Topics:

- Machine learning intro, applications (CV, NLP, etc.)
- Parametric models and their components

CS 4644 / 7643-A

ZSOLT KIRA

- **What's up with the capacity/waitlist?**
- **PS0 due Sunday night!**
  - Please do it!
  - We have fixed some gradescope autograder issues (sorry!)
- **Piazza**: not all enrolled!
  - Enroll now! https://piazza.com/gatech/spring2023/cs46447643/home (Code: DLSPR23 or through canvas)
  - Note: Do NOT post anything containing solutions publicly!
  - Make it active!
- **Office hours** start next week

Administrivia

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- **Collaboration**
  - Only on HWs and project (not allowed in HW0/PS0).
  - You may discuss the questions
  - Each student writes their own answers
  - Write on your homework anyone with whom you collaborate
  - Do NOT search for code implementing what we ask; search for concepts
  - **Each student must write their own code/proofs**

- **Zero tolerance on plagiarism**
  - Neither ethical nor in your best interest
  - Always credit your sources
  - Don't cheat. We will find out.

Collaboration Policy

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- **Grace period**
  - 2 days grace period for each assignment (**EXCEPT PS0**)
    - Intended for checking submission NOT to replace due date
    - No need to ask for grace, no penalty for turning it in within grace period
    - Can NOT use for PS0

- **After grace period, you get a 0 (no excuses except medical)**
  - Send all medical requests to dean of students (https://studentlife.gatech.edu/)
  - Form: https://gatech-advocate.symplicity.com/care_report/index.php/pid224342

- **DO NOT SEND US ANY MEDICAL INFORMATION!** We do not need any details, just a confirmation from dean of students

Grace Period

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CS231n Convolutional Neural Networks for Visual Recognition

Python Numpy Tutorial

This tutorial was contributed by Justin Johnson.

We will use the Python programming language for all assignments in this course. Python is a great general-purpose programming language on its own, but with the help of a few popular libraries (numpy, scipy, matplotlib) it becomes a powerful environment for scientific computing.

We expect that many of you will have some experience with Python and numpy; for the rest of you, this section will serve as a quick crash course both on the Python programming language and on the use of Python for scientific computing.

http://cs231n.github.io/python-numpy-tutorial/

Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

Machine Learning Overview

What is Machine Learning (ML)?

"A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P, if its performance at tasks in T, as measured by P, improves with experience E."

Tom Mitchell (Machine Learning, 1997)

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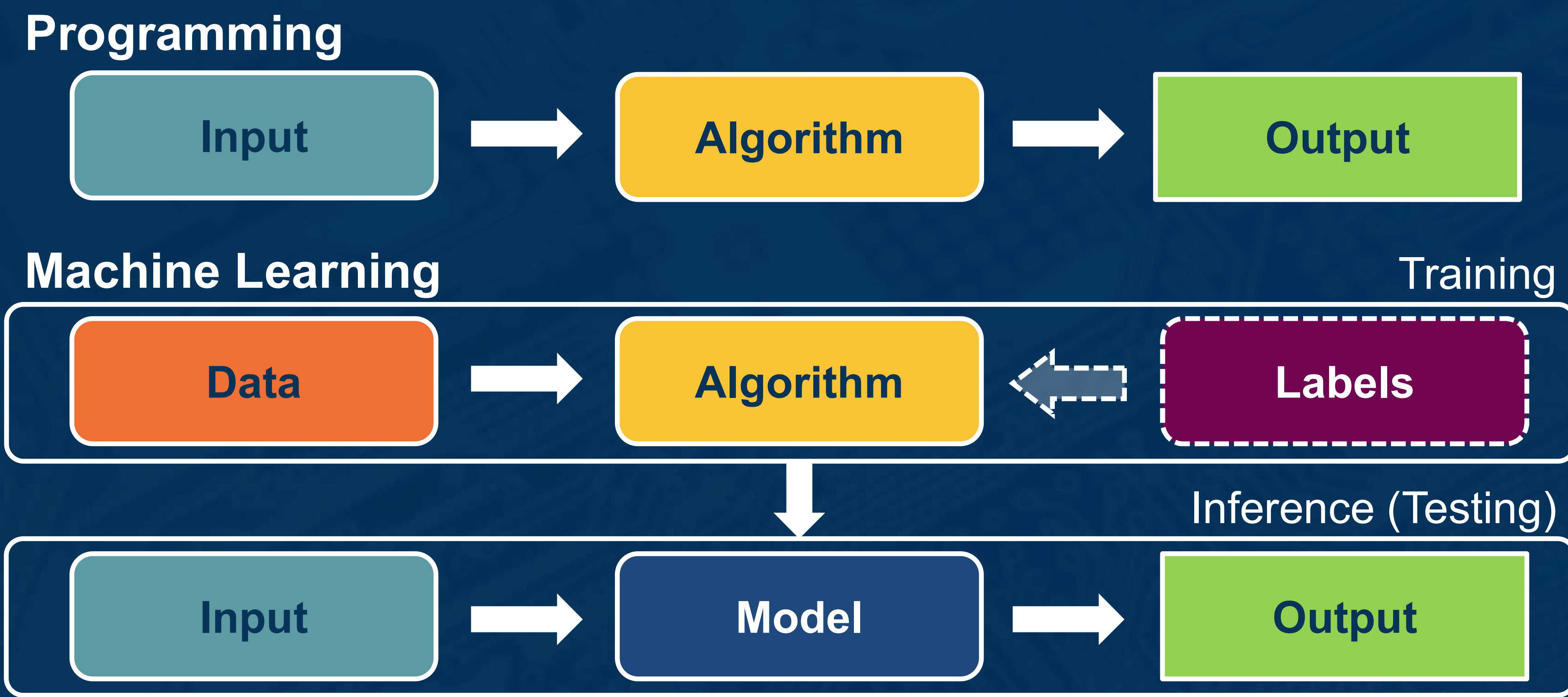
How is it Different than Programming?

