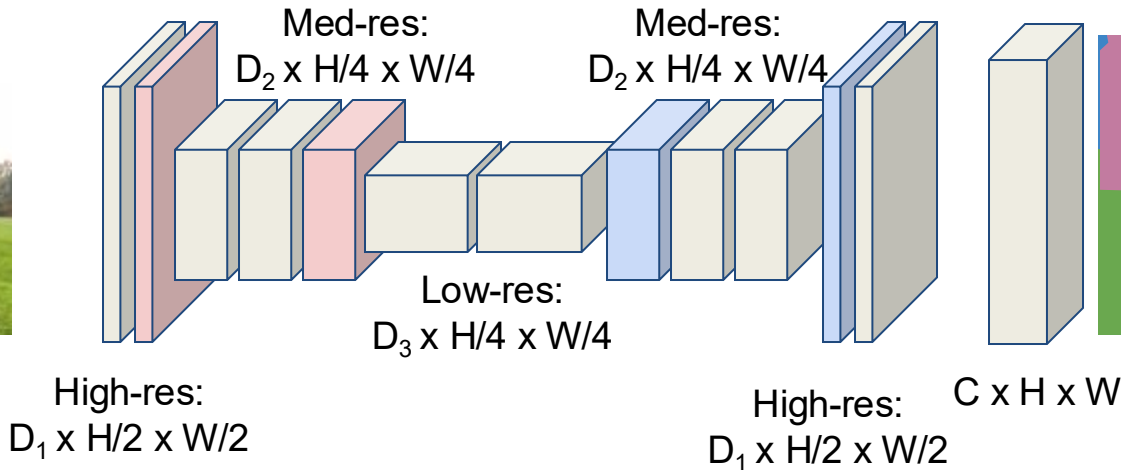
Downsampling:
Pooling, strided
convolution

Design network as a bunch of convolutional layers, with
downsampling and **upsampling** inside the network!

Upsampling:
???

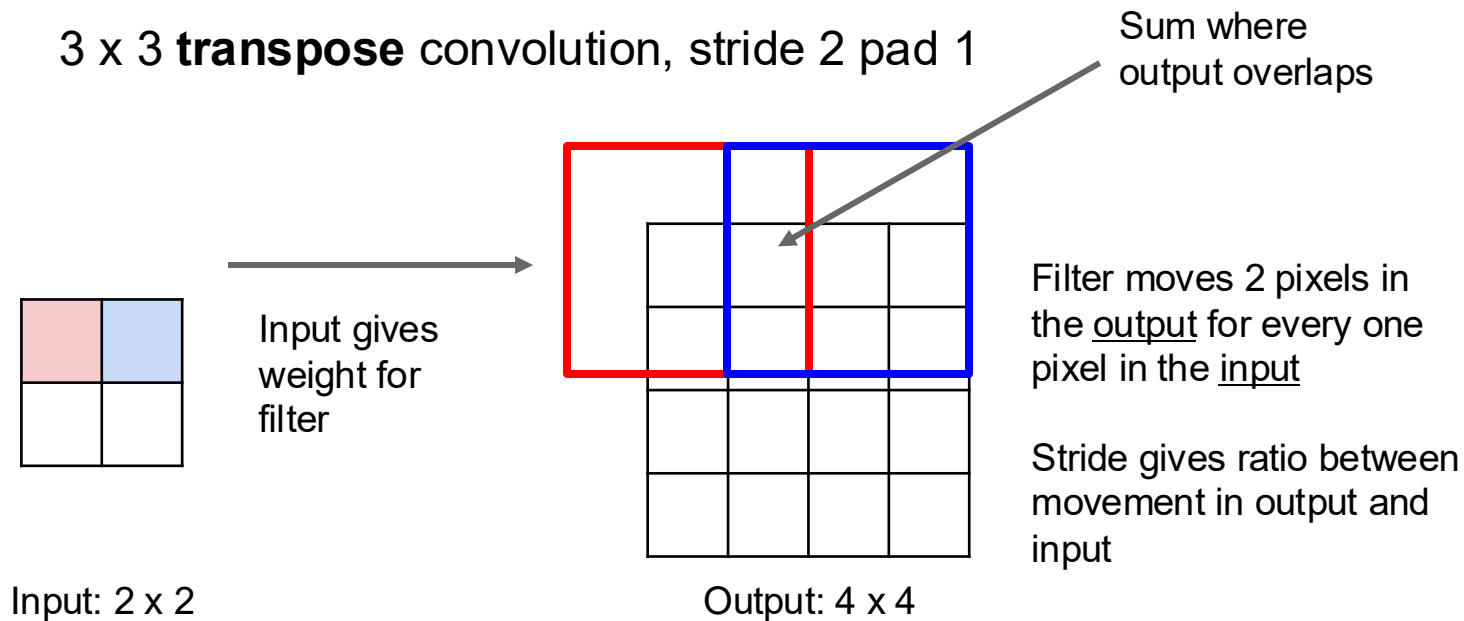


Input:
 $3 \times H \times W$

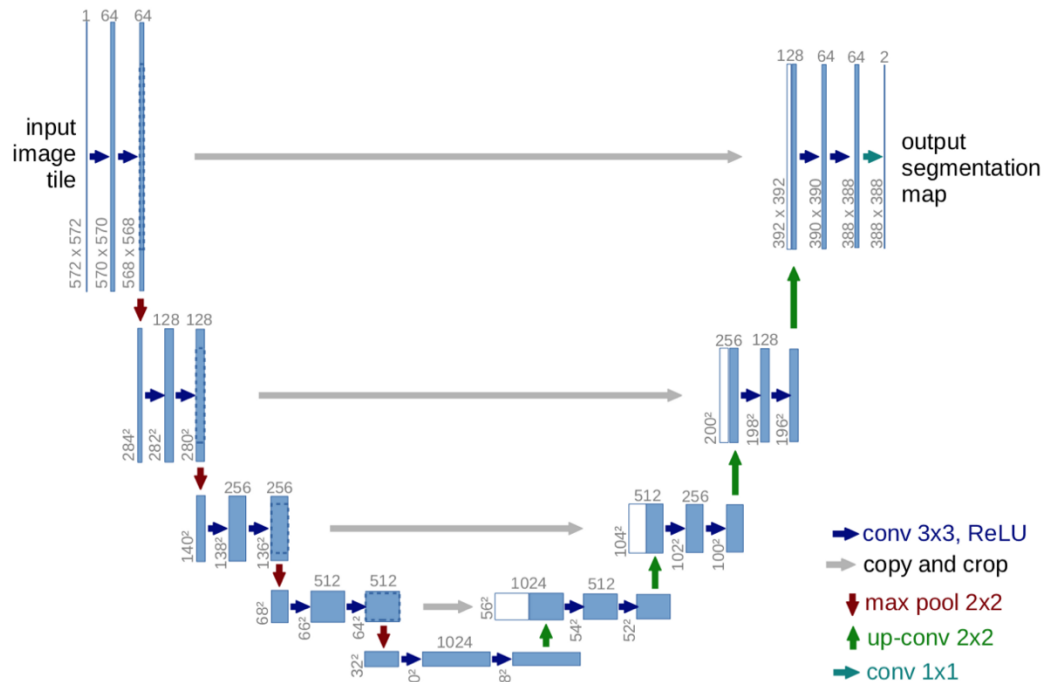


Predictions:
 $H \times W$

Learnable Upsampling: Transposed Convolution



Semantic Segmentation: U-Net



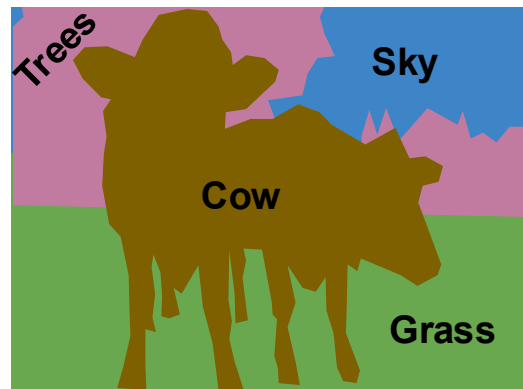
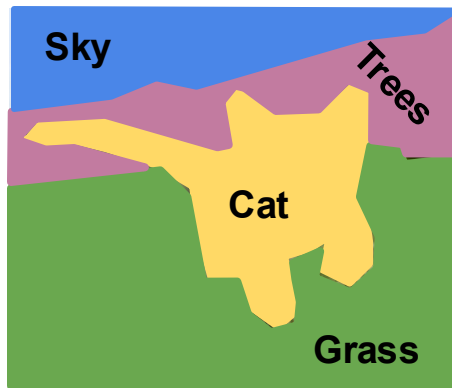
Idea: Concatenate feature maps from the downsampling stage with the features in the upsampling stage.

Very commonly used today!

Semantic Segmentation

Label each pixel in the image with a category label

Don't differentiate instances, only care about pixels



Object Detection

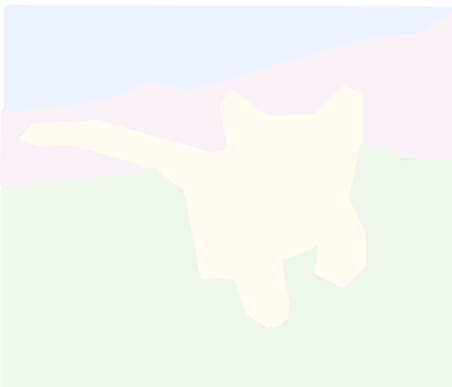
Classification



CAT

No spatial extent

Semantic Segmentation



GRASS, CAT,
TREE, SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

Instance Segmentation

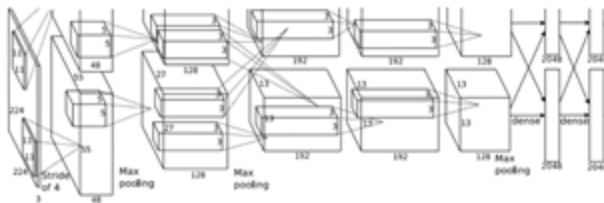


DOG, DOG, CAT

Multiple Object

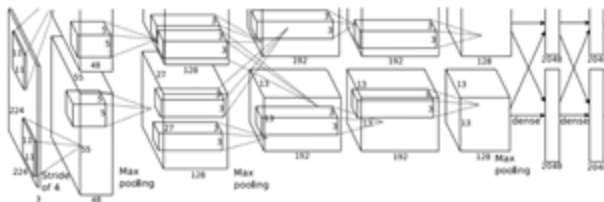
Object Detection: Multiple Objects

Each image needs a
different number of outputs!



CAT: (x, y, w, h)

4 numbers

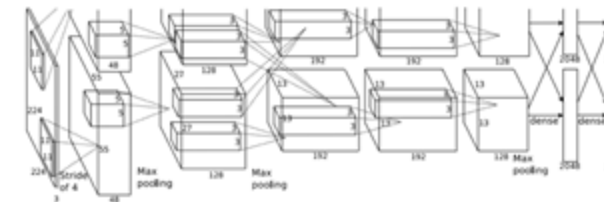


DOG: (x, y, w, h)

DOG: (x, y, w, h)

CAT: (x, y, w, h)

12 numbers



DUCK: (x, y, w, h)

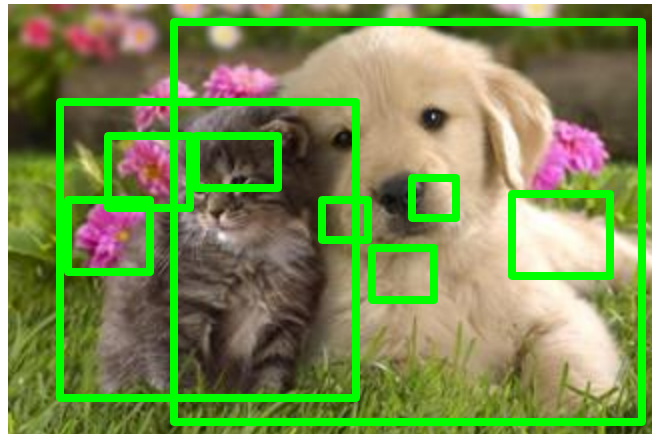
DUCK: (x, y, w, h)

....

Many
numbers!

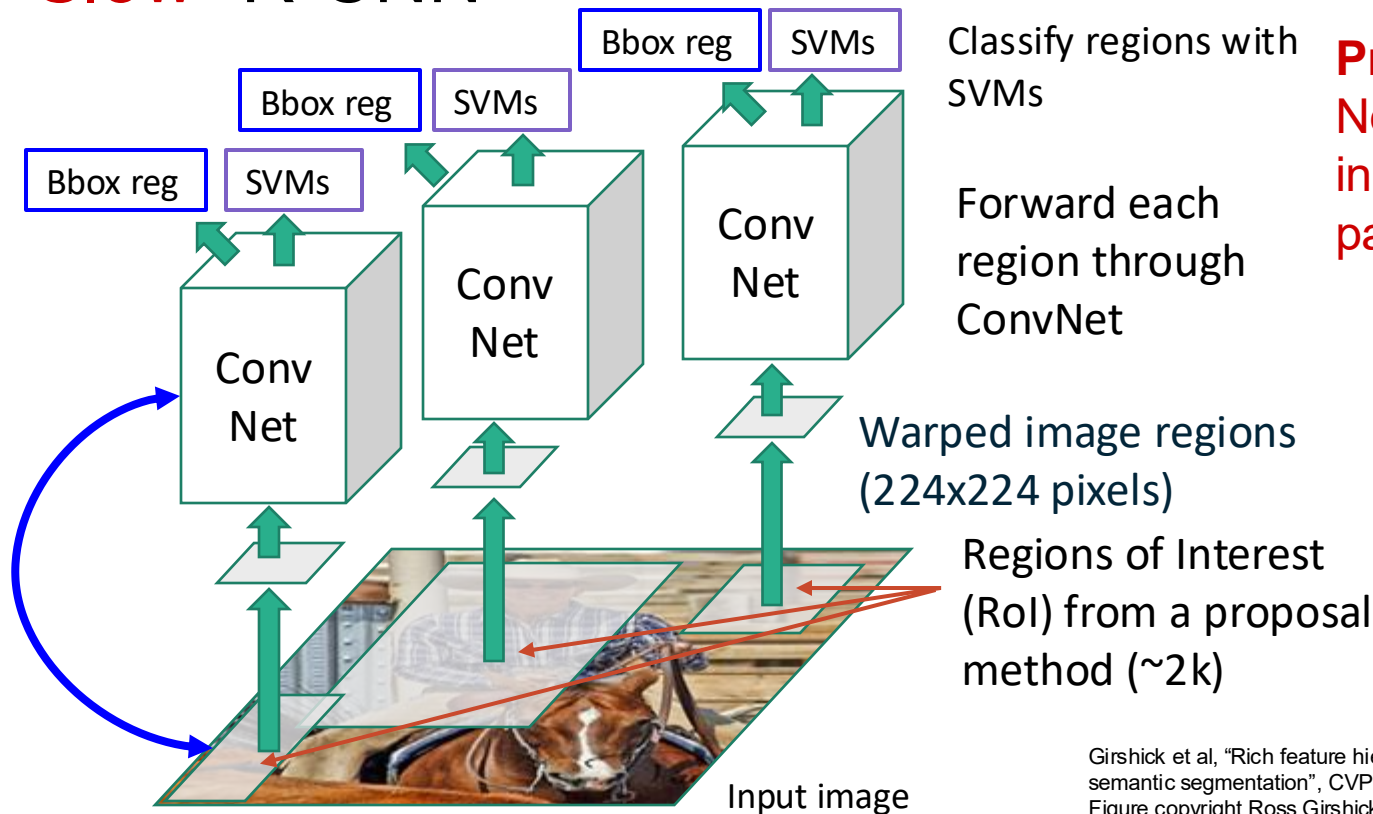
Region Proposals: Selective Search

- Find “blobby” image regions that are likely to contain objects
- Relatively fast to run; e.g. Selective Search gives 2000 region proposals in a few seconds on CPU



“Slow” R-CNN

Predict “corrections” to the RoI: 4 numbers: (dx, dy, dw, dh)



Classify regions with SVMs

Forward each region through ConvNet

Warped image regions (224x224 pixels)

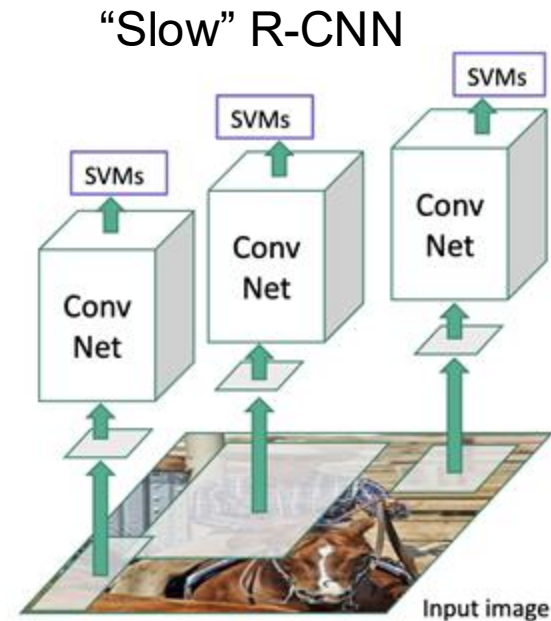
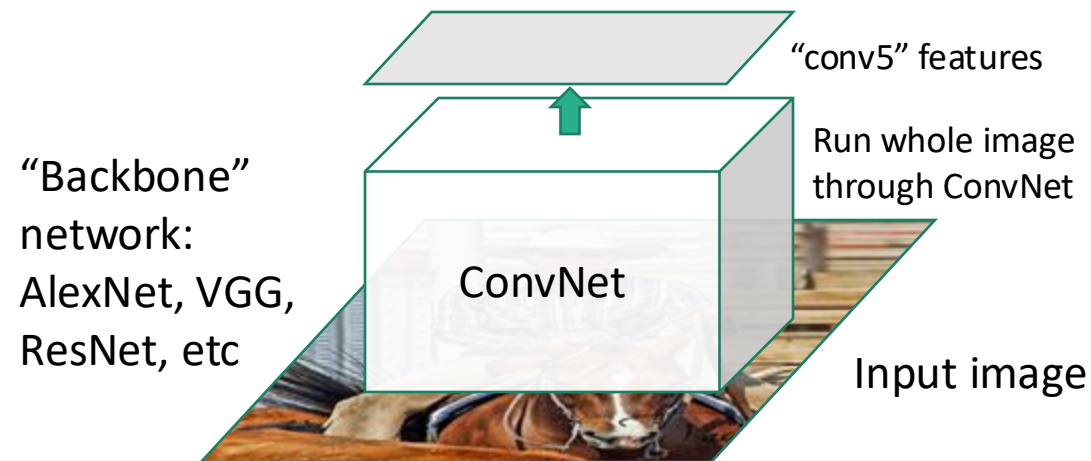
Regions of Interest (RoI) from a proposal method ($\sim 2k$)

Problem: Very slow!
Need to do $\sim 2k$ independent forward passes for each image!

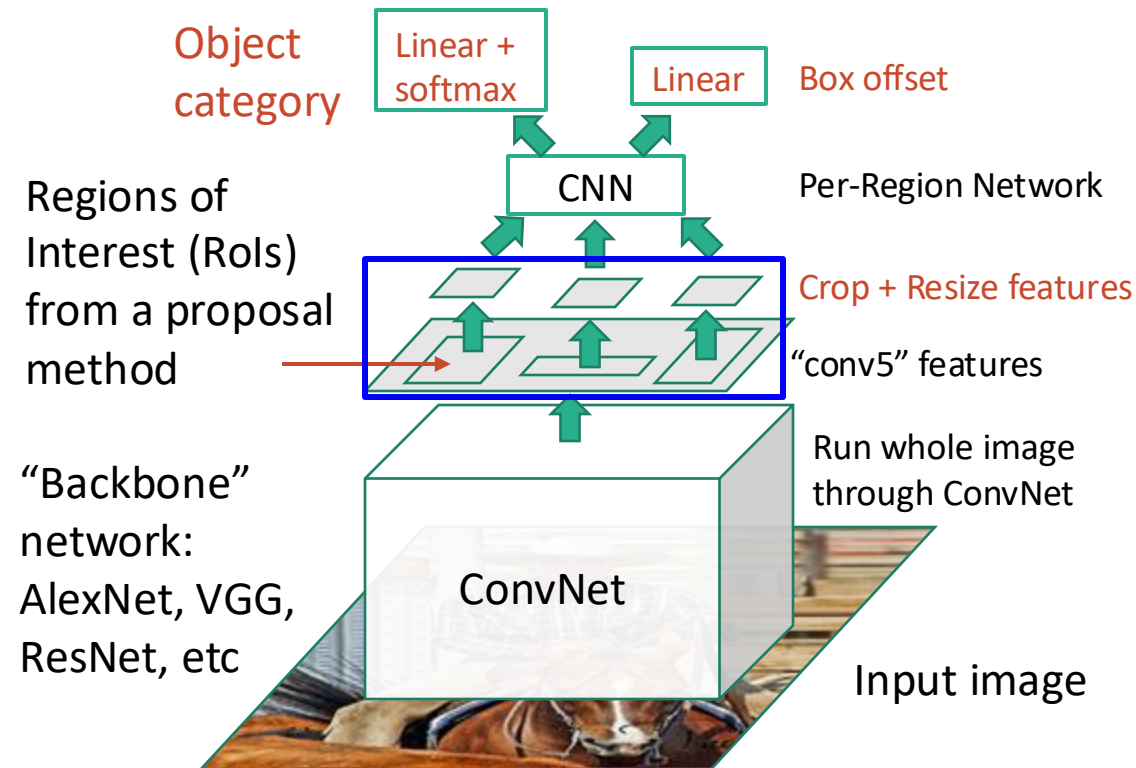
Idea: Pass the image through convnet before cropping! Crop the conv feature instead!

Girshick et al, “Rich feature hierarchies for accurate object detection and semantic segmentation”, CVPR 2014.
Figure copyright Ross Girshick, 2015; [source](#). Reproduced with permission.

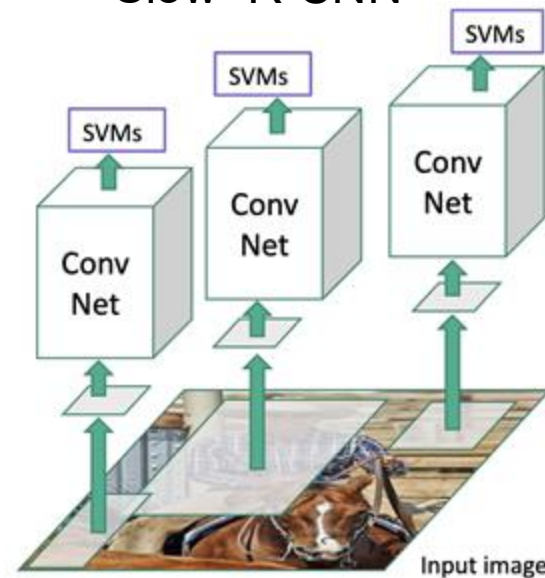
Fast R-CNN



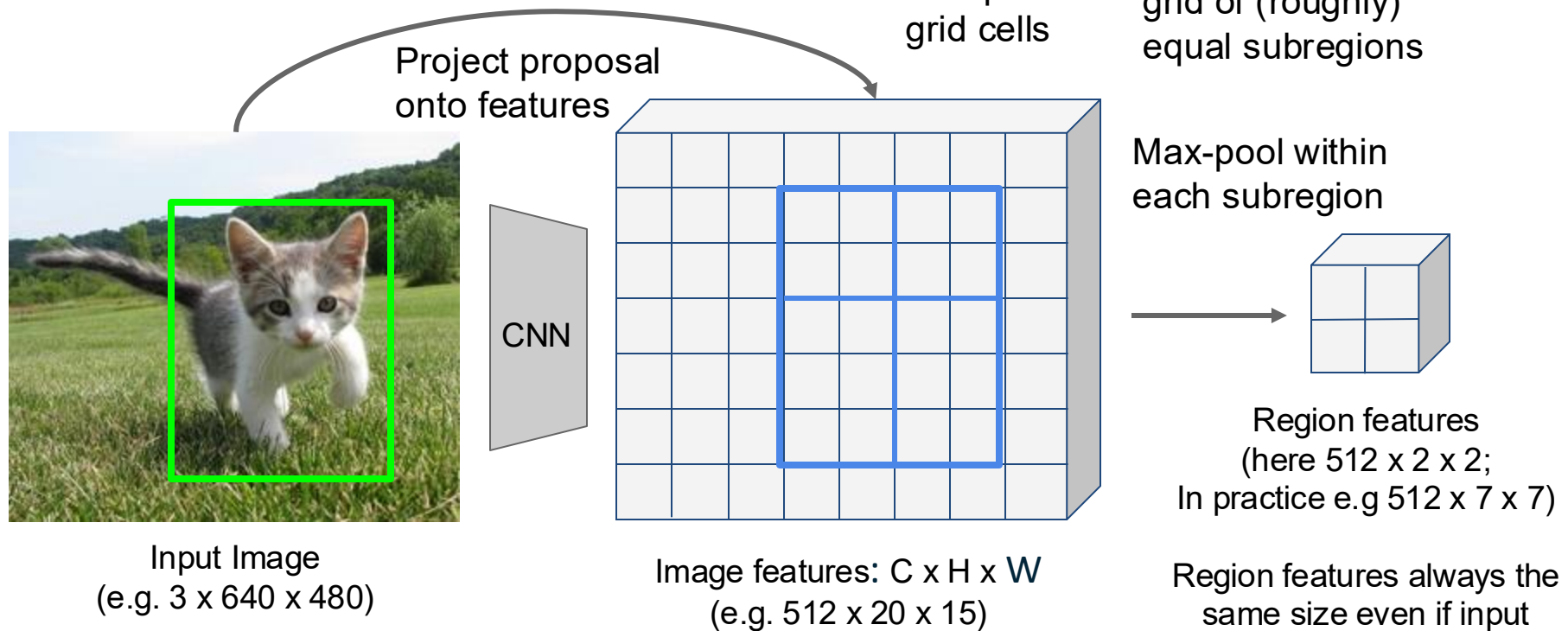
Fast R-CNN



"Slow" R-CNN



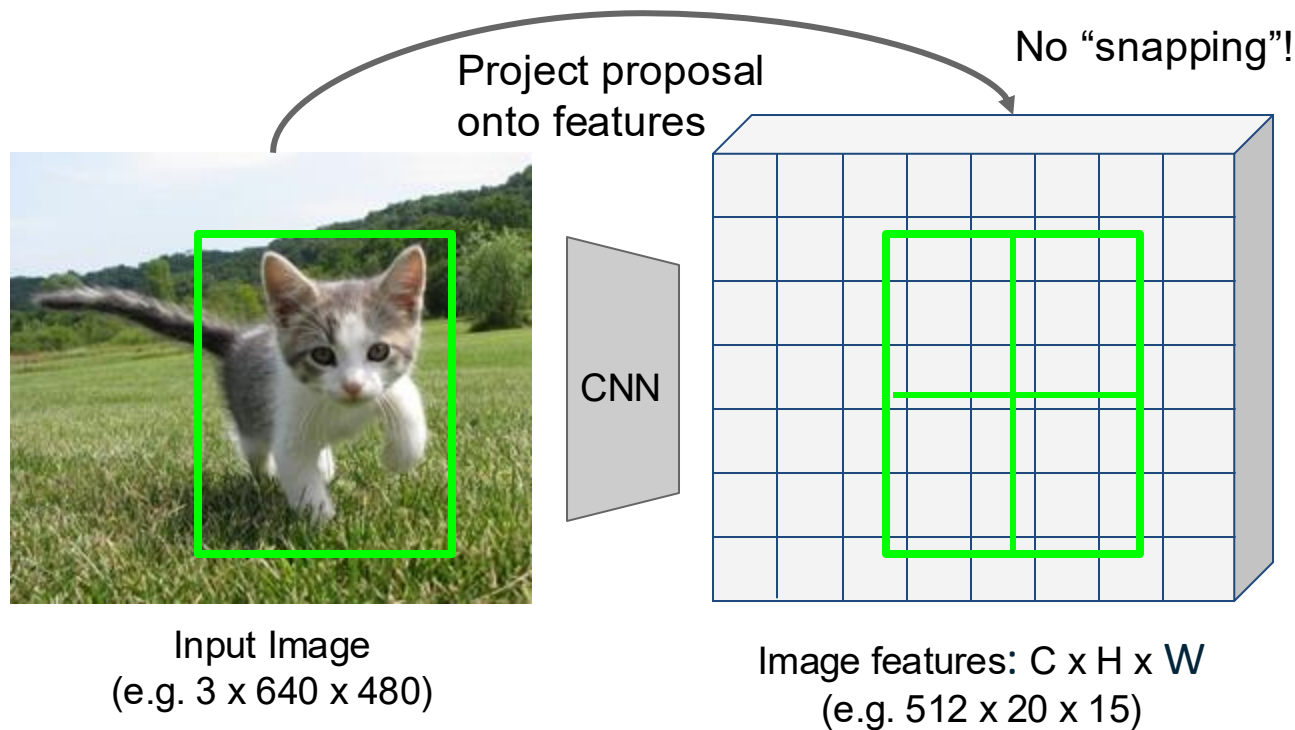
Cropping Features: RoI Pool



Region features always the same size even if input regions have different sizes!

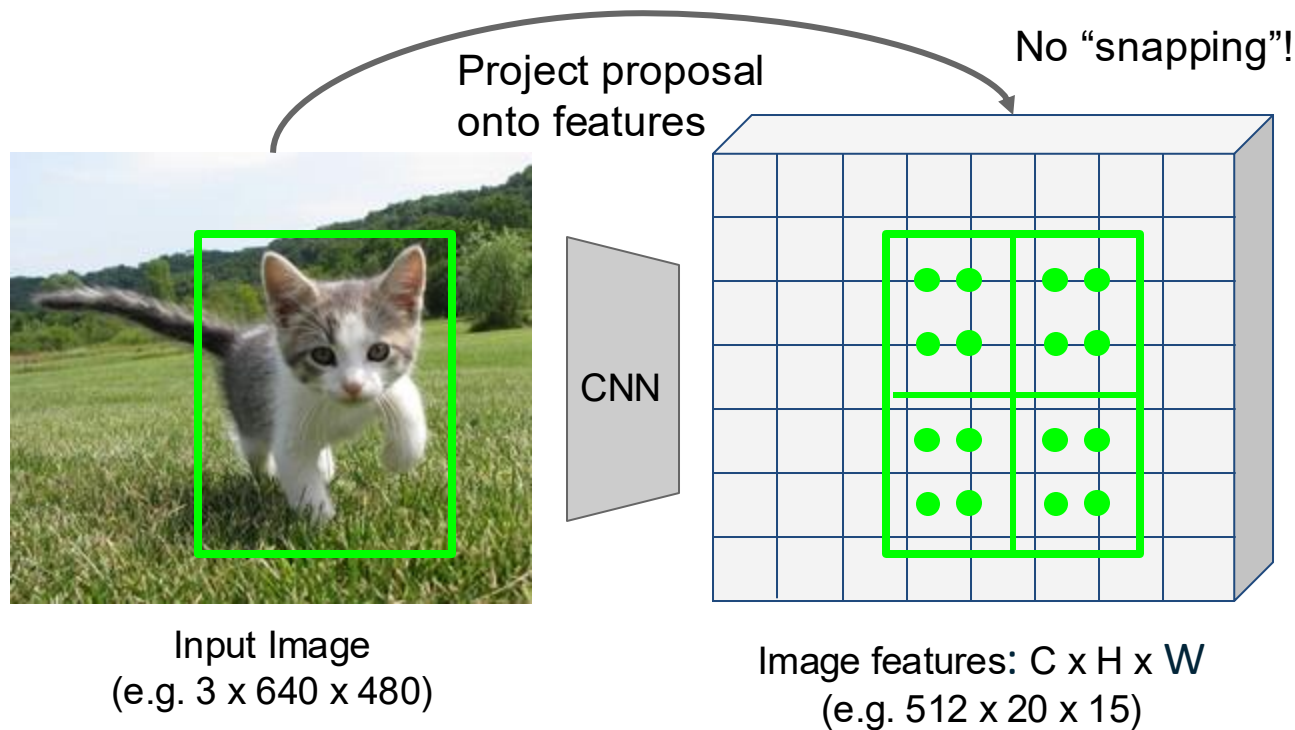
Problem: Region features slightly misaligned

Cropping Features: RoI Align

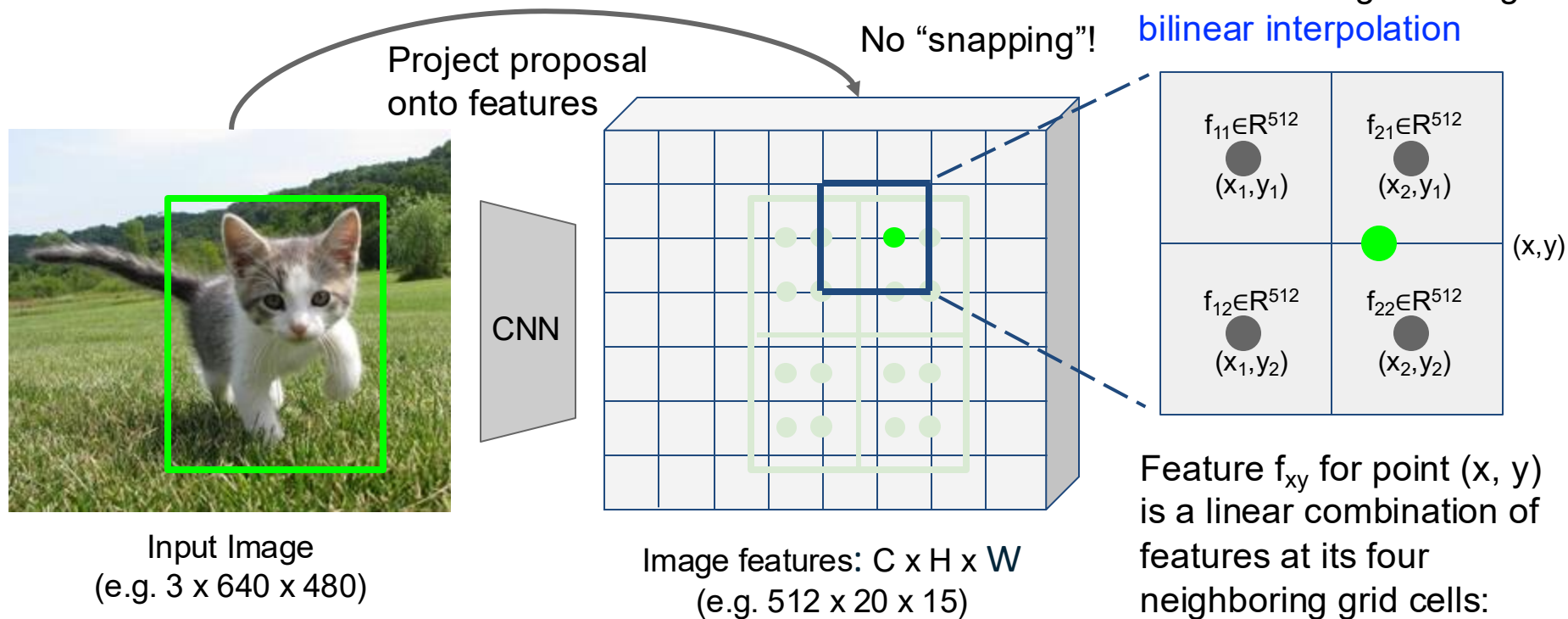


Cropping Features: RoI Align

Sample at regular points
in each subregion using
bilinear interpolation

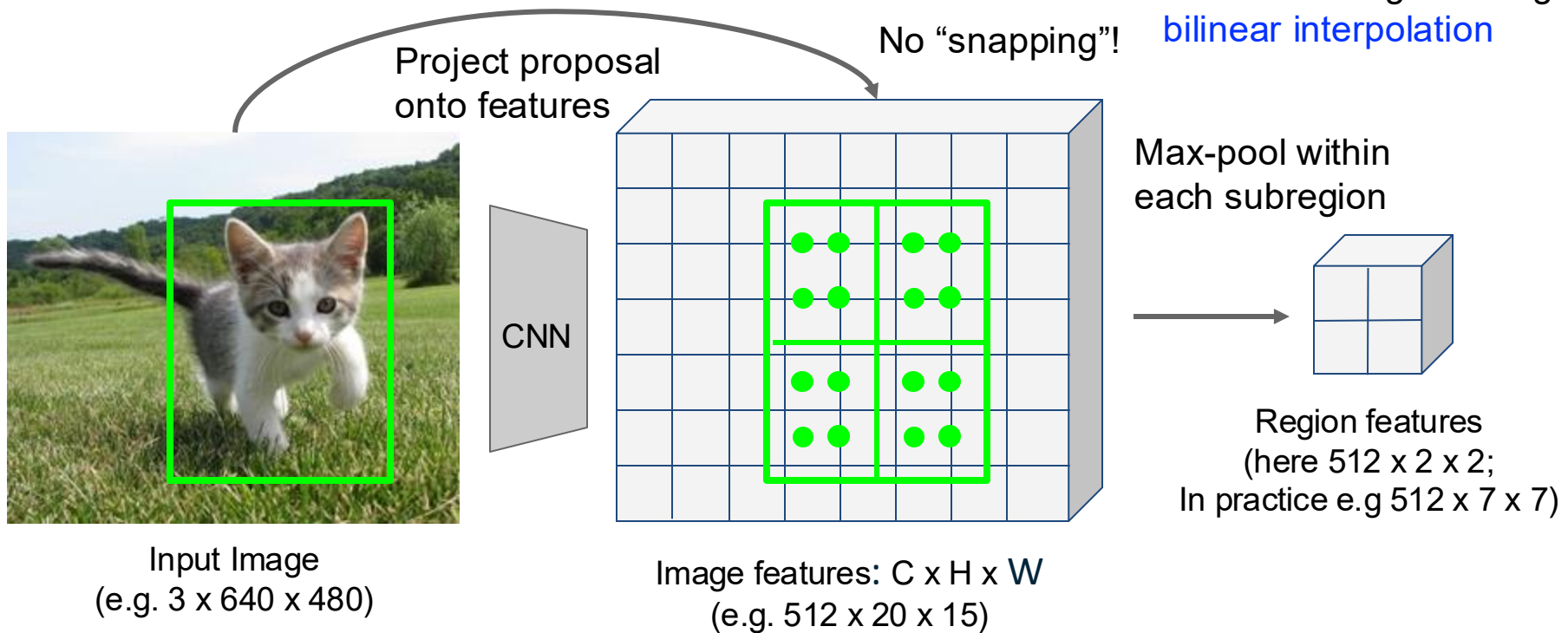


Cropping Features: RoI Align



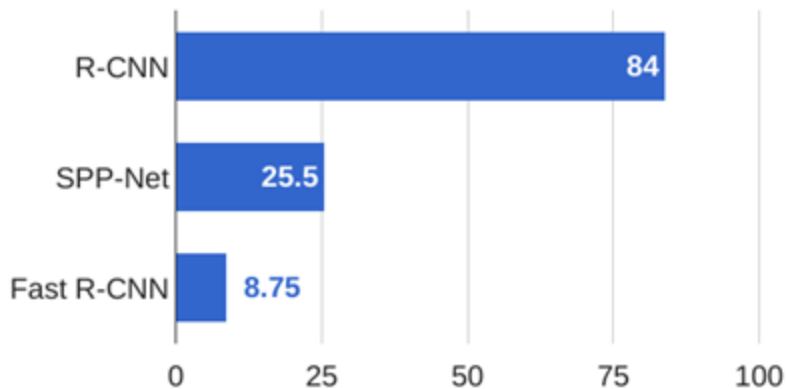
$$f_{xy} = \sum_{i,j=1}^2 f_{i,j} \max(0, 1 - |x - x_i|) \max(0, 1 - |y - y_j|)$$

Cropping Features: RoI Align

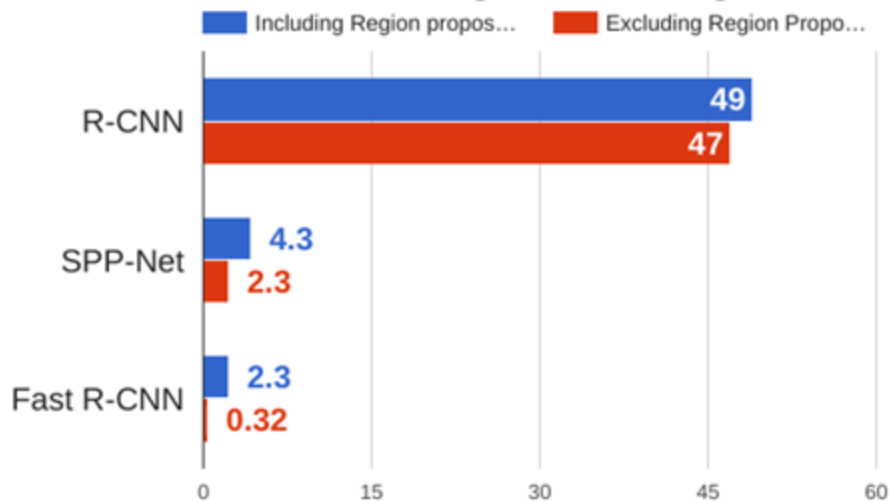


R-CNN vs Fast R-CNN

Training time (Hours)



Test time (seconds)



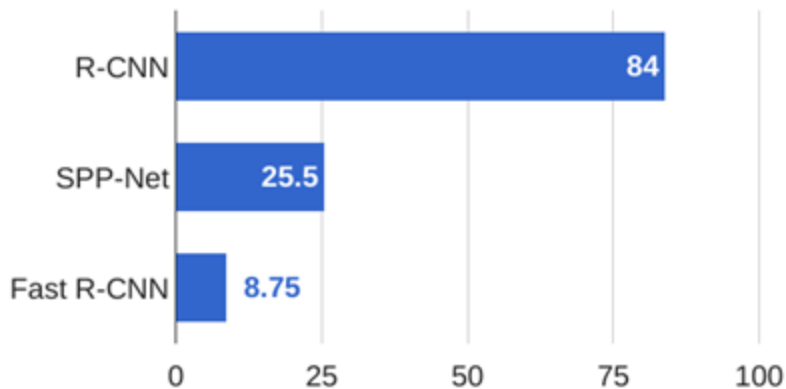
Girshick et al, "Rich feature hierarchies for accurate object detection and semantic segmentation", CVPR 2014.

He et al, "Spatial pyramid pooling in deep convolutional networks for visual recognition", ECCV 2014

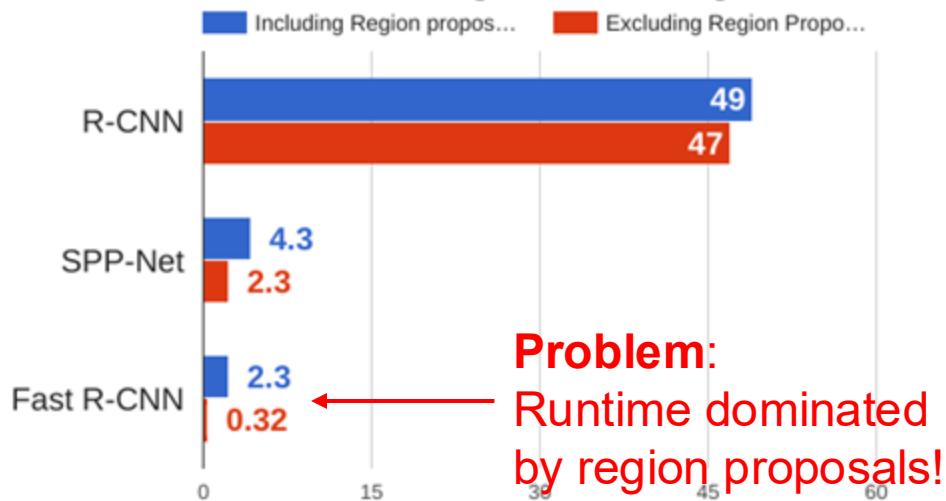
Girshick, "Fast R-CNN", ICCV 2015

R-CNN vs Fast R-CNN

Training time (Hours)



Test time (seconds)



Girshick et al, "Rich feature hierarchies for accurate object detection and semantic segmentation", CVPR 2014.

He et al, "Spatial pyramid pooling in deep convolutional networks for visual recognition", ECCV 2014

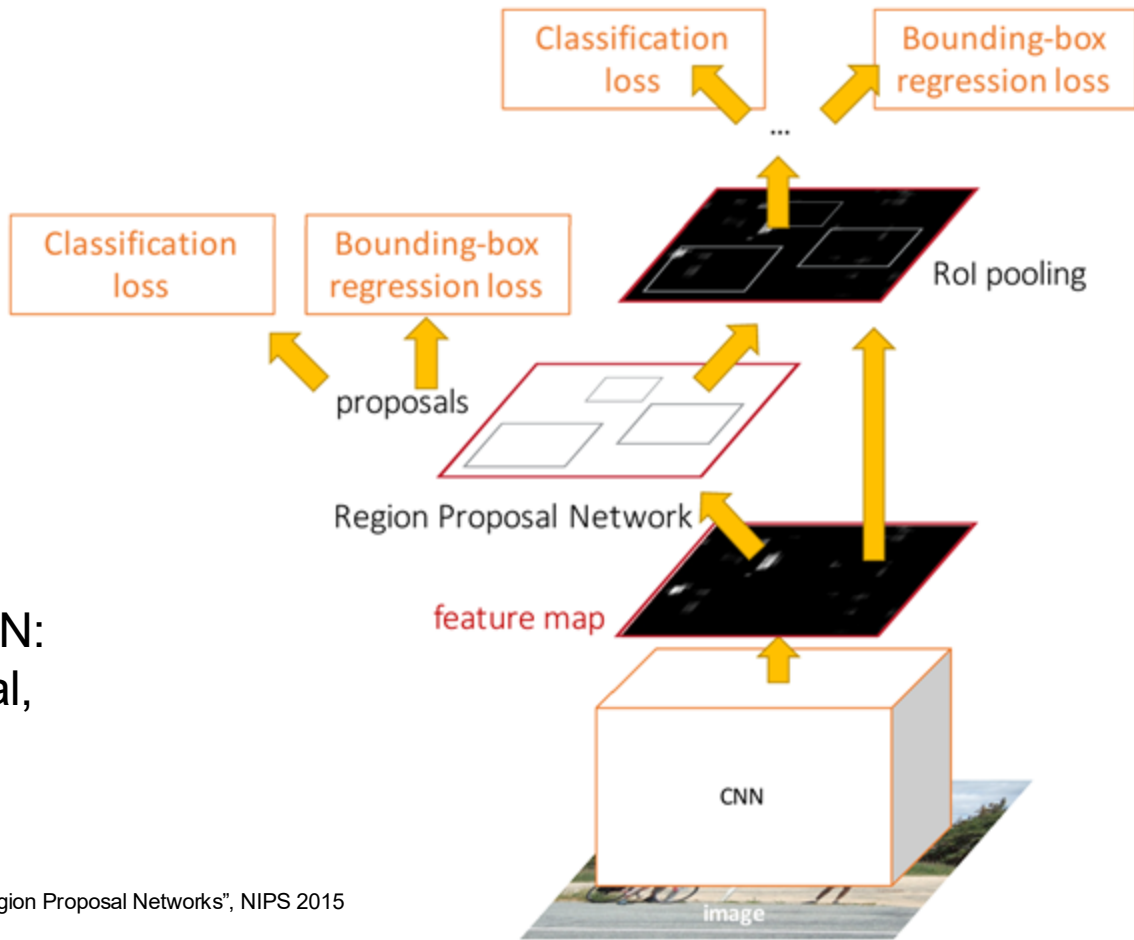
Girshick, "Fast R-CNN", ICCV 2015

Faster R-CNN:

Make CNN do proposals!

Insert **Region Proposal Network (RPN)** to predict proposals from features

Otherwise same as Fast R-CNN:
Crop features for each proposal,
classify each one

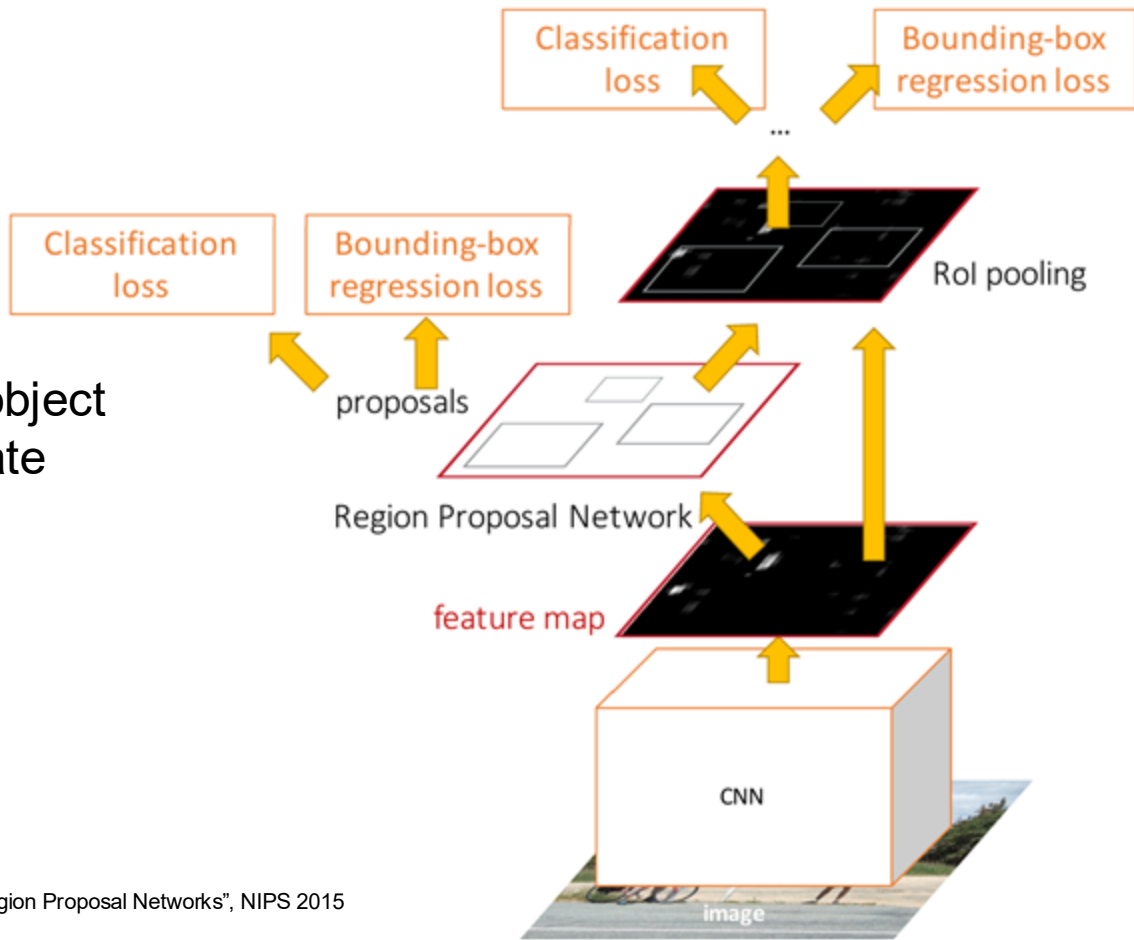


Faster R-CNN:

Make CNN do proposals!

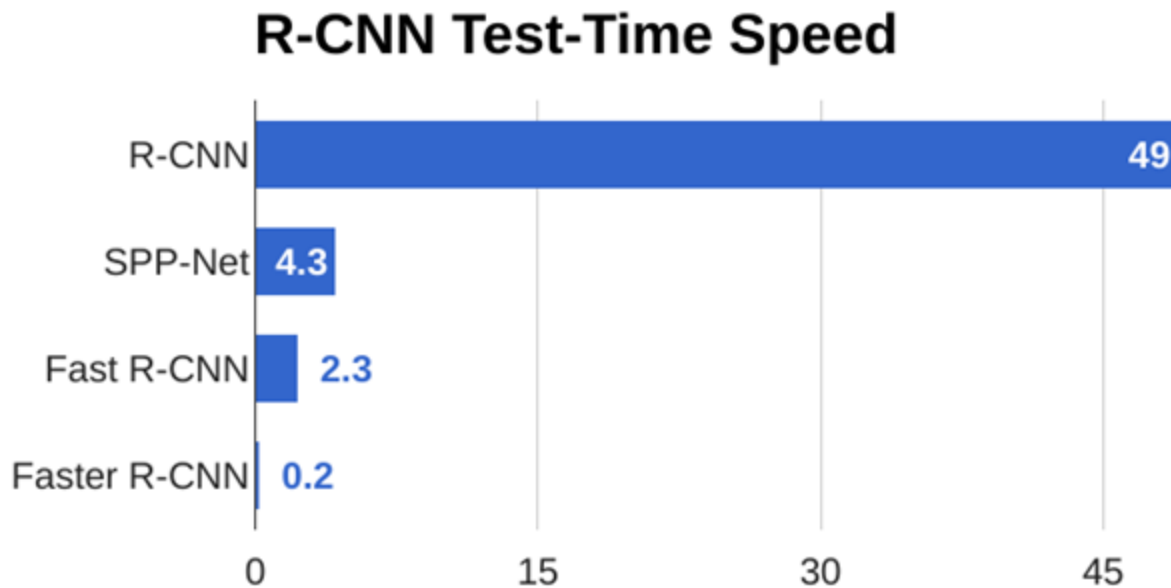
Jointly train with 4 losses:

1. RPN classify object / not object
2. RPN regress box coordinate residuals
3. Final classification score (object classes)
4. Final box coordinates

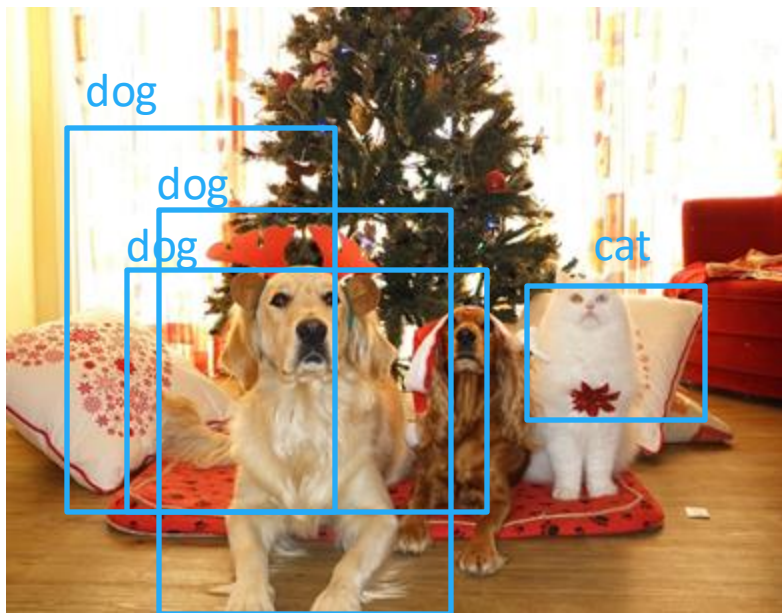


Faster R-CNN:

Make CNN do proposals!



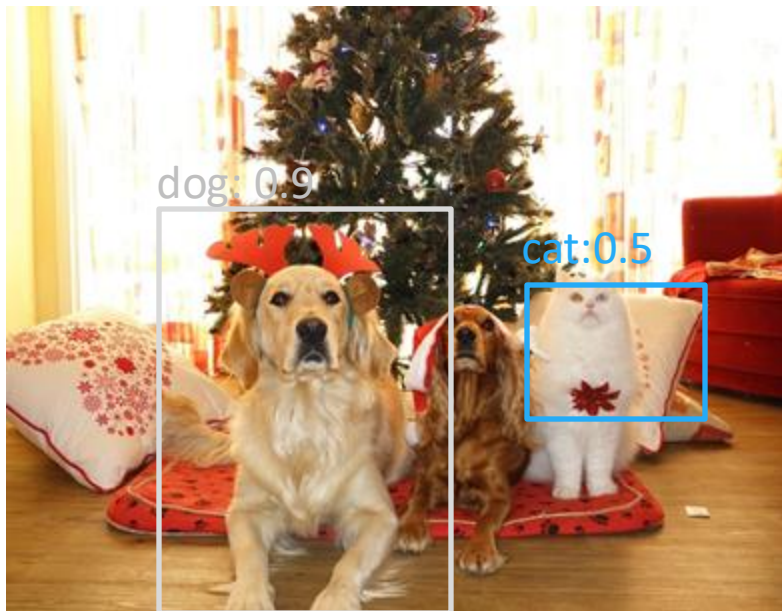
Which prediction to pick?



Problem: Detectors almost always generate more box predictions than the number of objects in the image!
E.g., 300 is an upper bound how many objects we wish to detect.

We need to remove the **redundant predictions!**

Non-Max Suppression (NMS)



Intuitively: locally pick the box that has the highest “objectness” or class score and suppress other boxes that have significant overlap with the chosen box

Step 1: Pick highest-score prediction box

Step 2: Remove bounding boxes with

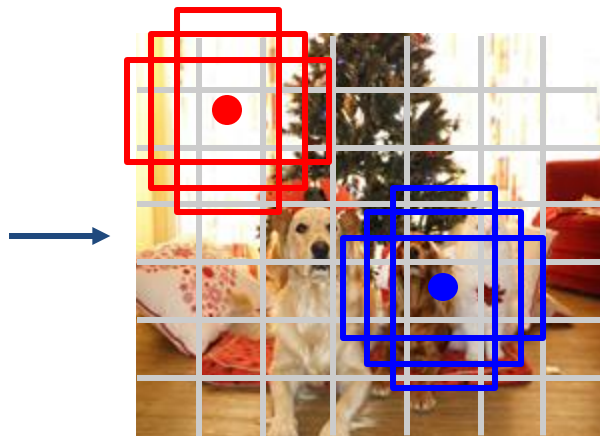
Intersection over Union (IoU) scores higher than certain threshold (e.g., 0.5)

Go back to step 1

Single-Stage Object Detectors: YOLO / SSD / RetinaNet



Input image
 $3 \times H \times W$



Divide image into grid
 7×7

Image a set of **base boxes**
centered at each grid cell
Here $B = 3$

Within each grid cell:

- Regress from each of the B base boxes to a final box with 5 numbers:
($dx, dy, dh, dw, confidence$)
- Predict scores for each of C classes (including background as a class)
- Looks a lot like RPN, but category-specific!

Output:

$$7 \times 7 \times (5 * B + C)$$

Redmon et al, "You Only Look Once:
Unified, Real-Time Object Detection", CVPR 2016
Liu et al, "SSD: Single-Shot MultiBox Detector", ECCV 2016
Lin et al, "Focal Loss for Dense Object Detection", ICCV 2017

Object Detection: Lots of variables ...

Backbone

Network

VGG16

ResNet-101

Inception V2

Inception V3

Inception

ResNet

MobileNet

“Meta-Architecture”

Two-stage: Faster R-CNN

Single-stage: YOLO / SSD

Hybrid: R-FCN

Image Size

Region Proposals

...

Takeaways

Faster R-CNN is slower
but more accurate

SSD is much faster but
not as accurate

Bigger / Deeper
backbones work better

Huang et al, “Speed/accuracy trade-offs for modern convolutional object detectors”, CVPR 2017

Zou et al, “Object Detection in 20 Years: A Survey”, arXiv 2019

R-FCN: Dai et al, “R-FCN: Object Detection via Region-based Fully Convolutional Networks”, NIPS 2016

Inception-V2: Ioffe and Szegedy, “Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift”, ICML 2015

Inception V3: Szegedy et al, “Rethinking the Inception Architecture for Computer Vision”, arXiv 2016

Inception ResNet: Szegedy et al, “Inception-V4, Inception-ResNet and the Impact of Residual Connections on Learning”, arXiv 2016

MobileNet: Howard et al, “Efficient Convolutional Neural Networks for Mobile Vision Applications”, arXiv 2017

Instance Segmentation

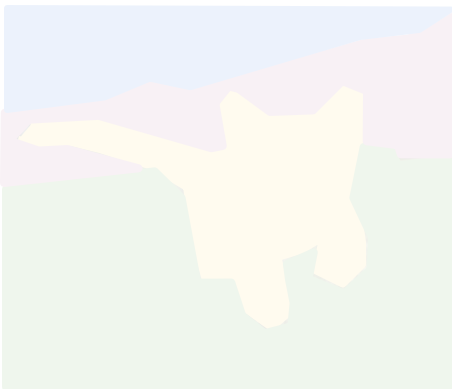
Classification



CAT

No spatial extent

Semantic Segmentation



GRASS, CAT,
TREE, SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

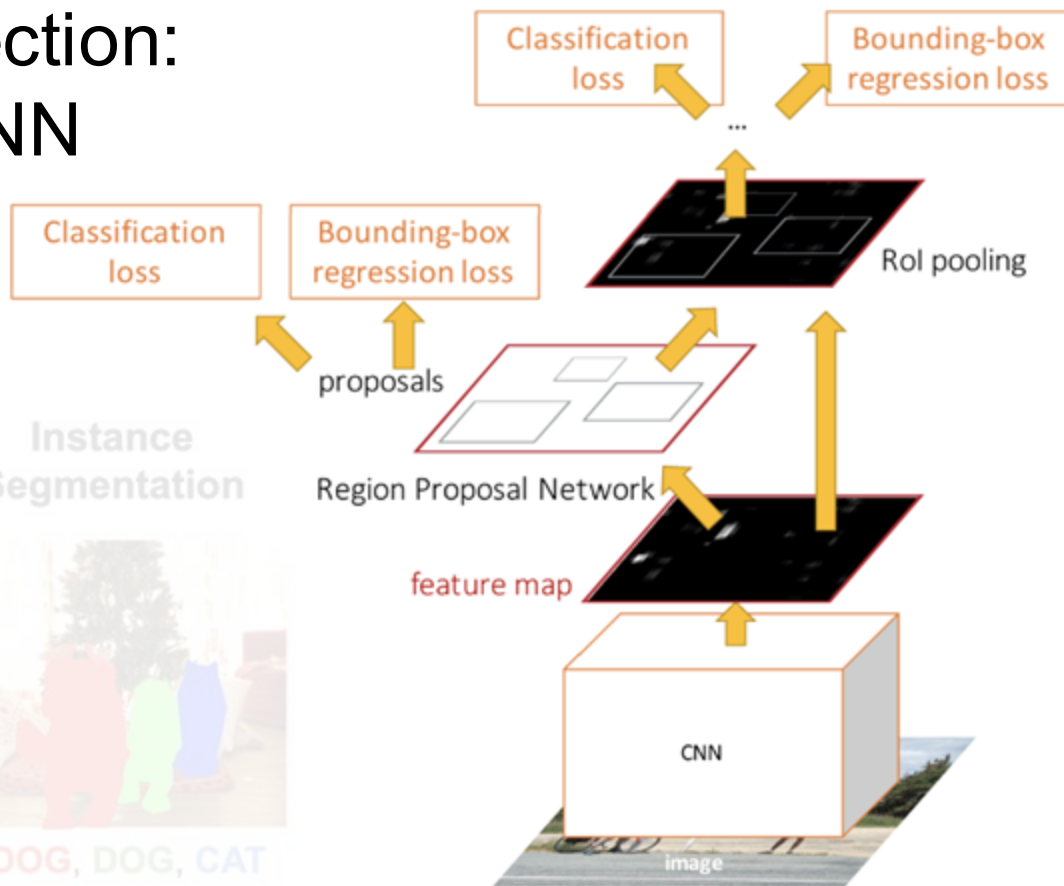
Multiple Object

Instance Segmentation

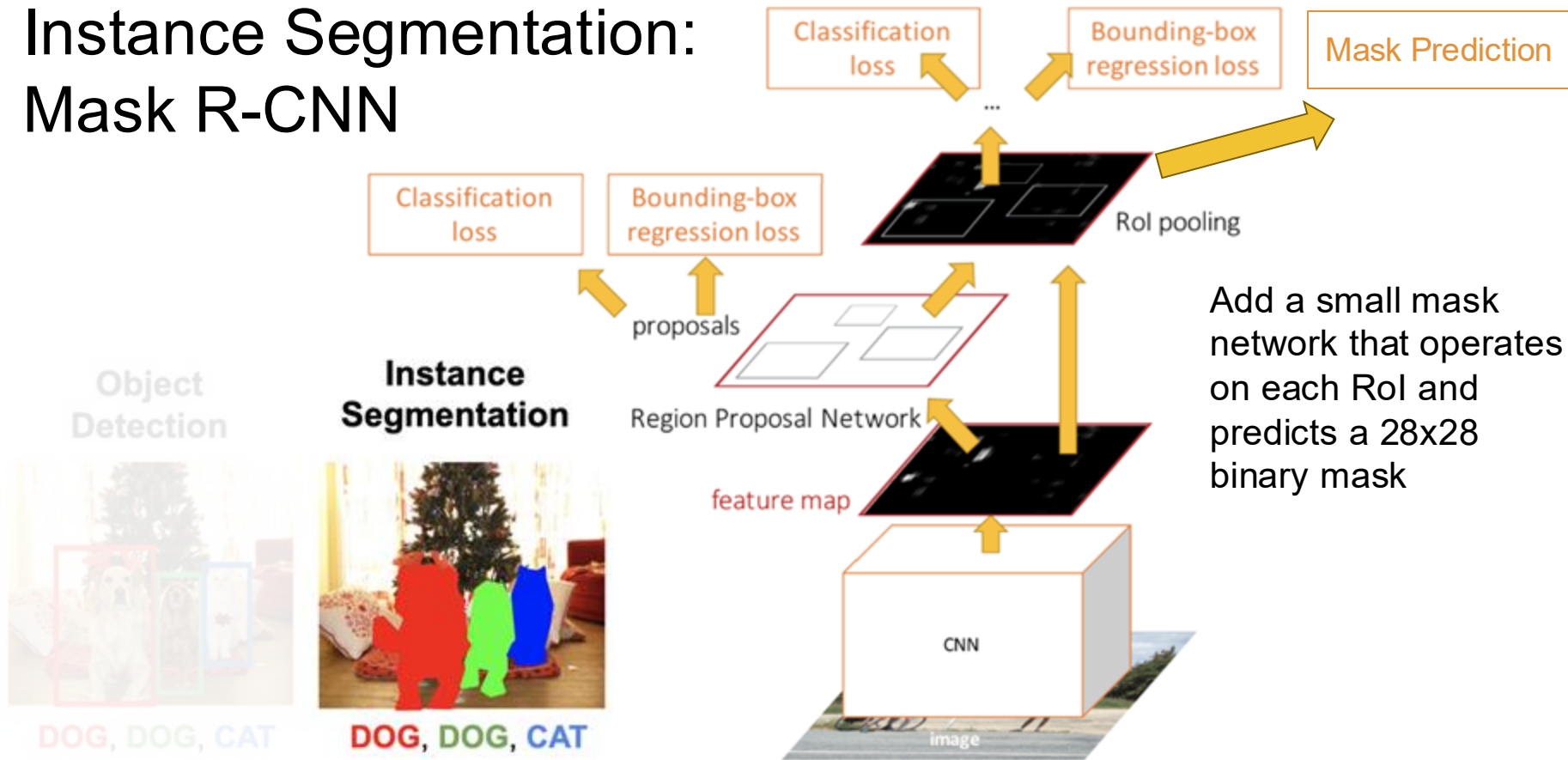


DOG, DOG, CAT

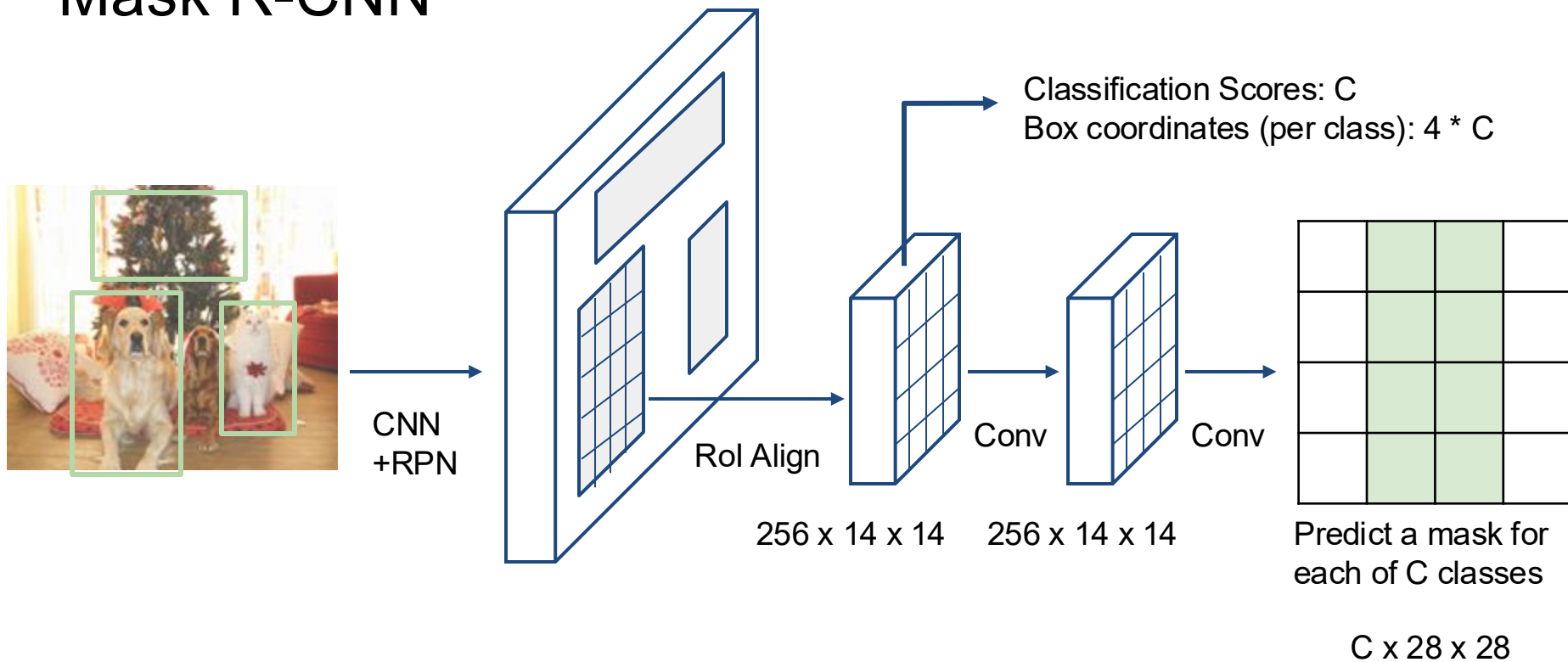
Object Detection: Faster R-CNN



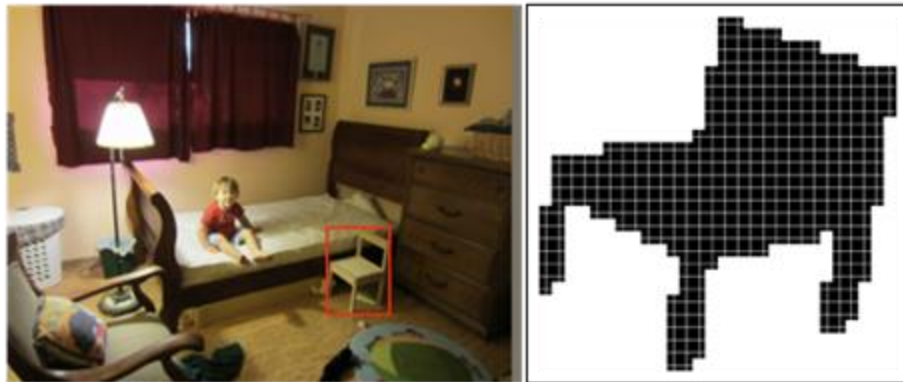
Instance Segmentation: Mask R-CNN



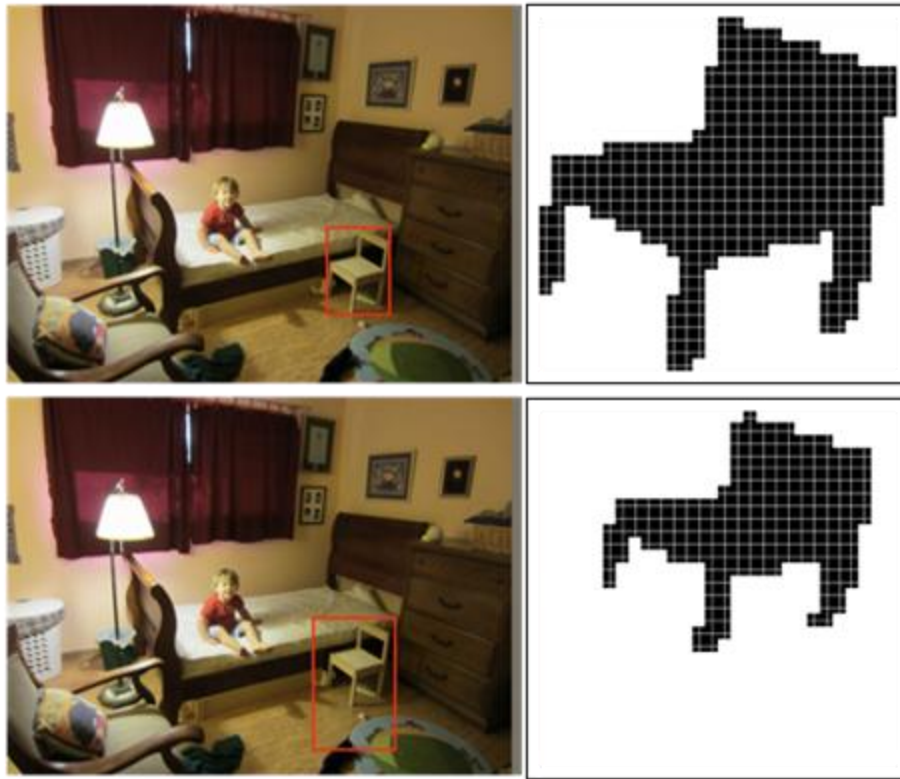
Mask R-CNN



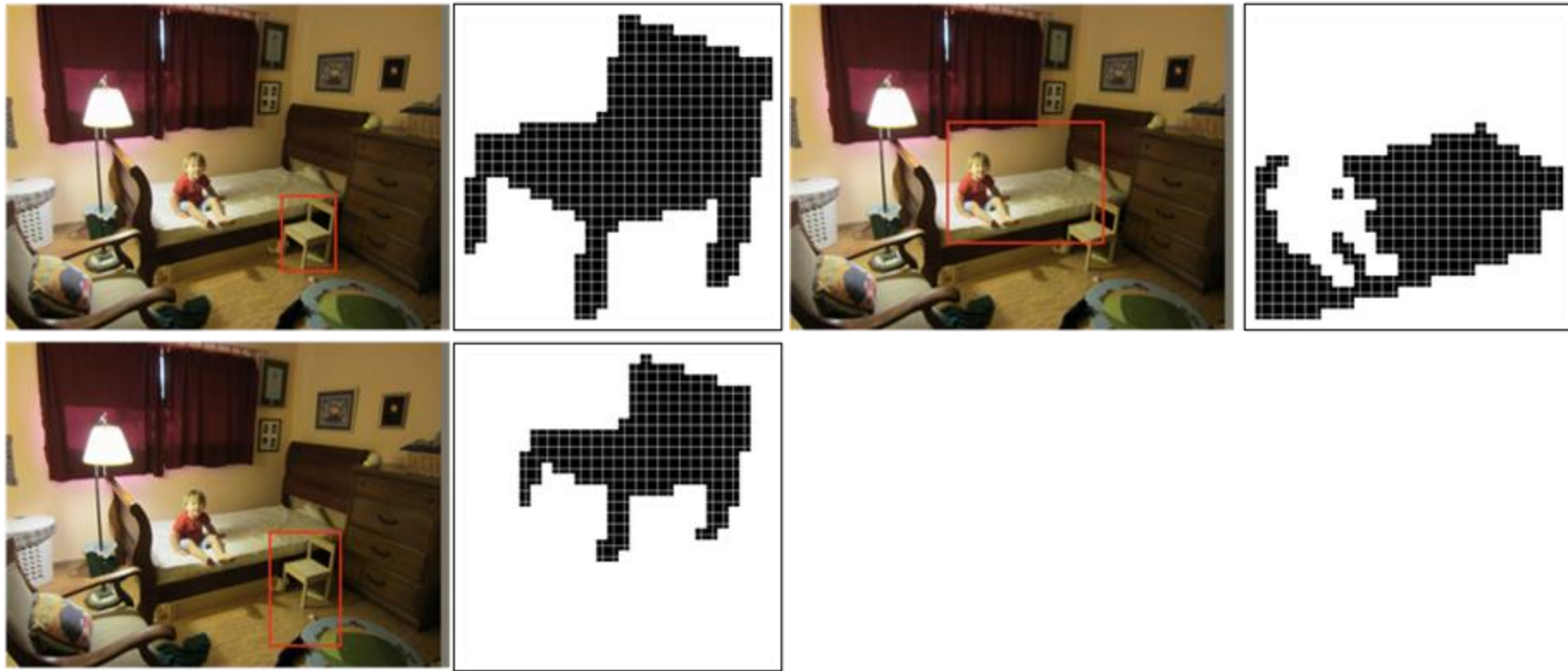
Mask R-CNN: Example Mask Training Targets



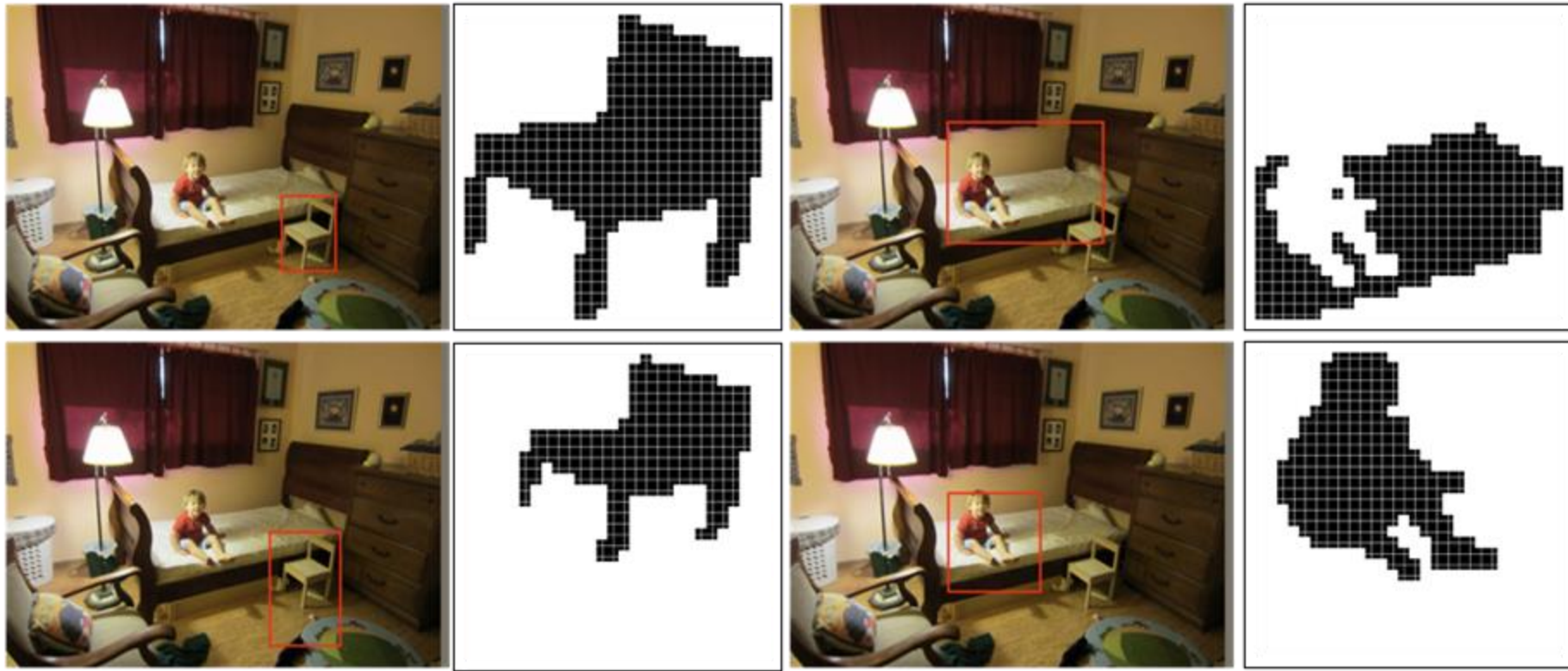
Mask R-CNN: Example Mask Training Targets



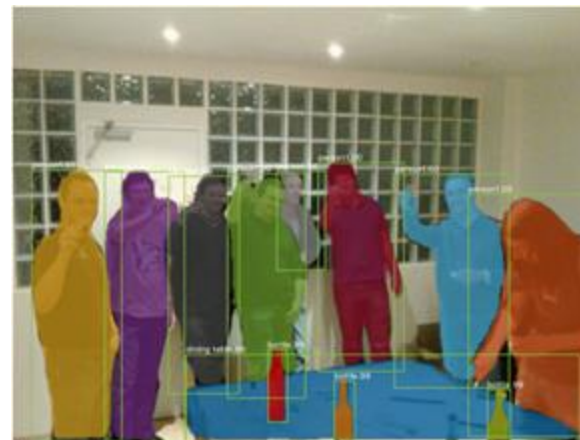
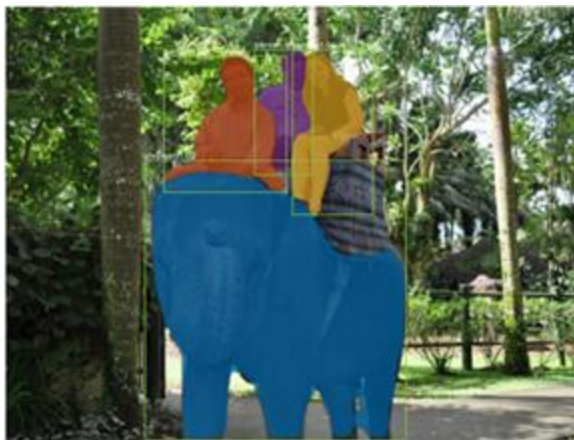
Mask R-CNN: Example Mask Training Targets



Mask R-CNN: Example Mask Training Targets

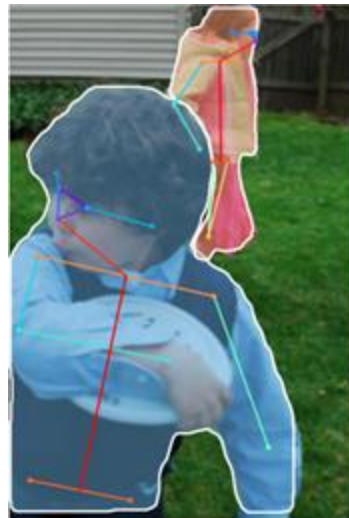
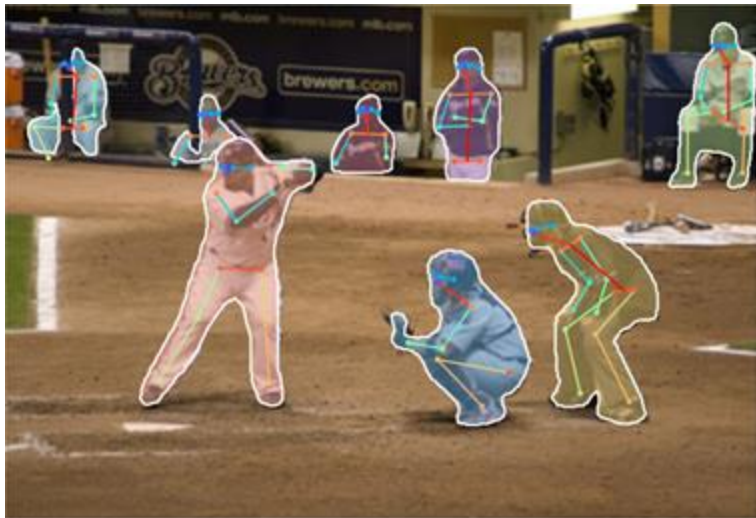


Mask R-CNN: Very Good Results!



Mask R-CNN

Also does pose

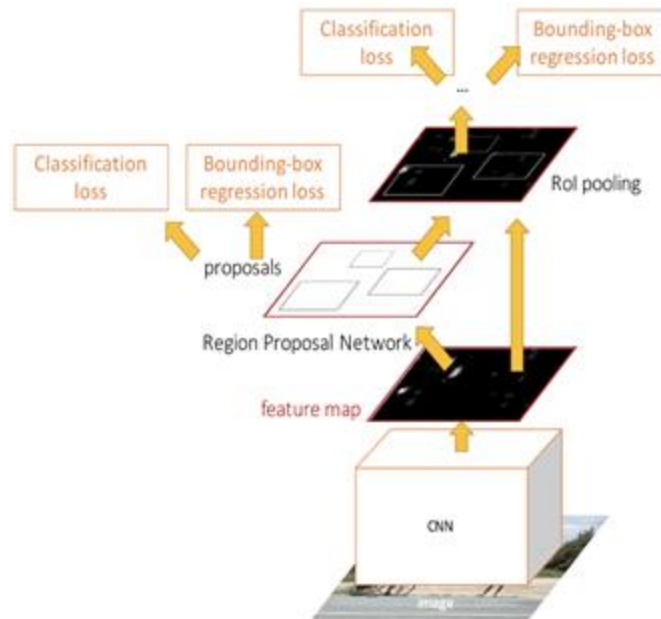


RCNN Series

- **R-CNN**: Per-region detection, hand-crafted region proposal
- **Fast R-CNN**: Shared feature extraction, RoI Pooling, Anchors
- **Faster R-CNN**: Region Proposal Networks, RoI Align
- **Mask R-CNN**: Instance Segmentation

Detectors are becoming more complex!
Many hyperparameters to tune for each
components ...

Can we simplify it?



End-to-End Object Detection with Transformers

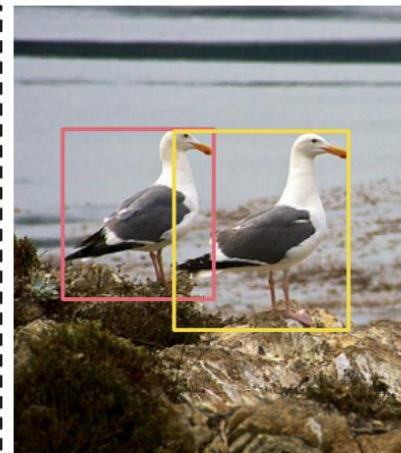
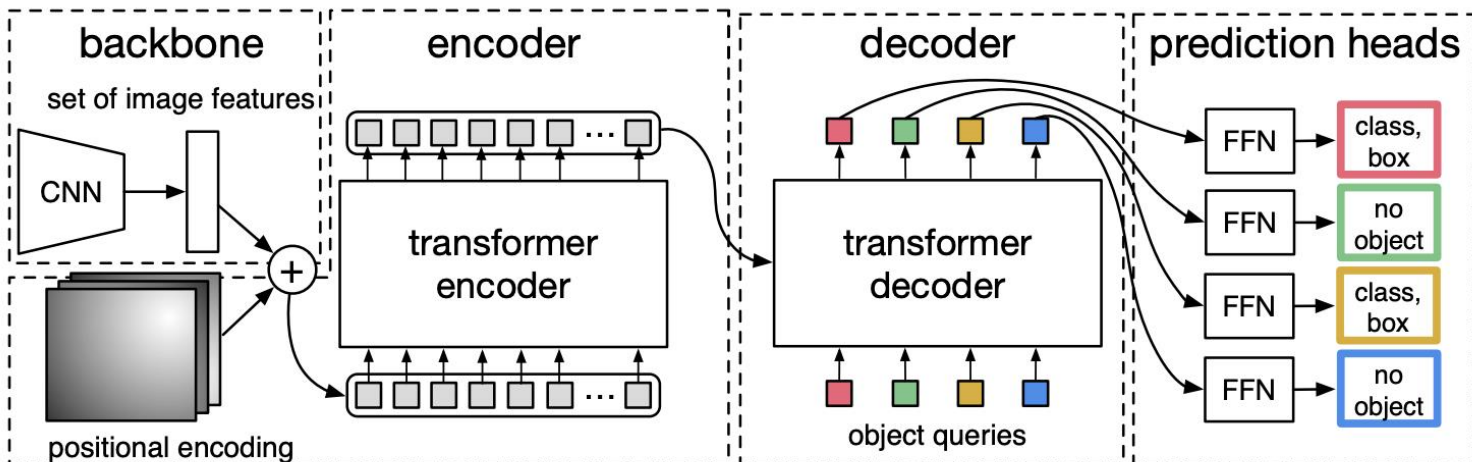
, Nicolas Carion*, Francisco Massa*, Gabriel Synnaeve, Nicolas Usunier,
Alexander Kirillov, and Sergey Zagoruyko

Facebook AI

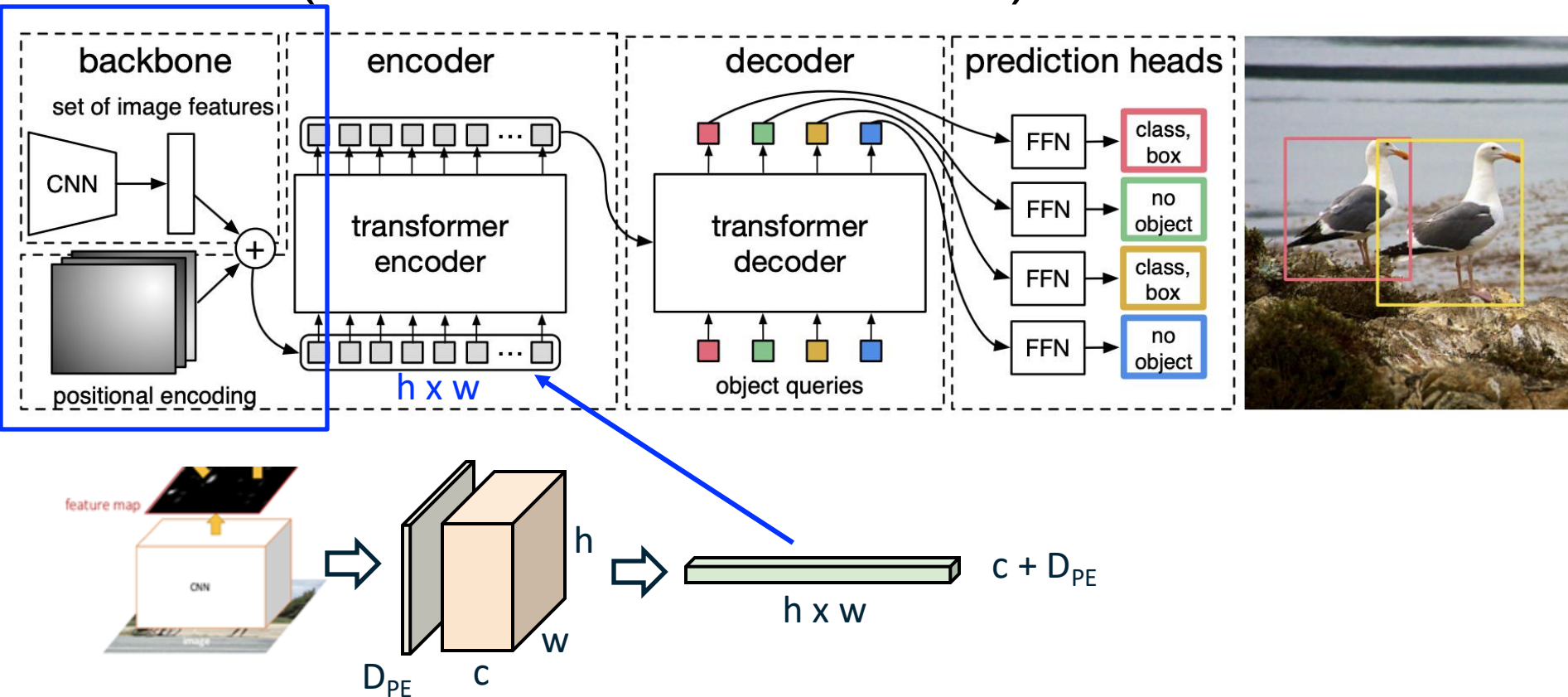
Key ideas:

- Detection as a **set-to-set prediction** problem
- Use Transformer to model the detection problem

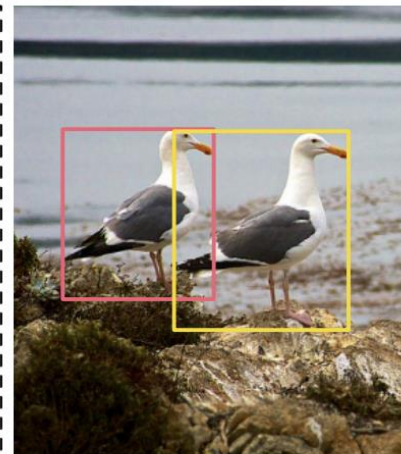
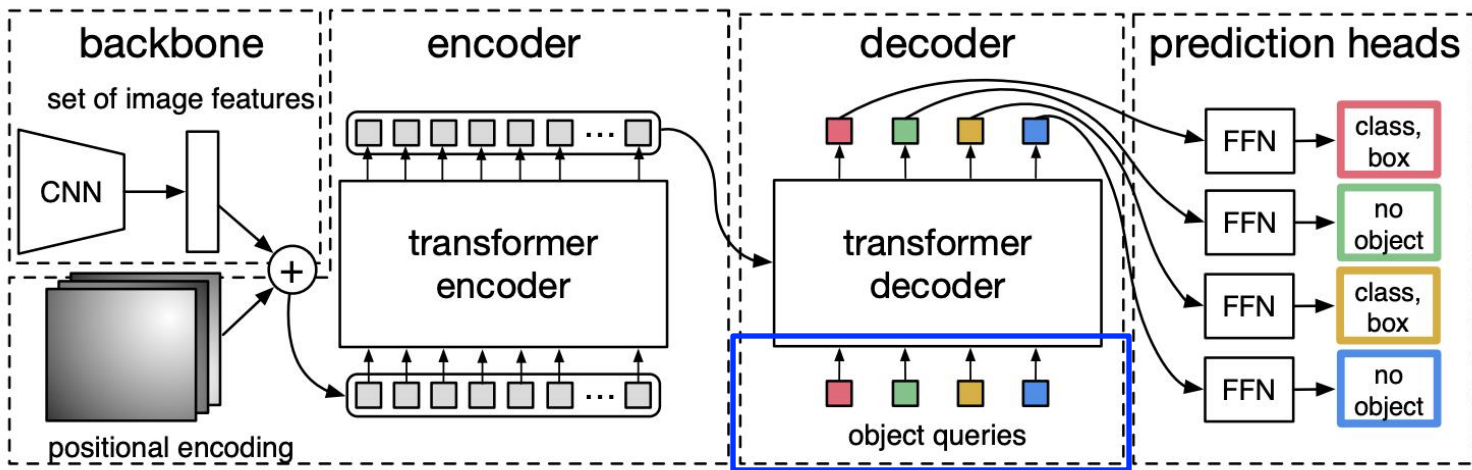
DETR (DEtection TRansformer)



DETR (DEtection TRansformer)



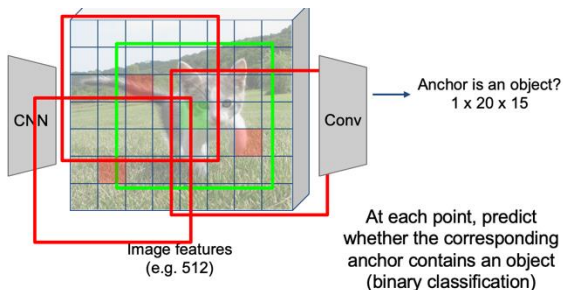
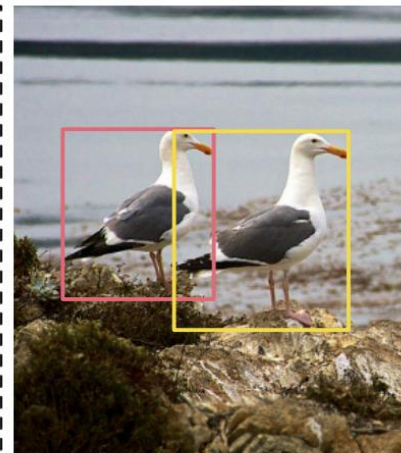
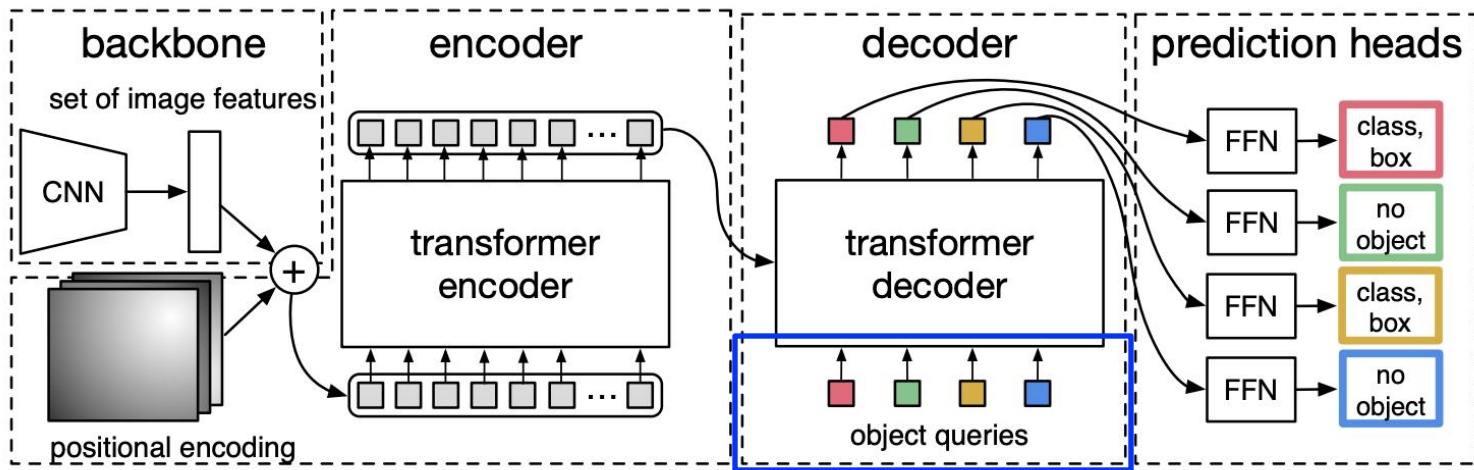
DETR (DEtection TRansformer)



A fixed set of *learnable embeddings*,
e.g., 300 size-N vectors

Q: Why?

DETR (DEtection TRansformer)



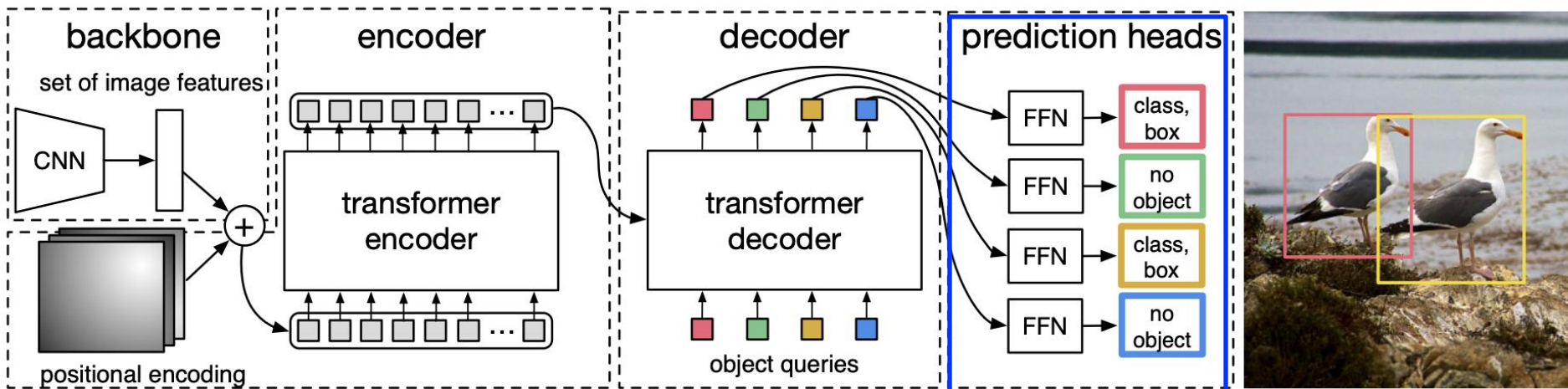
A fixed set of learnable embeddings,
e.g., 300 size-N vectors

Q: Why?

A: Break the symmetry of predictions, so
that each prediction is different.

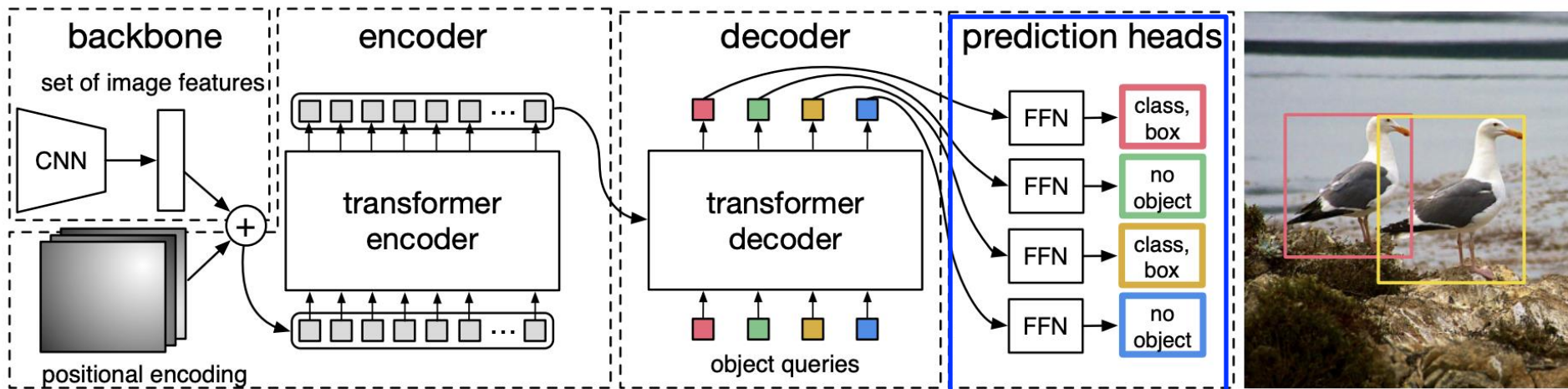
Analogous to anchors in *R-CNN, but **no
spatial location**

DETR (DEtection TRansformer)



Problem: We don't know which query corresponds to which ground truth during training! We can't predetermine a fixed order like in sequence decoding.

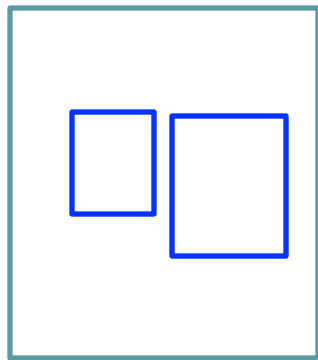
DETR (DEtection TRansformer)



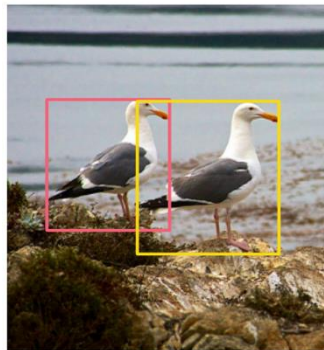
Problem: We don't know which query corresponds to which ground truth during training! We can't predetermine a fixed order like in sequence decoding.

Solution: Set matching loss --- train your model to generate a set of predictions that matches ground truth regardless of its order.

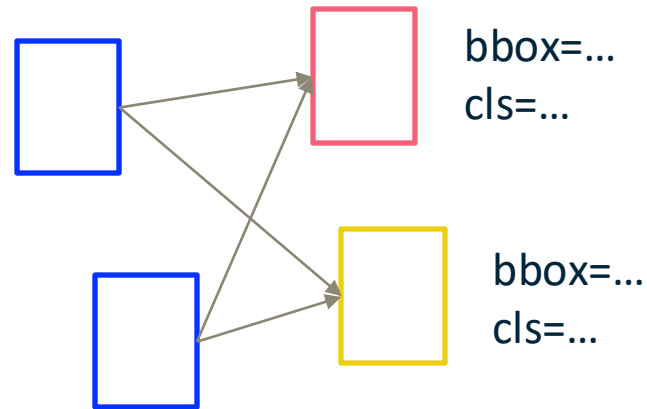
Hungarian Loss (Set Matching Loss)



Prediction



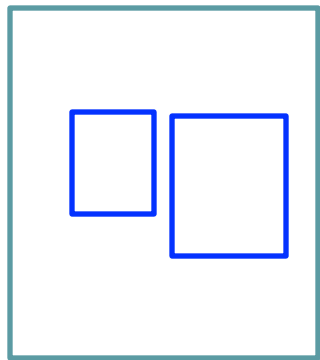
Ground Truth



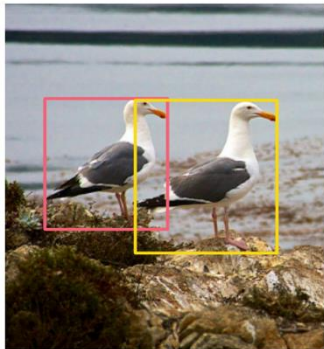
Goal: minimize bipartite distance

Problem: each query should be trained to match one ground truth. We don't know the matching!

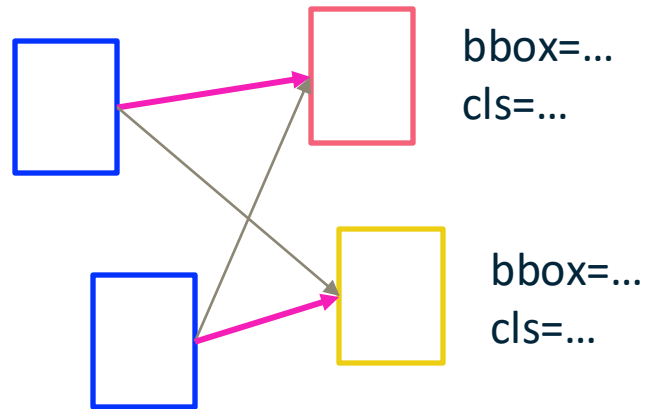
Hungarian Loss (Set Matching Loss)



Prediction



Ground Truth



Goal: minimize bipartite distance

1. **Hungarian matching:** find the **minimum-loss bipartite matching** between prediction and ground truth **given the current prediction**.
2. **Minimize matched loss:** Given the matched prediction and ground truth, minimize the detection loss (bounding box distance and classification CE loss)

DETR vs. FasterRCNN

Model	GFLOPS/FPS	#params	AP	AP ₅₀	AP ₇₅	AP _S	AP _M	AP _L
Faster RCNN-DC5	320/16	166M	39.0	60.5	42.3	21.4	43.5	52.5
Faster RCNN-FPN	180/26	42M	40.2	61.0	43.8	24.2	43.5	52.0
Faster RCNN-R101-FPN	246/20	60M	42.0	62.5	45.9	25.2	45.6	54.6
Faster RCNN-DC5+	320/16	166M	41.1	61.4	44.3	22.9	45.9	55.0
Faster RCNN-FPN+	180/26	42M	42.0	62.1	45.5	26.6	45.4	53.4
Faster RCNN-R101-FPN+	246/20	60M	44.0	63.9	47.8	27.2	48.1	56.0
DETR	86/28	41M	42.0	62.4	44.2	20.5	45.8	61.1
DETR-DC5	187/12	41M	43.3	63.1	45.9	22.5	47.3	61.1
DETR-R101	152/20	60M	43.5	63.8	46.4	21.9	48.0	61.8
DETR-DC5-R101	253/10	60M	44.9	64.7	47.7	23.7	49.5	62.3

Similar size, simpler, and (mostly) better!

We are still detecting a fixed number of object with finite vocabulary ...

Segment Anything

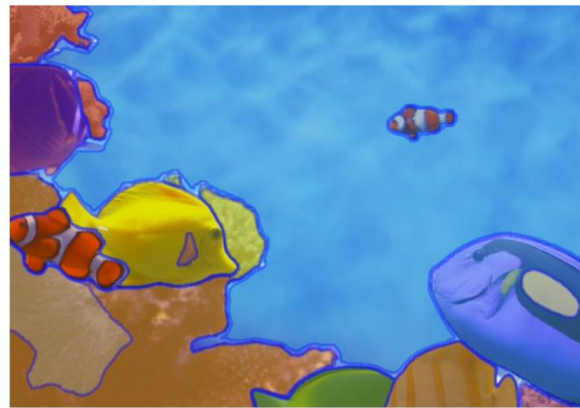
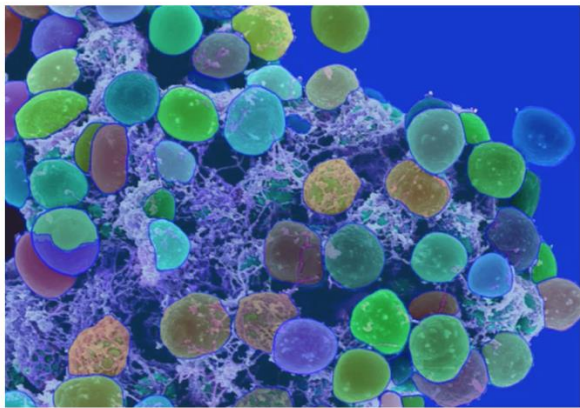
Alexander Kirillov^{1,2,4} Eric Mintun² Nikhila Ravi^{1,2} Hanzi Mao² Chloe Rolland³ Laura Gustafson³
Tete Xiao³ Spencer Whitehead Alexander C. Berg Wan-Yen Lo Piotr Dollár⁴ Ross Girshick⁴
¹project lead ²joint first author ³equal contribution ⁴directional lead

Meta AI Research, FAIR

Key ideas:

- Query-based prediction instead of fixed set-to-set prediction
- Large-scale training data with auto-labeling

Foundation Image Segmentation Models



SegmentAnything (Meta AI, 2023)

Try it yourself! <https://segment-anything.com/demo#>

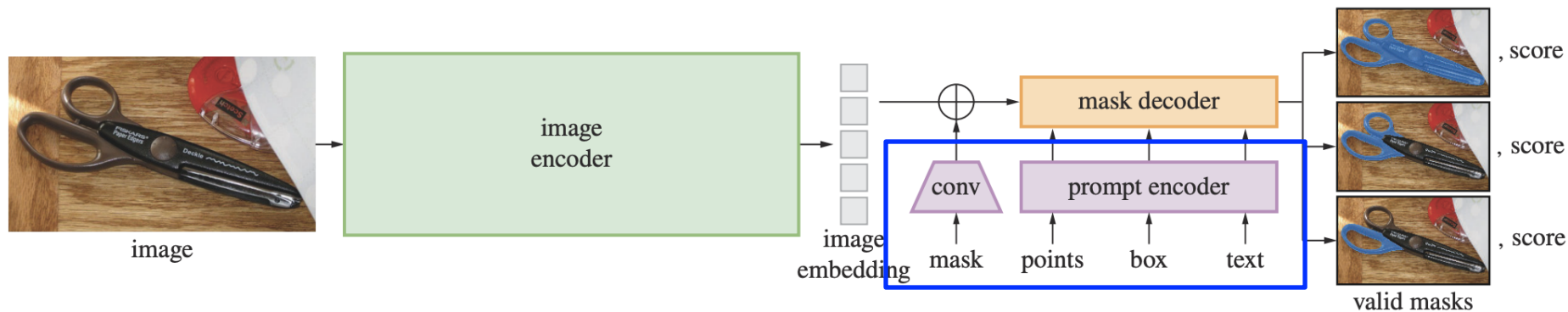
Foundation Image Segmentation Models



SegmentAnything (Meta AI, 2023)

Try it yourself! <https://segment-anything.com/demo#>

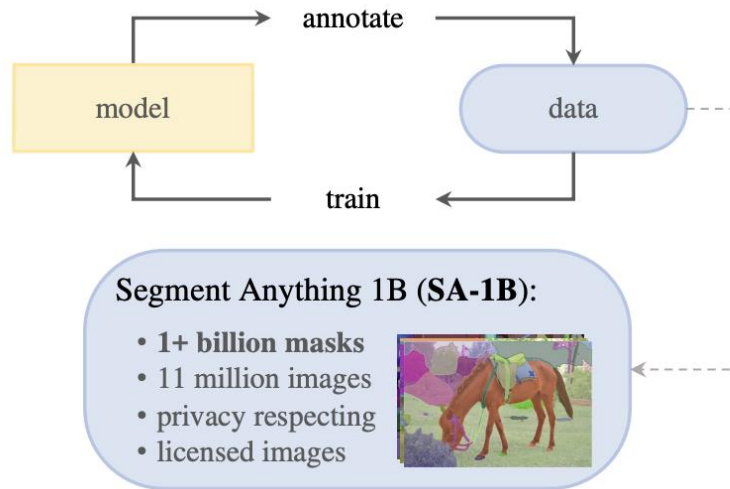
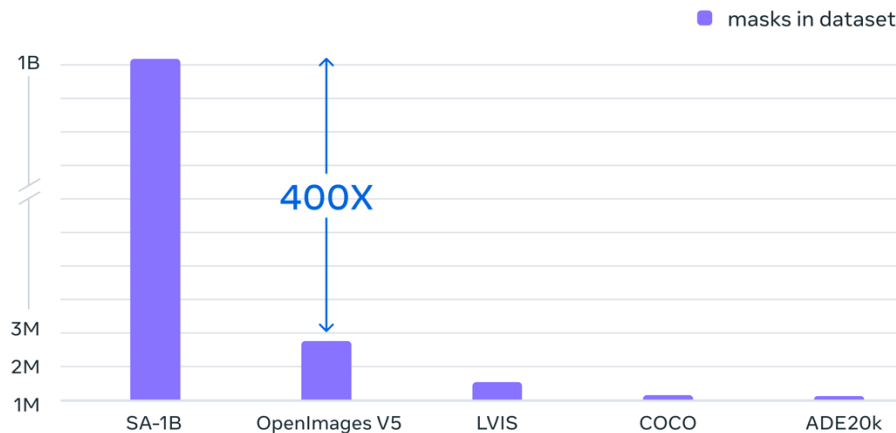
Foundation Image Segmentation Models



No more learned embeddings. Query anything you want!

SegmentAnything (Meta AI, 2023)

Foundation Image Segmentation Models



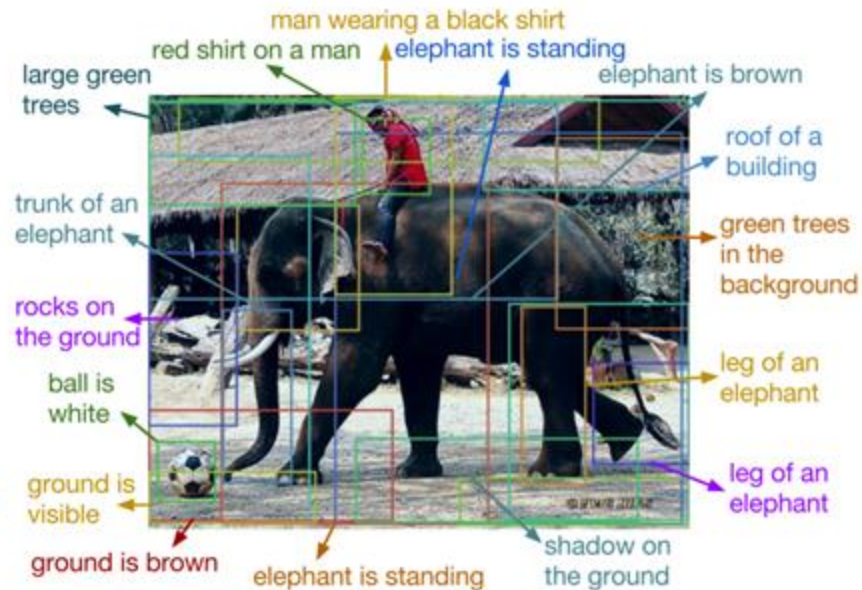
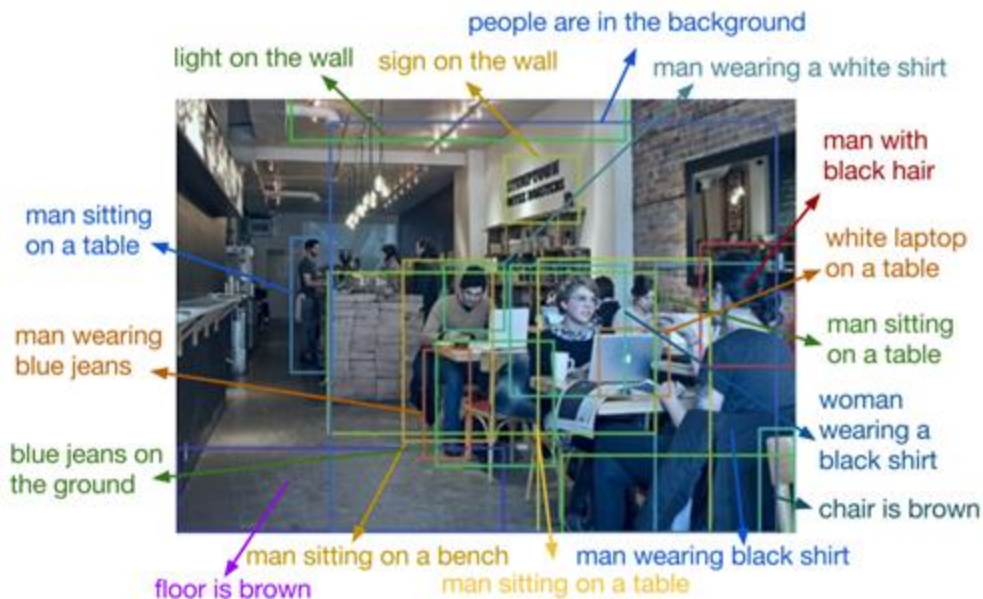
SegmentAnything (Meta AI, 2023)

Summary: Segmentation and Detection

- Object segmentation and detection are most common application of computer vision research.
- They have driven decades of advancement in Autonomous Vehicles, Robotics, traffic analytics, and basically any devices that have camera and adequate computing power (e.g., Smart Phone)
- Segmentation and Detection with DNNs evolved through similar paths (sliding window, feature sharing, input-output, alignment etc.)
- We have a new wave of foundation detection and segmentation models driven by Transformer + ConvNet + large dataset

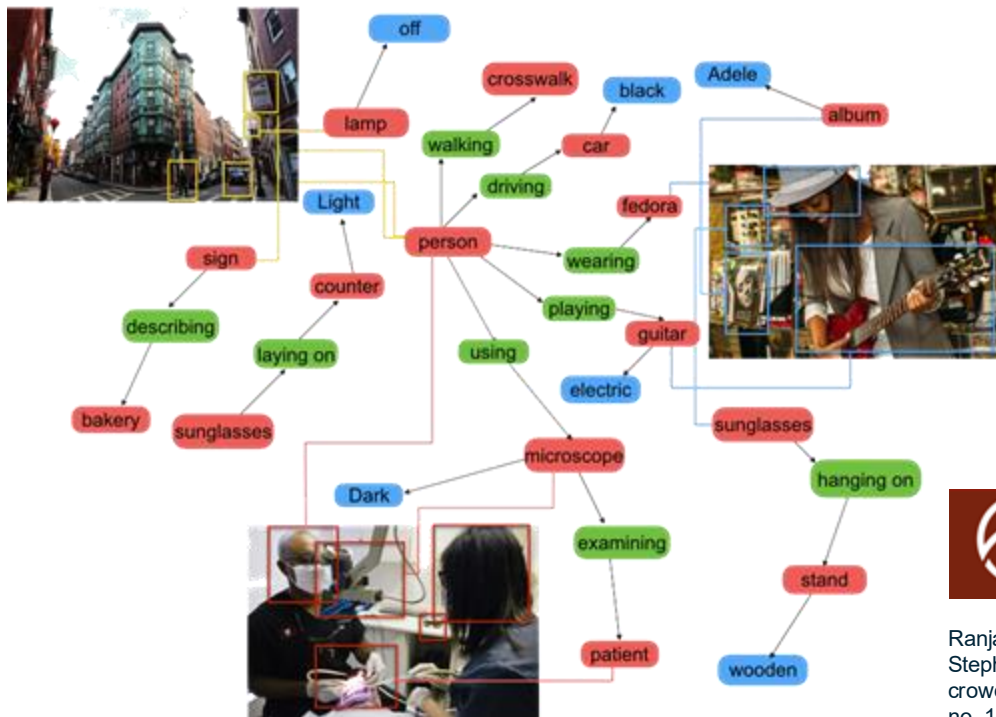
Beyond 2D Object Detection...

Object Detection + Captioning = Dense Captioning



Johnson, Karpathy, and Fei-Fei, "DenseCap: Fully Convolutional Localization Networks for Dense Captioning", CVPR 2016
Figure copyright IEEE, 2016. Reproduced for educational purposes.

Objects + Relationships = Scene Graphs



108,077 Images

5.4 Million Region Descriptions

1.7 Million Visual Question Answers

3.8 Million Object Instances

2.8 Million Attributes

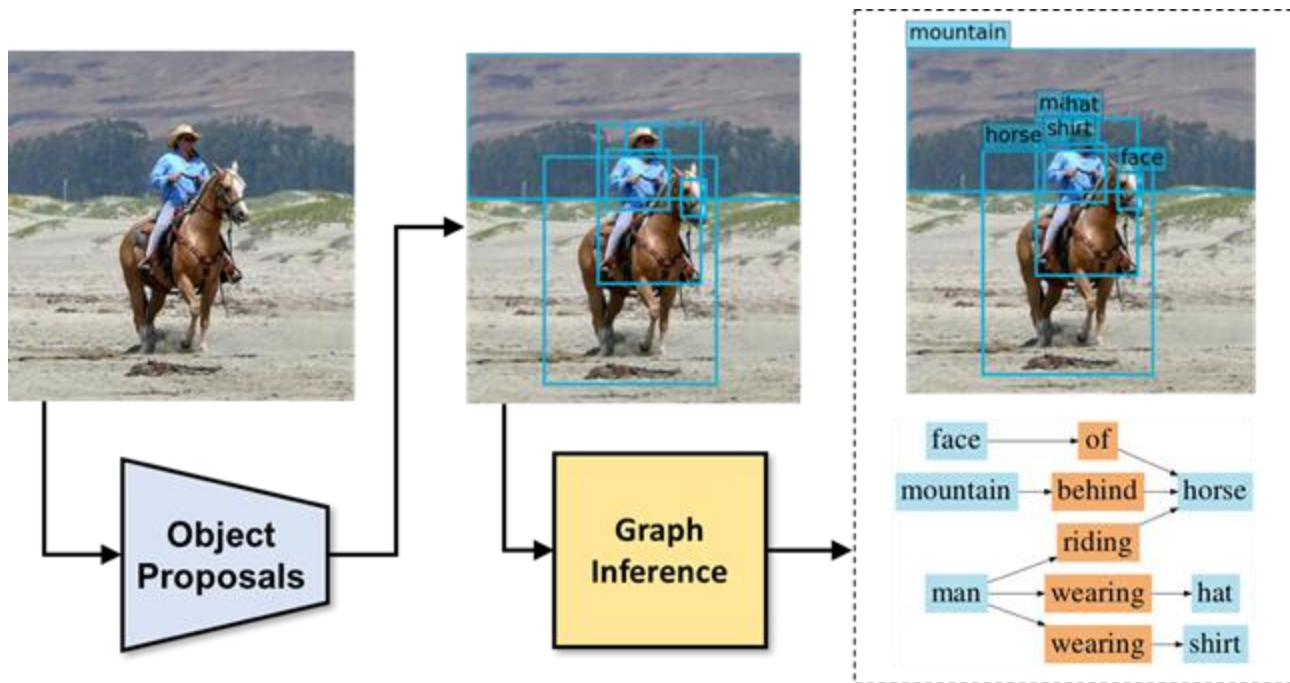
2.3 Million Relationships

Everything Mapped to Wordnet Synsets



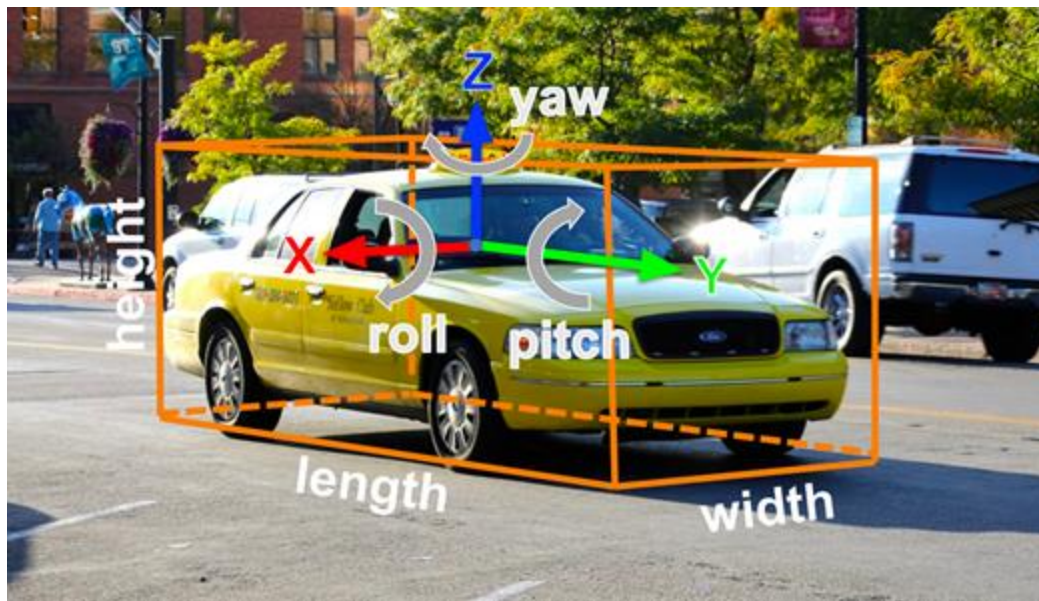
Ranjay Krishna, Yuke Zhu, Oliver Groth, Justin Johnson, Kenji Hata, Joshua Kravitz, Stephanie Chen et al. "Visual genome: Connecting language and vision using crowdsourced dense image annotations." International Journal of Computer Vision 123, no. 1 (2017): 32-73.

Scene Graph Prediction



Xu, Zhu, Choy, and Fei-Fei, "Scene Graph Generation by Iterative Message Passing", CVPR 2017
Figure copyright IEEE, 2018. Reproduced for educational purposes.

3D Object Detection



2D Object Detection:

2D bounding box

(x, y, w, h)

3D Object Detection:

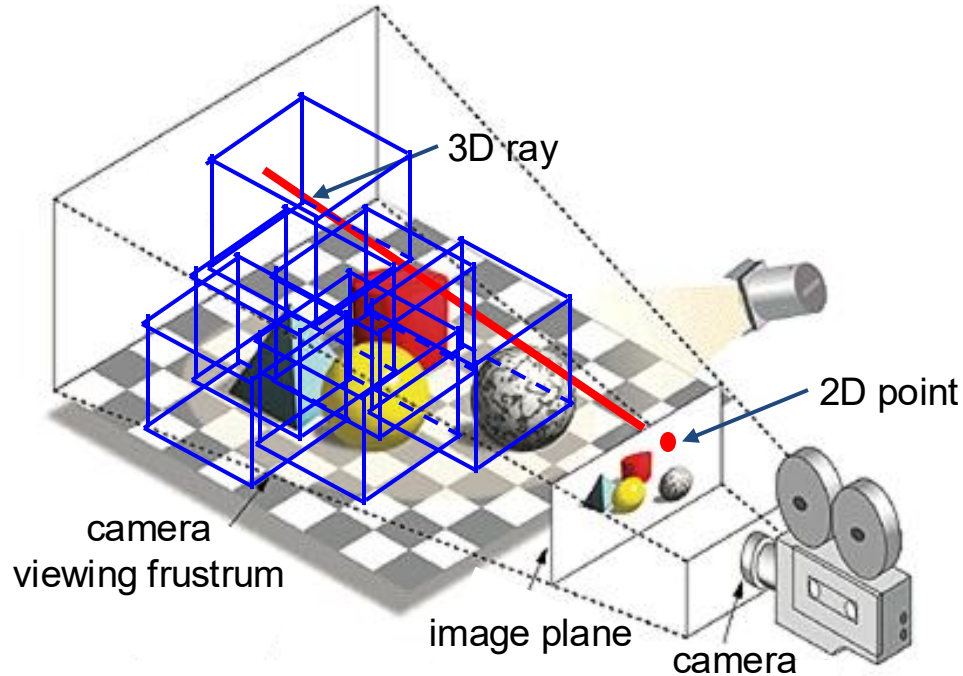
3D oriented bounding box

$(x, y, z, w, h, l, r, p, y)$

Simplified bbox: no roll & pitch

Much harder problem than 2D
object detection!

3D Object Detection: Simple Camera Model

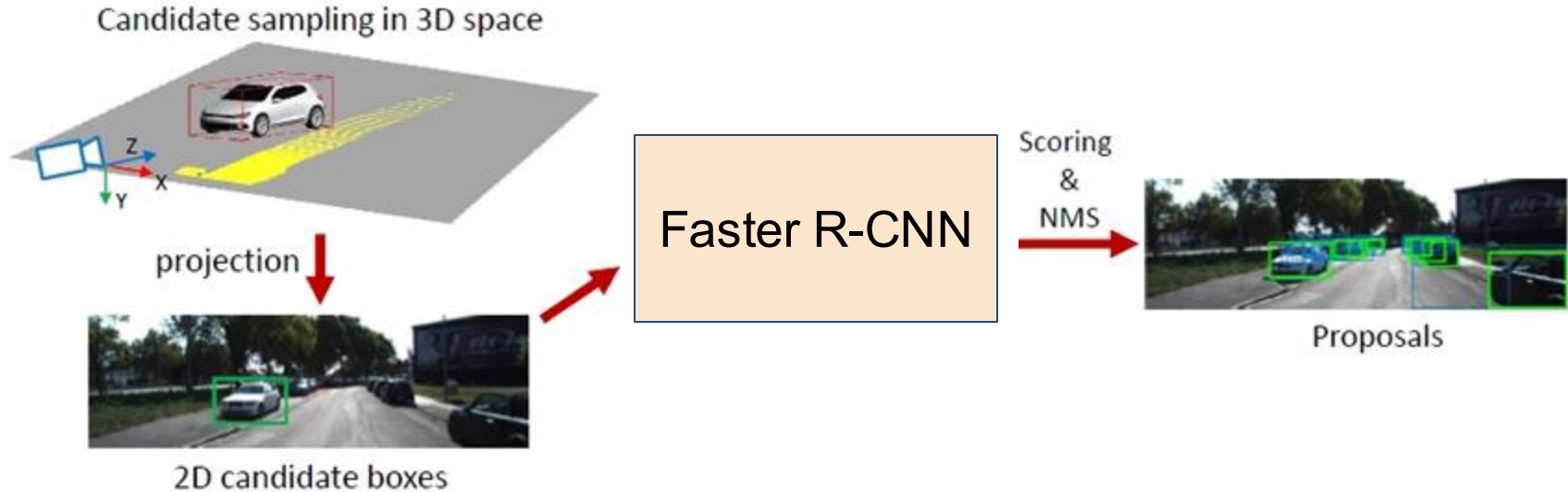


A point on the image plane corresponds to a **ray** in the 3D space

A 2D bounding box on an image is a **frustum** in the 3D space

Localize an object in 3D:
The object can be anywhere in the **camera viewing frustum**!

3D Object Detection: Monocular Camera



- Same idea as Faster RCNN, but proposals are in 3D
- 3D bounding box proposal, regress 3D box parameters + class score

Chen, Xiaozi, Kaustav Kundu, Ziyu Zhang, Huimin Ma, Sanja Fidler, and Raquel Urtasun. "Monocular 3d object detection for autonomous driving." CVPR 2016.

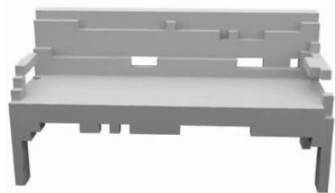
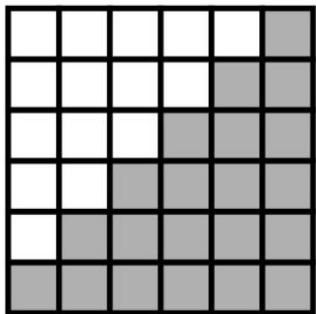
How to Represent 3D Data?



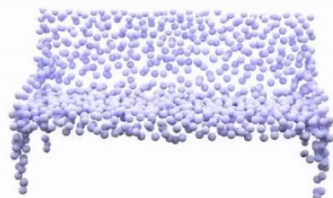
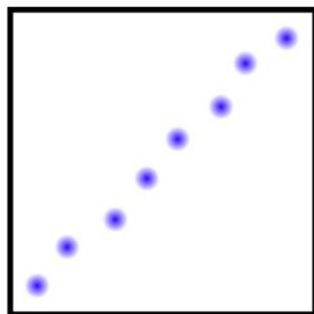
```
[[105 112 108 111 104 99 106 99 96 103 112 118 104 97 93 871  
[ 91 98 102 106 104 79 98 103 99 105 123 136 118 105 94 851  
[ 76 85 98 105 128 185 87 98 95 99 115 112 106 103 99 851  
[ 99 81 81 93 128 131 127 108 95 98 102 99 96 93 101 941  
[106 91 81 64 65 91 88 85 101 107 109 98 75 84 96 951  
[114 100 85 55 55 69 64 54 64 87 112 129 98 74 84 911  
[133 137 147 103 65 81 88 65 52 54 74 84 102 93 85 821  
[128 137 144 148 109 95 86 78 62 65 63 63 68 73 86 1011  
[125 133 148 137 119 121 117 94 65 79 88 65 54 64 72 981  
[127 125 131 147 133 127 126 131 111 96 89 75 61 64 72 841  
[115 114 109 123 158 148 131 118 133 109 100 92 74 65 72 781  
[ 89 93 98 97 108 147 131 118 113 114 113 109 106 95 77 801  
[ 63 77 98 81 77 79 102 123 117 115 117 125 138 115 871  
[ 62 65 82 89 78 71 88 101 124 126 119 101 103 114 131 1191  
[ 63 65 75 88 89 71 62 81 120 138 135 105 81 98 118 1181  
[ 87 65 71 87 106 95 69 45 76 138 126 107 92 94 105 1121  
[118 87 82 86 117 123 116 66 41 51 95 93 89 95 102 1071  
[154 146 112 88 82 128 124 104 76 48 45 68 88 101 102 1091  
[157 178 157 128 93 86 114 132 112 97 69 55 78 82 99 941  
[138 128 134 161 139 108 109 118 121 134 114 87 65 53 69 861  
[128 112 96 117 158 144 128 115 184 187 182 93 87 81 72 791  
[123 187 96 86 83 112 153 149 122 189 184 75 98 107 112 991  
[122 121 182 88 82 86 94 117 145 148 153 182 58 79 92 1871  
[122 164 148 183 71 56 78 83 93 183 119 139 182 61 69 841]]
```

?

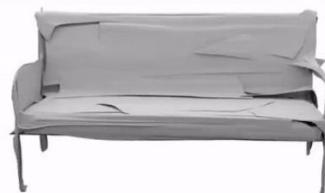
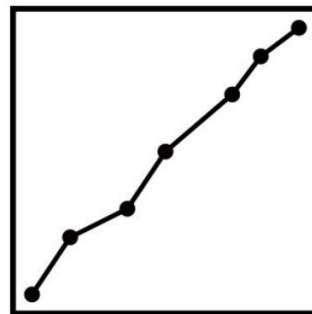
3D Representations



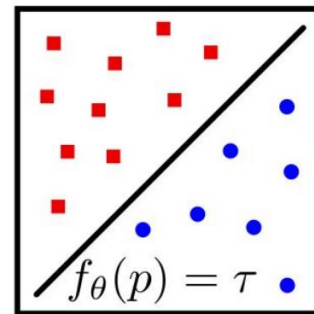
Occupancy Grid
[h, w, l]



Point Cloud
[num_pts, 3]

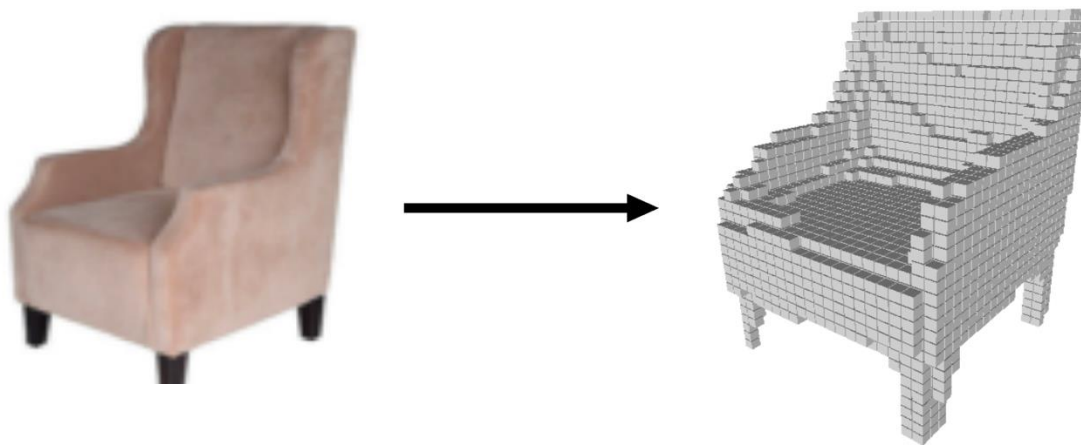


Surface Mesh
(edge list, face list, vertex list)



Implicit Functions
(x, y, z -> d)

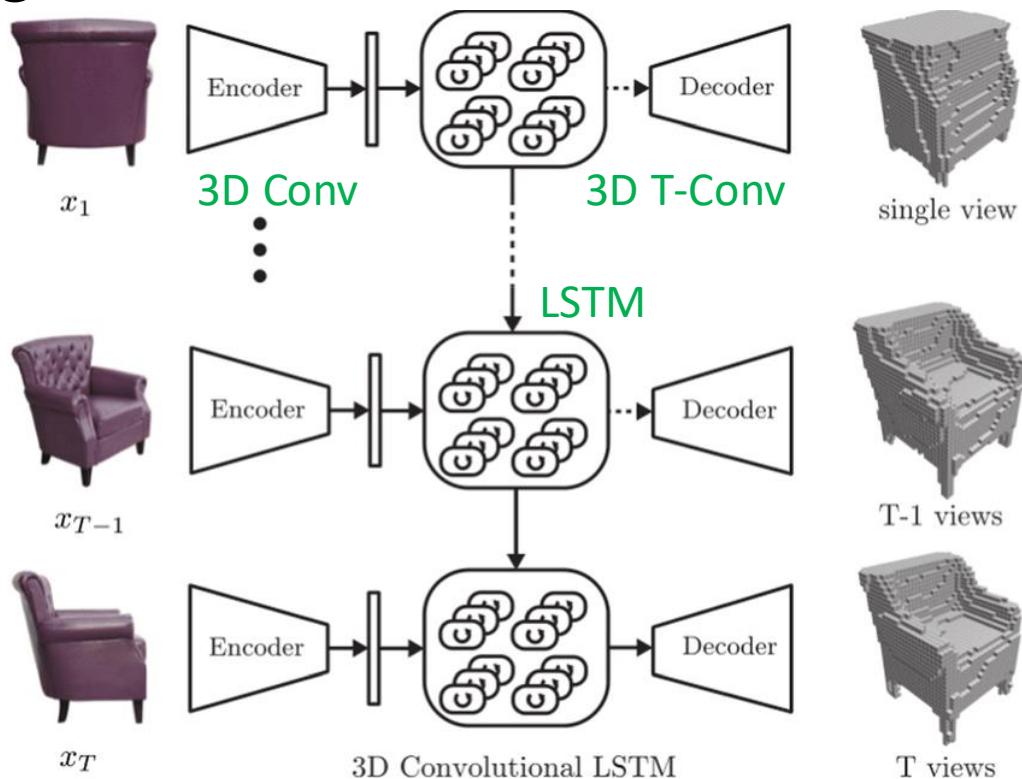
3D Occupancy Grid



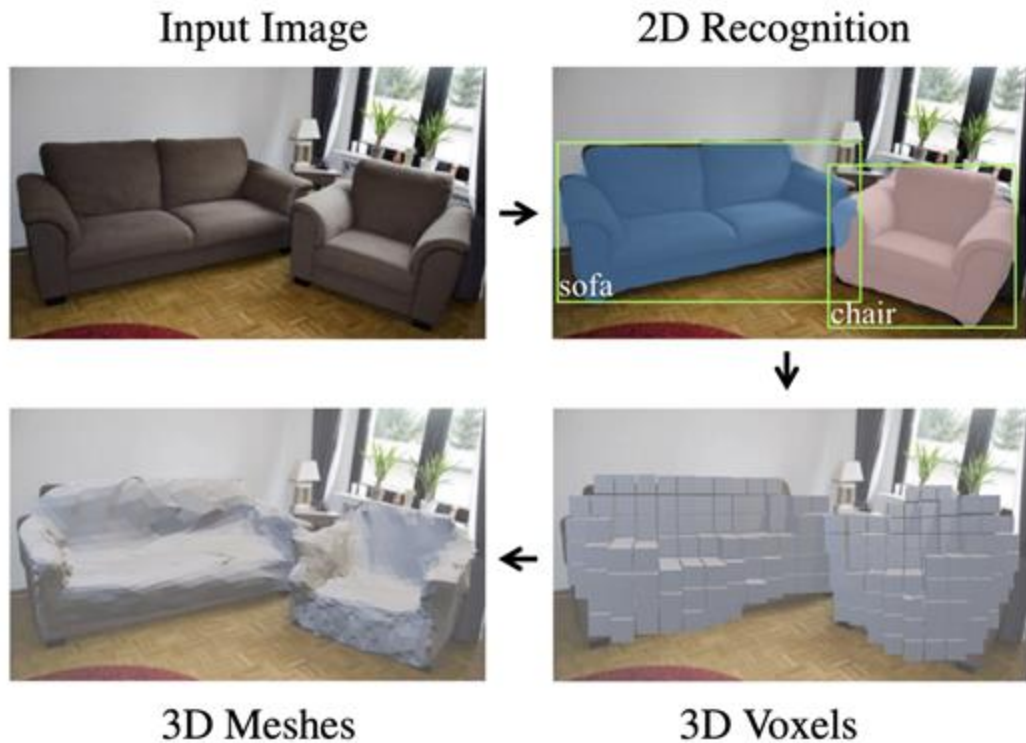
Represent the “occupancy” of objects in 3D space with a 3D voxel grid

- $V \in \{0, 1\}^{[H,W,L]}$
- Just like segmentation in Masked-RCNN, but in 3D!
- Conceptually simple
- Not trivial to scale to high-resolution shapes

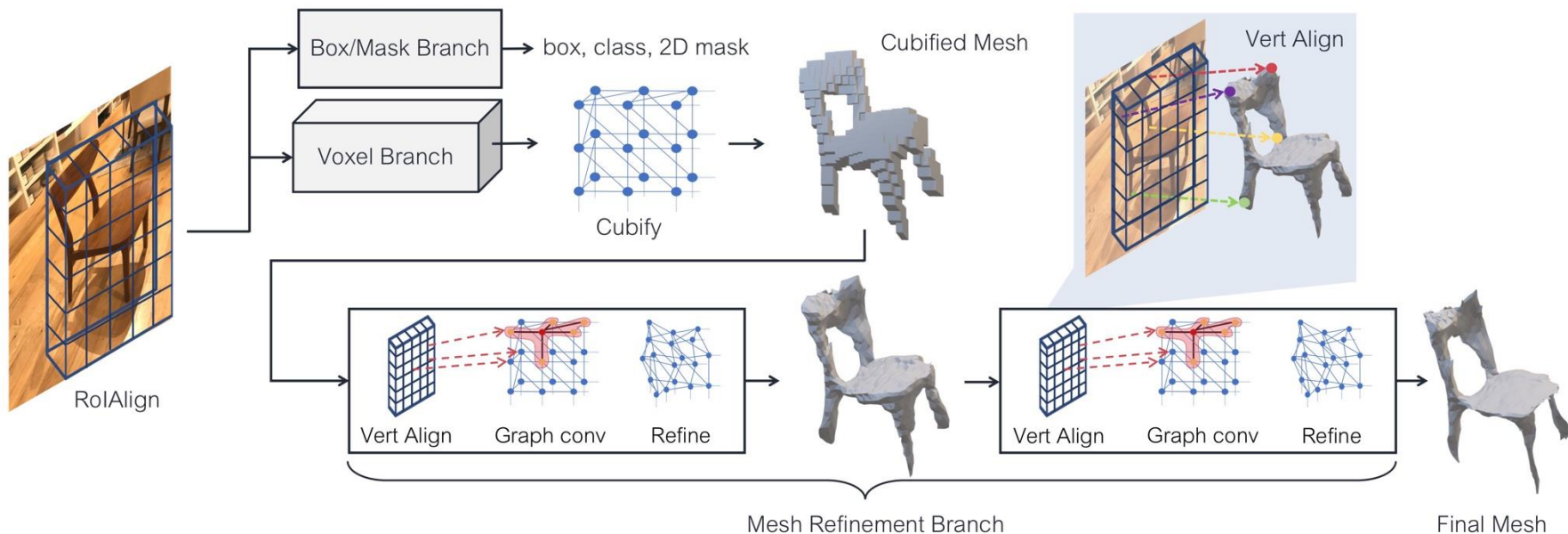
Predicting 3D Voxel Grid with 3D ConvNet



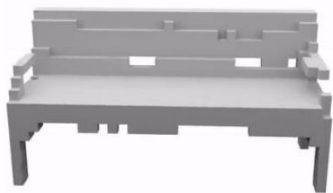
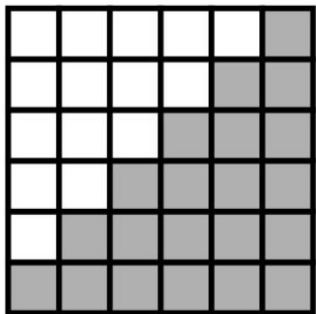
Detection + Reconstruction: Mesh R-CNN



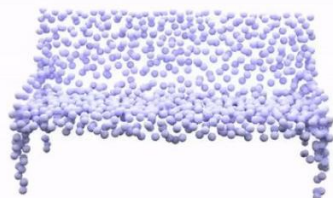
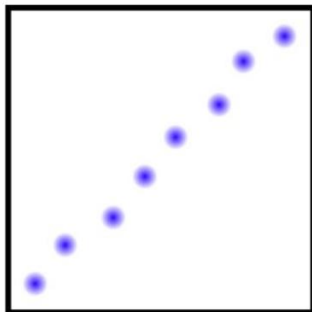
Detection + Reconstruction: Mesh R-CNN



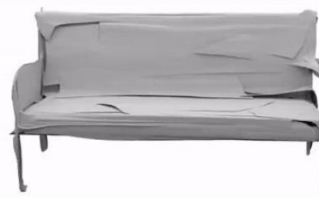
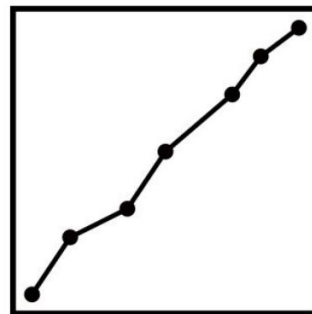
3D Representations



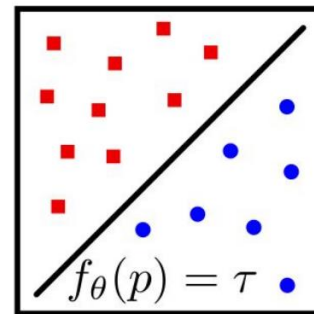
Occupancy Grid
[h, w, l]



Point Cloud
[num_pts, 3]



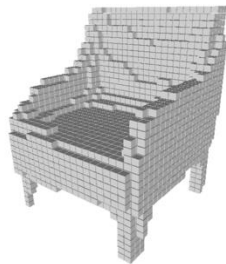
Surface Mesh
(edge list, face
list, vertex list)



Implicit Functions
(x, y, z -> d)

What is an implicit representation for 3D data?

Example: representing a 3D occupancy grid



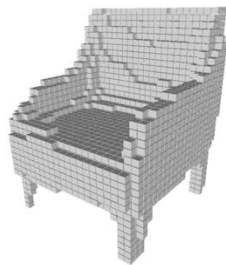
Explicit: A tensor of **3D voxel grid** $V \in \{0, 1\}^{[H,W,L]}$

Implicit: A **function** that maps locations to occupancies

$$F_{\theta}: x, y, z \rightarrow \{0, 1\}$$

What is an implicit representation for 3D data?

Example: representing a 3D occupancy grid



Explicit: A tensor of **3D voxel grid** $V \in \{0, 1\}^{[H,W,L]}$

Implicit: A **function** that maps locations to occupancies

$$F_{\theta}: x, y, z \rightarrow \{0, 1\}$$

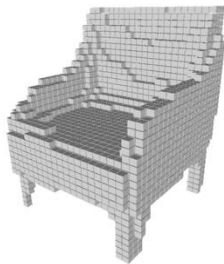
Implicit representation describes 3D shapes using **mathematical functions** rather than explicit voxels, points, or mesh.

Example: Signed Distance Function

$$F_{\theta}: \mathbb{R}^3 \rightarrow \mathbb{R}$$

What is an implicit representation for 3D data?

Example: representing a 3D occupancy grid



Explicit: A tensor of **3D voxel grid** $V \in \{0, 1\}^{[H,W,L]}$

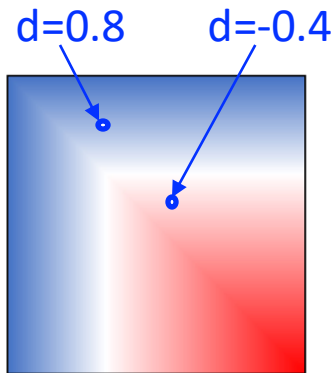
Implicit: A **function** that maps locations to occupancies

$$F_{\theta}: x, y, z \rightarrow \{0, 1\}$$

Implicit representation describes 3D shapes using **mathematical functions** rather than explicit voxels, points, or mesh.

Example: Signed Distance Function

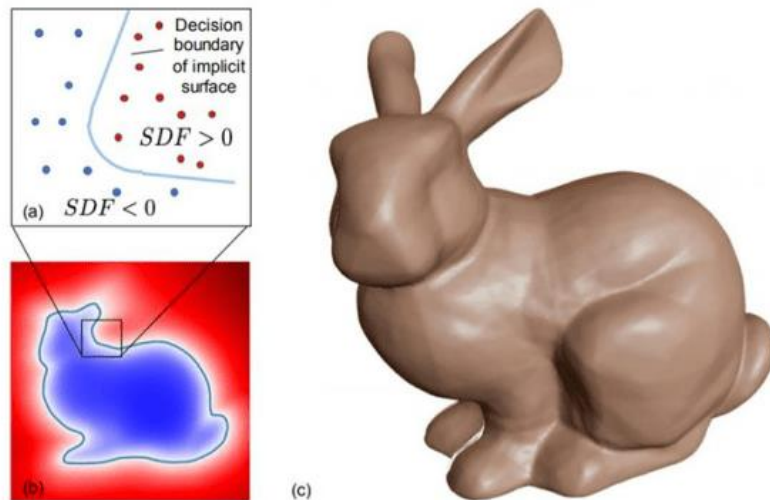
$$F_{\theta}: \mathbb{R}^N \rightarrow \mathbb{R}$$



How far is a point from the nearest surface, and is the point *inside or outside* of the shape?

SDF distance map

What is an implicit representation for 3D data?



DeepSDF representation applied to the Stanford Bunny: (a) depiction of the underlying implicit surface $SDF = 0$ trained on sampled points inside $SDF < 0$ and outside $SDF > 0$ the surface, (b) 2D cross-section of the signed distance field, (c) rendered 3D surface recovered from $SDF = 0$.

Can we train NNs to represent more than just geometry of a 3D shape?

Implicit 3D Representation: Beyond Geometry

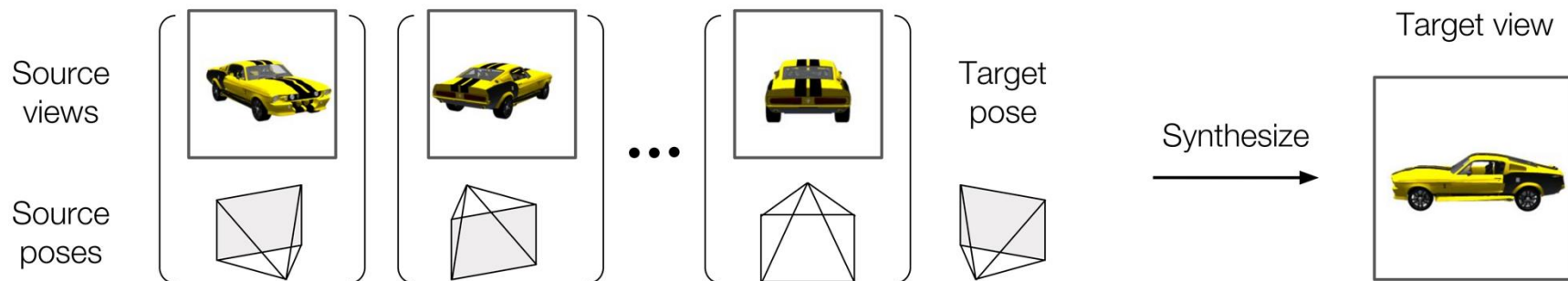


$$f_{\theta}(\text{viewpoint}) = \text{Image}$$

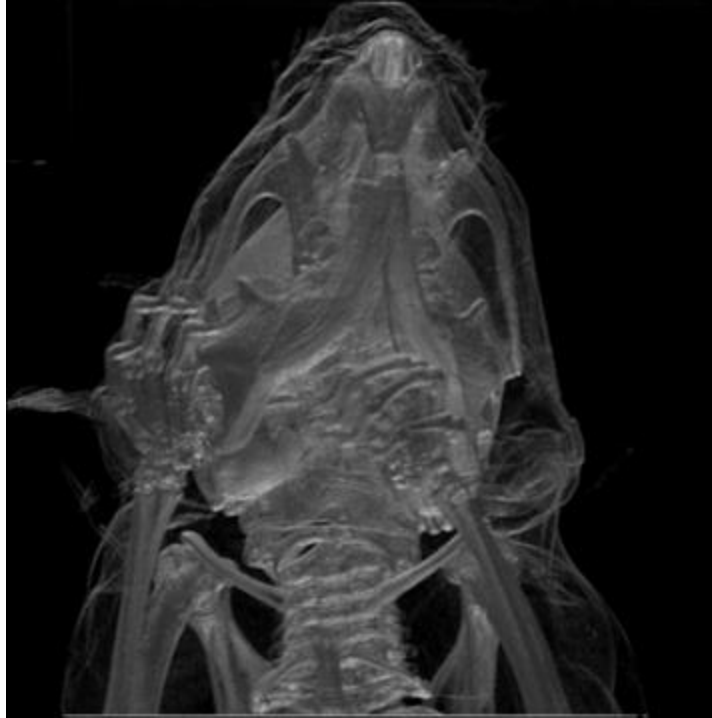
Goal: Learn an implicit 3D representation function that maps any camera viewpoint to full RGB images

Can we implicitly represent a full 3D scene, including its fine-grained geometry (e.g., surface occupancy) and appearance?

Problem: Novel View Synthesis



Basics: Volume Rendering

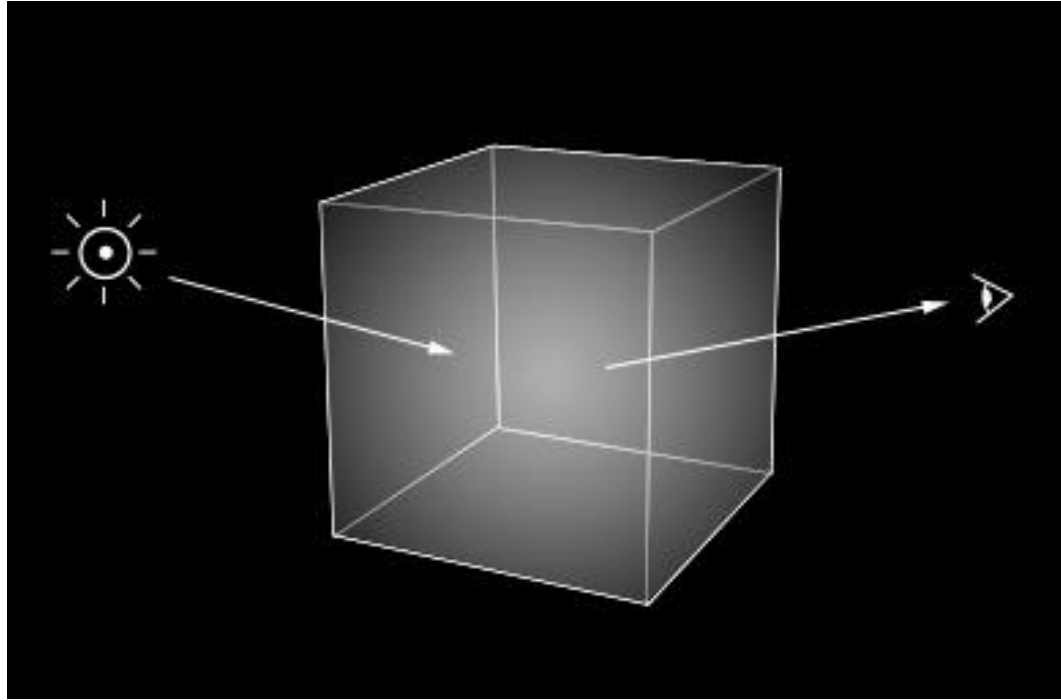


https://en.wikipedia.org/wiki/Volume_rendering

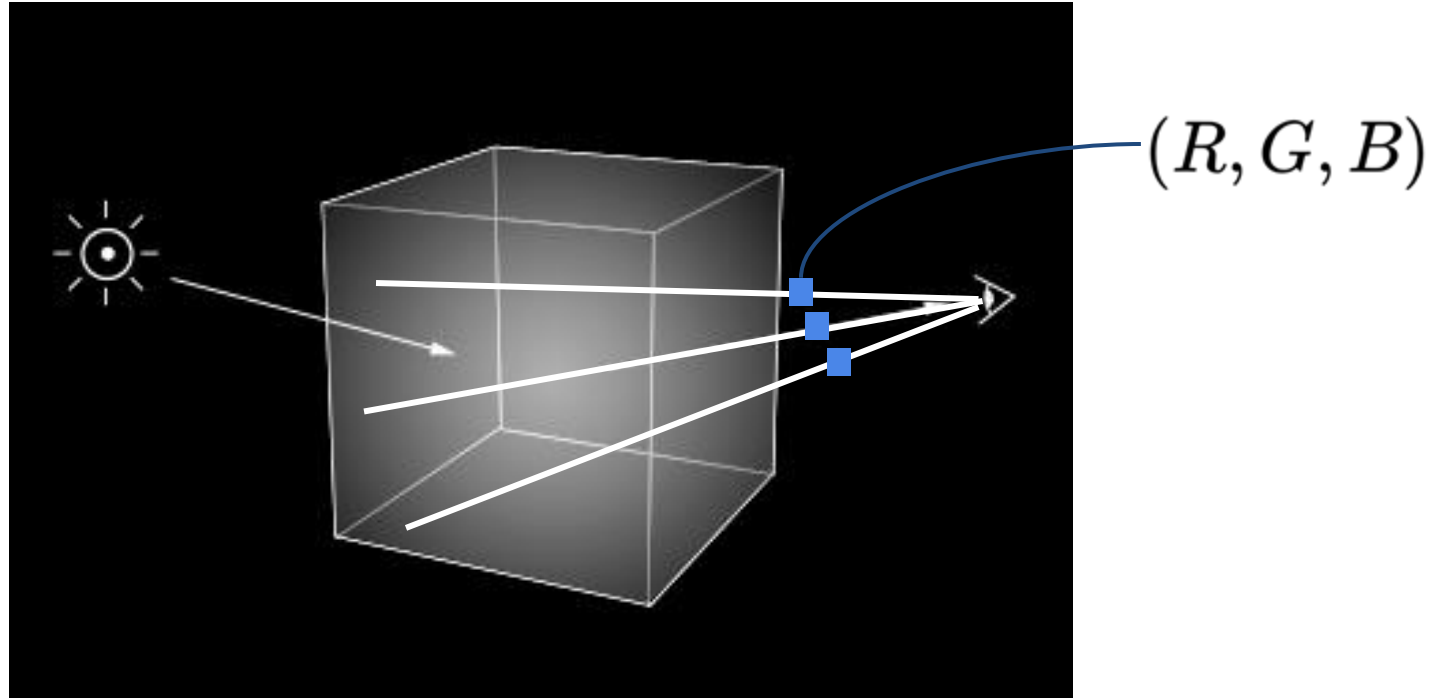


<https://coronarenderer.freshdesk.com/support/solutions/articles/12000045276-how-to-use-the-corona-volume-grid->

Volume Rendering: Scene Representation



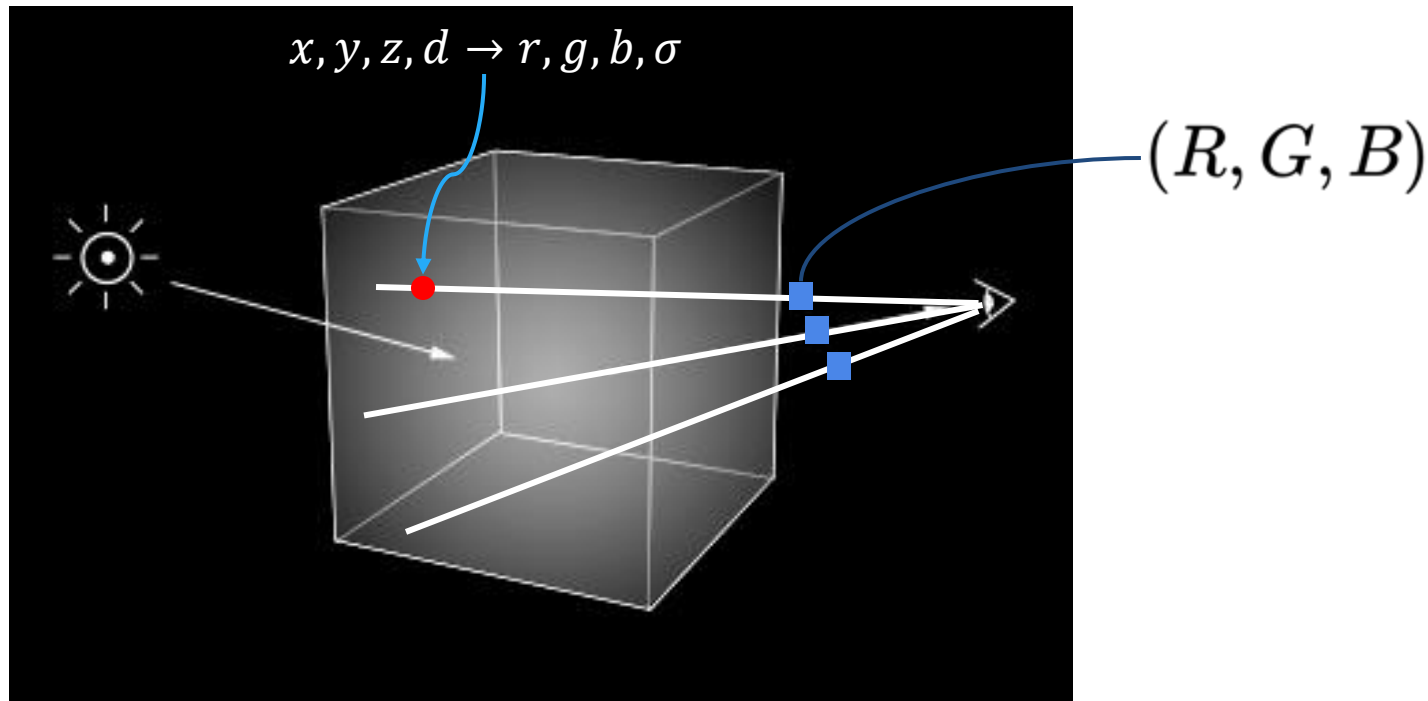
Volume Rendering: Scene Representation



Volume Rendering: Scene Representation

Each location (x, y, z) emits certain color r, g, b when viewed with direction d .

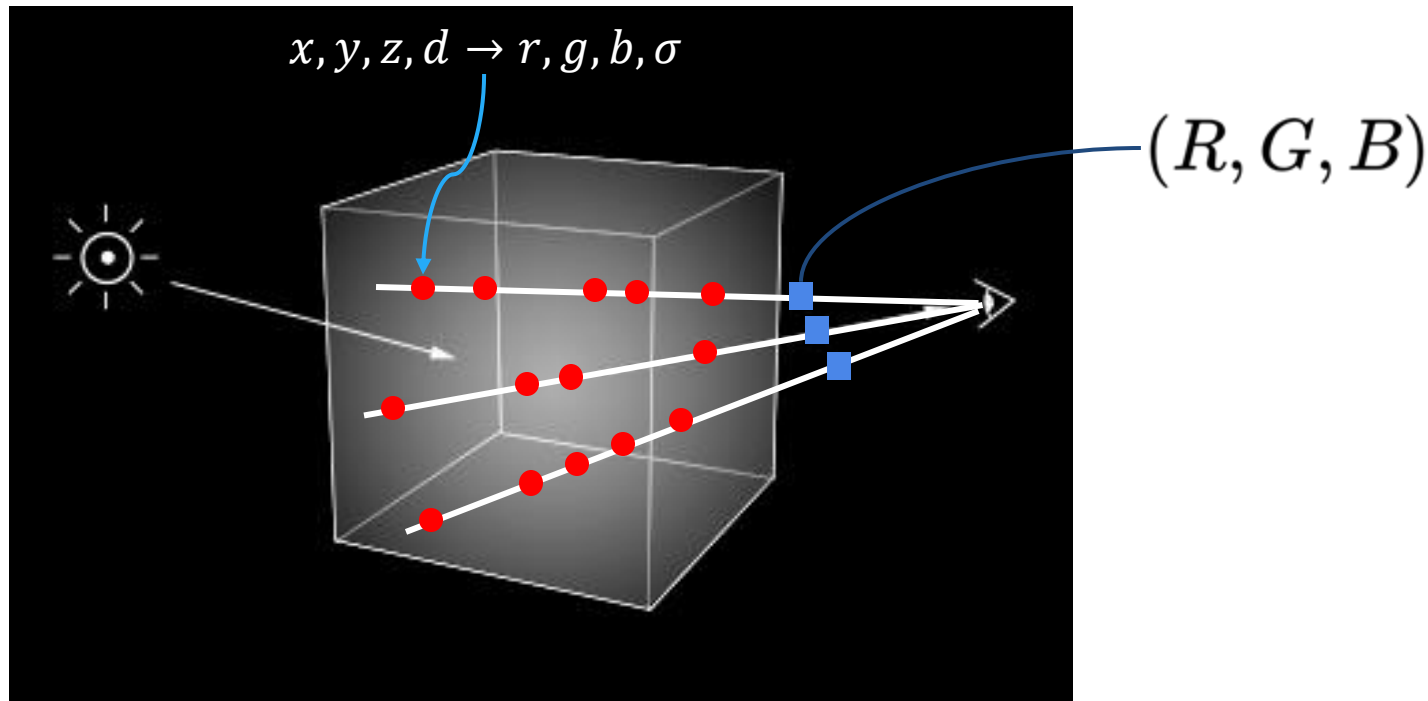
We represent point occupancy continuously as density d .



Volume Rendering: Scene Representation

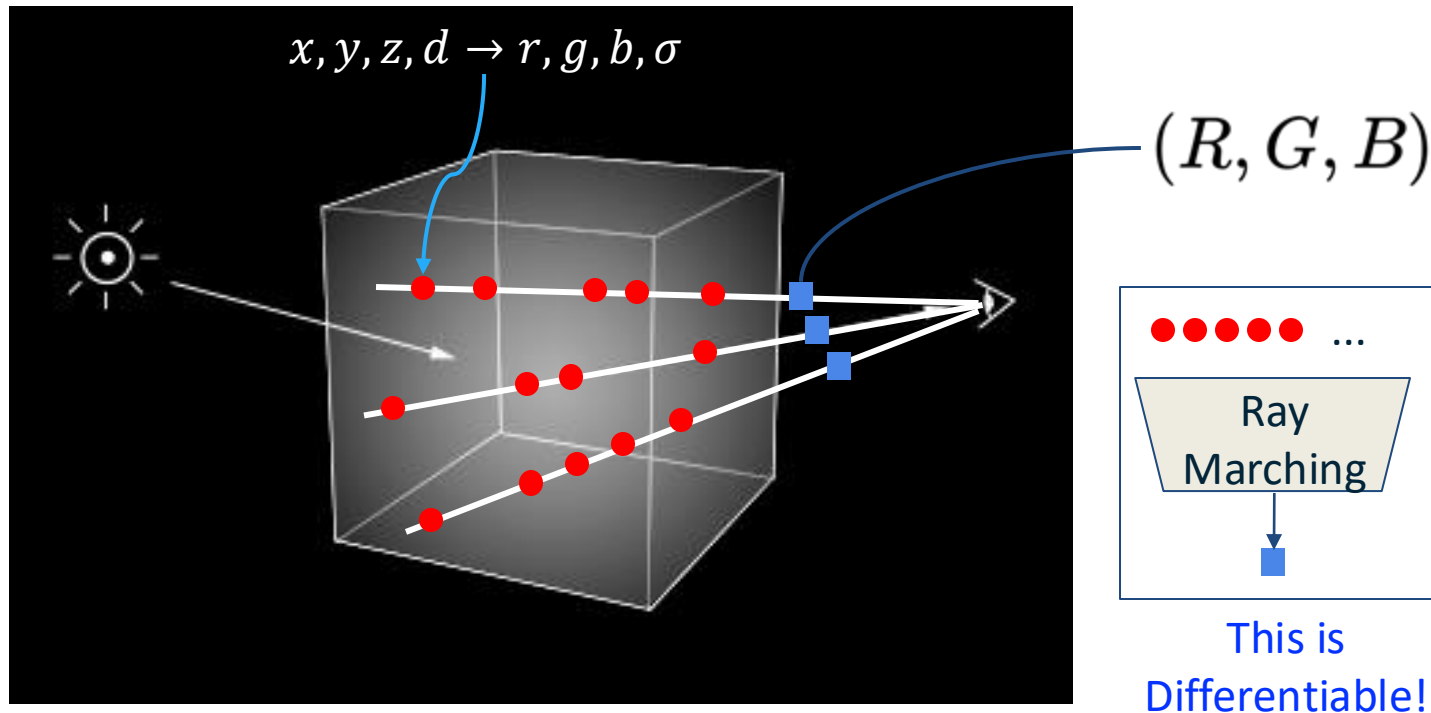
Each location (x, y, z) emits certain color r, g, b when viewed with direction d .

We represent point occupancy continuously as density d .



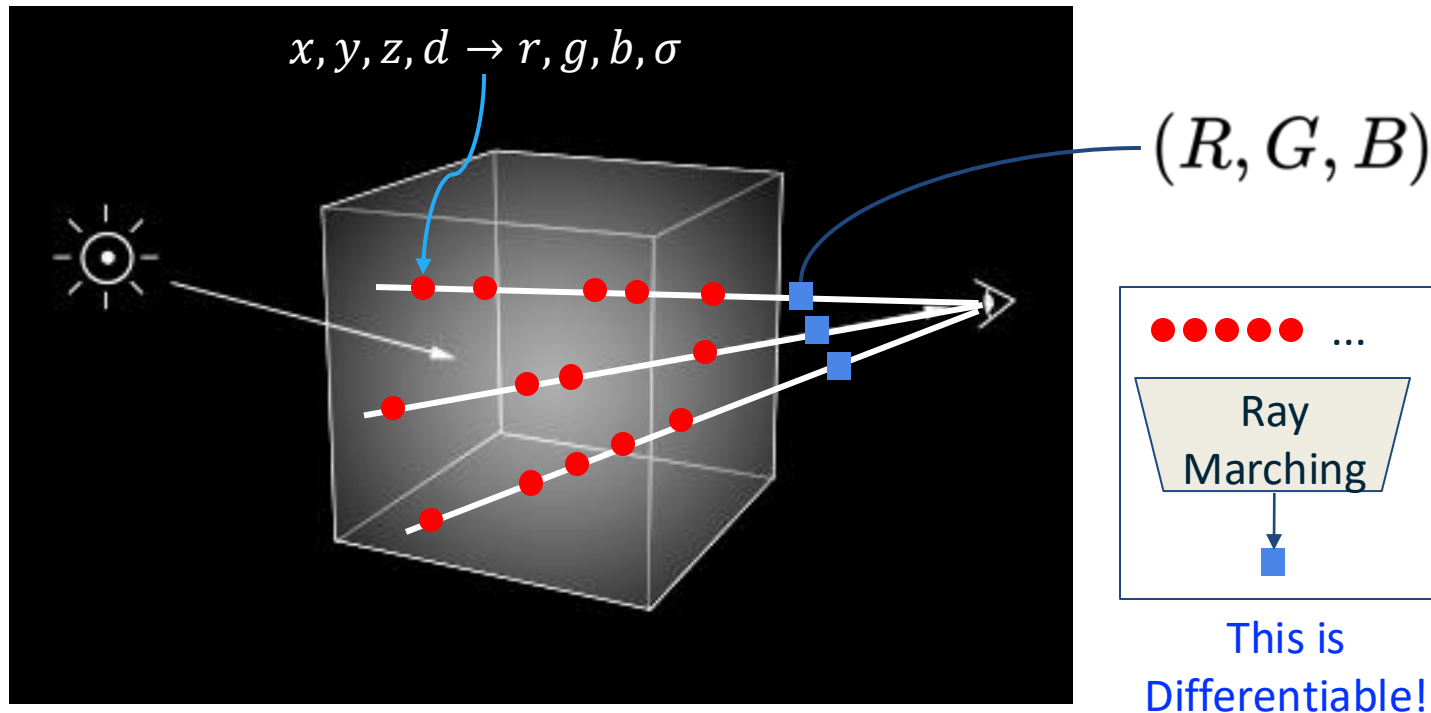
Volume Rendering: Ray Marching

Ray Marching: Integrate color and density of points along a ray (via discretization) to render an RGB value. Render many points -> An image!



Volume Rendering: Ray Marching

Idea: Train a neural network to represent the ray marching volume rendering function:
 $F_{\theta}(x, y, z, d) \rightarrow (r, g, b, \sigma)$. **Each NN encodes a 3D scene.**

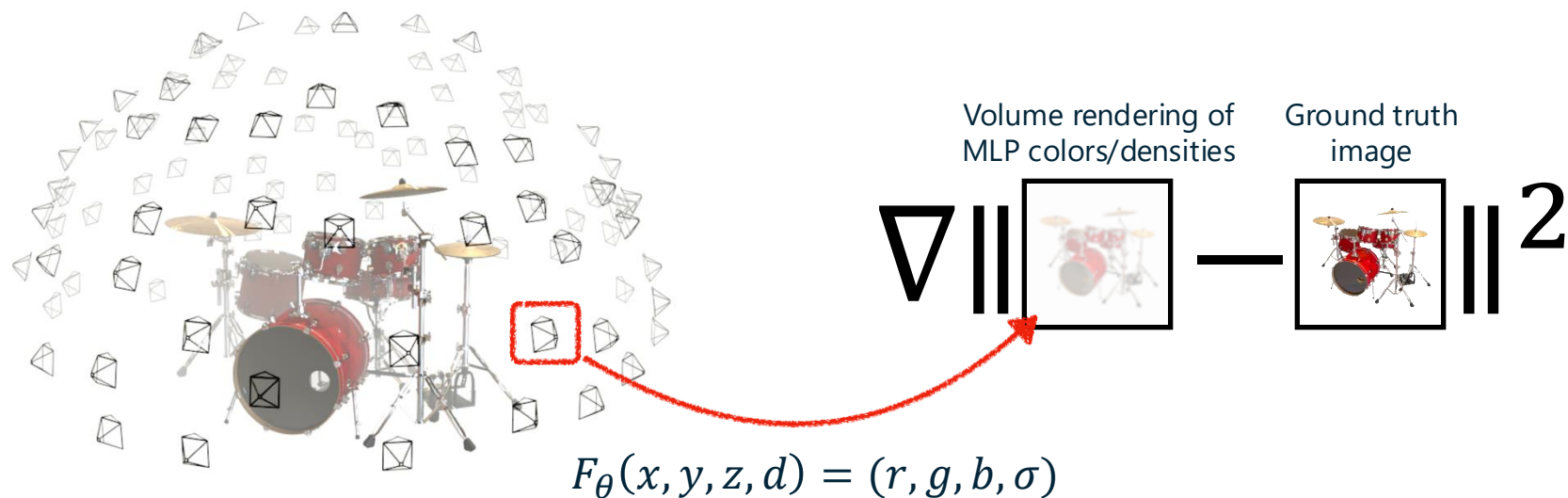


NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis

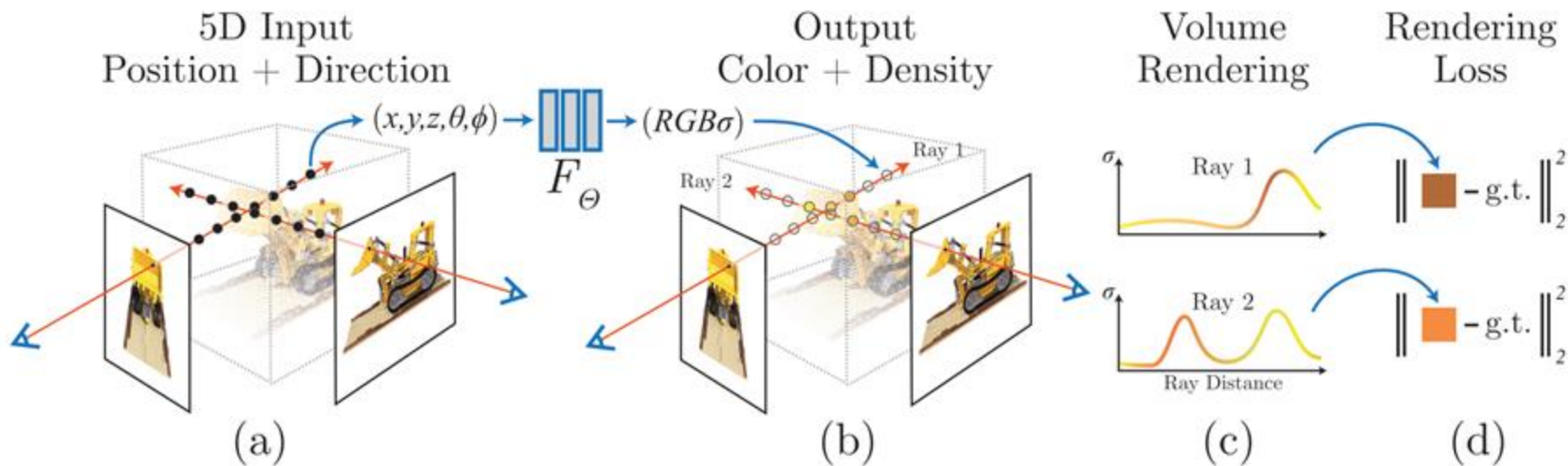
Ben Mildenhall^{1*} Pratul P. Srinivasan^{1*} Matthew Tancik^{1*}
Jonathan T. Barron² Ravi Ramamoorthi³ Ren Ng¹

¹UC Berkeley ²Google Research ³UC San Diego

Train a Single Neural Network to Reproduce the Ground Truth Images of a Scene



NeRF Overview



NeRF: Optimization

The volume density $\sigma(\mathbf{x})$ can be interpreted as the differential probability of a ray terminating at an infinitesimal particle at location $\mathbf{x}$. The expected color $C(\mathbf{r})$ of camera ray $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$ with near and far bounds t_n and t_f is:

$$C(\mathbf{r}) = \int_{t_n}^{t_f} T(t) \sigma(\mathbf{r}(t)) \mathbf{c}(\mathbf{r}(t), \mathbf{d}) dt, \text{ where } T(t) = \exp\left(-\int_{t_n}^t \sigma(\mathbf{r}(s)) ds\right). \quad (1)$$

Solution: Numerically estimate the integral (quadrature).

1. Discretize the ray into bins.
2. Sample point in each bin.
3. Compute numerical integration.

$$\hat{C}(\mathbf{r}) = \sum_{i=1}^N T_i (1 - \exp(-\sigma_i \delta_i)) c_i, \text{ where } T_i = \exp\left(-\sum_{j=1}^{i-1} \sigma_j \delta_j\right)$$

Key Insight 1: Positional Encoding

Challenge: Having F_θ operate directly on (x, y, z, d) performs poorly.

Solution: Positional encoding

$$\gamma(p) = (\sin(2^0 \pi p), \cos(2^0 \pi p), \dots, \sin(2^{L-1} \pi p), \cos(2^{L-1} \pi p))$$



Ground Truth



Complete Model



No View Dependence



No Positional Encoding

Key Insight 2: Hierarchical Volume Rendering

Challenge: Waste of compute on empty space.

Solution: coarse-to-fine prediction.

$$\hat{C}_c(\mathbf{r}) = \sum_{i=1}^{N_c} w_i c_i, \quad w_i = T_i(1 - \exp(-\sigma_i \delta_i)). \quad (5)$$

Normalizing these weights as $\hat{w}_i = w_i / \sum_{j=1}^{N_c} w_j$ produces a piecewise-constant PDF along the ray. We sample a second set of N_f locations from this distribution using inverse transform sampling, evaluate our “fine” network at the union of the first and second set of samples, and compute the final rendered color of the ray $\hat{C}_f(\mathbf{r})$ using Eqn. 3 but using all $N_c + N_f$ samples. This procedure allocates more



NeRF encodes convincing view-dependent effects using directional dependence



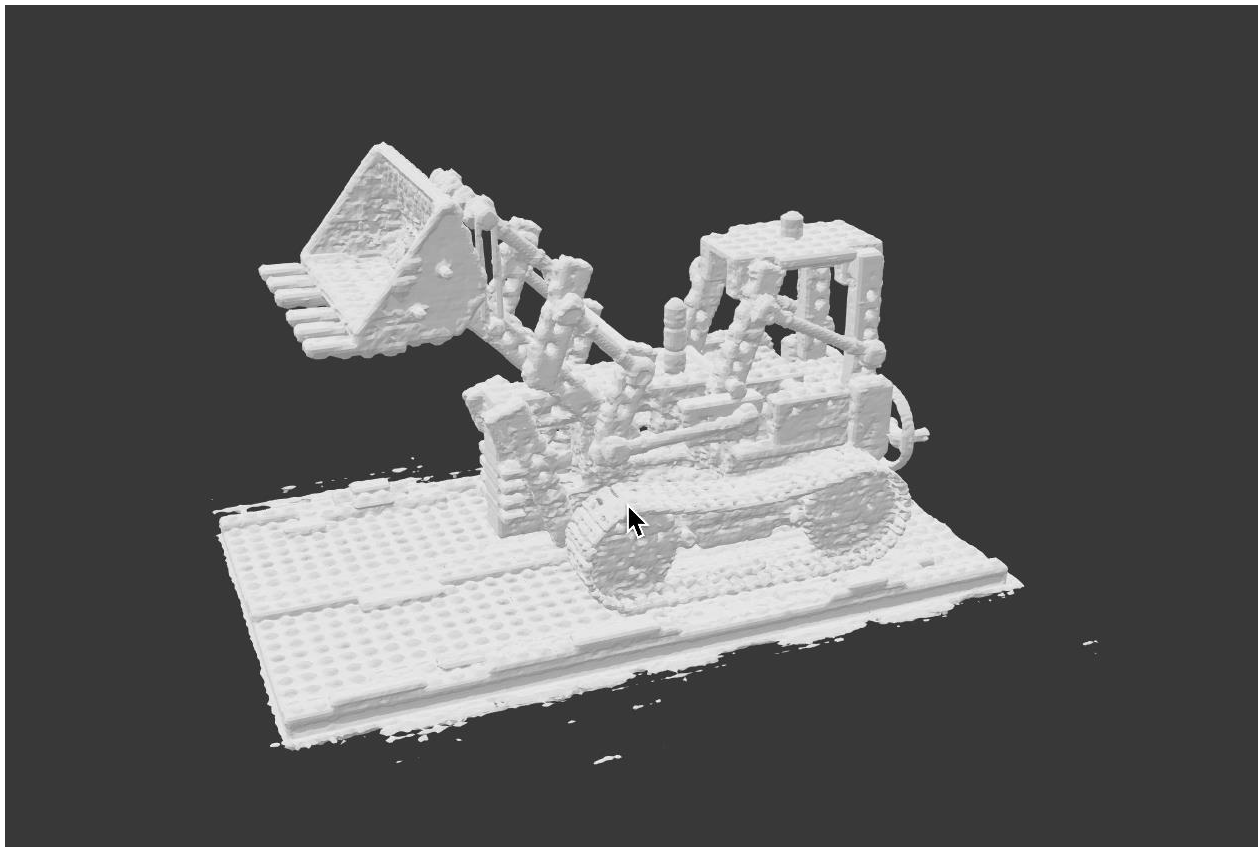
NeRF encodes convincing view-dependent effects using directional dependence



NeRF encodes detailed scene geometry with occlusion effects



NeRF encodes detailed scene geometry

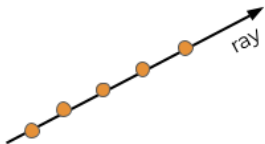


3D Gaussian Splatting (Kerbl and Kopanas et al., 2023)

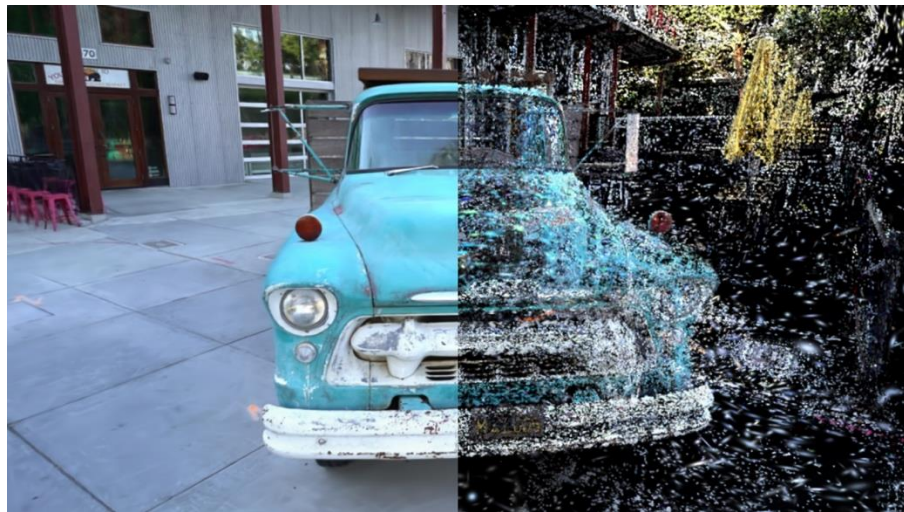
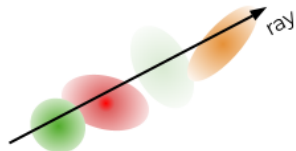
Key idea: 3D Gaussians as an **explicit representation** of a scene

- Train Gaussian blobs via inverse rendering (similar to NeRF)
- Store scene as Gaussian blobs instead of neural network weights (NeRF)
- Much faster during inference, but takes a lot of space to store

NeRF



Gaussian Splatting



Summary: 3D Representation and Neural Rendering

- Representation matters a lot for 3D computer vision tasks (detection, reconstruction, etc.)
- 3D Voxels are intuitive representation of space but struggles with high-resolution shape and large scenes
- Implicit function emerge as a new paradigm in representing scenes with Neural Networks
- Neural volume rendering: represent scenes implicit as point-direction to color-density neural networks. Photorealistic rendering, slow to train and evaluate
- More recent works on trading off space and time

Next Time: Vision Language Models