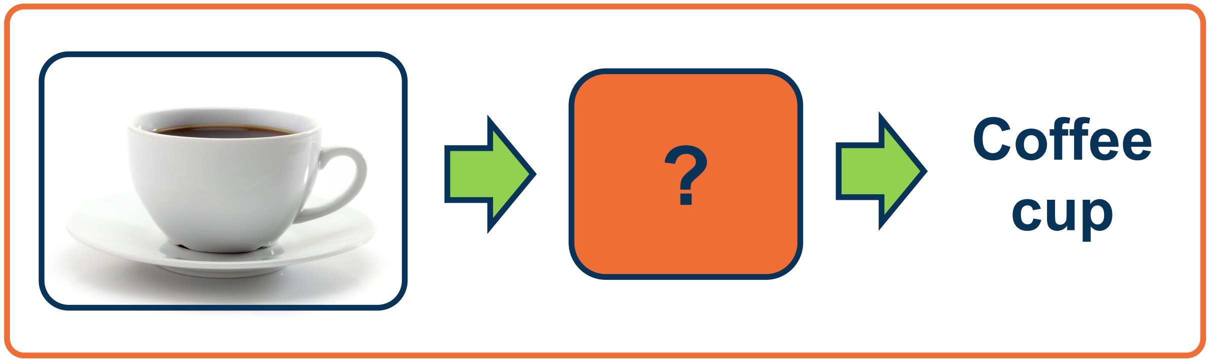


Machine learning thrives when it is **difficult to design an algorithm** to perform the task

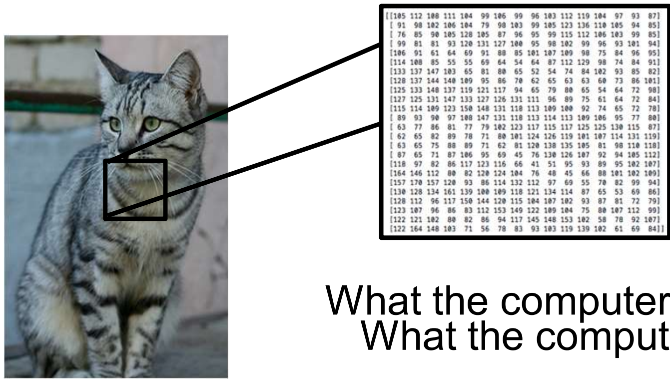
Applications:

```
algorithm quicksort(A, lo, hi) is
    if lo < hi then
        p := partition(A, lo, hi)
        quicksort(A, lo, p - 1)
        quicksort(A, p + 1, hi)

algorithm partition(A, lo, hi) is
    pivot := A[hi]
    i := lo
    for j := lo to hi do
        if A[j] < pivot then
            swap A[i] with A[j]
            i := i + 1
    swap A[i] with A[hi]
    return i
```



Why Image Classification is Hard

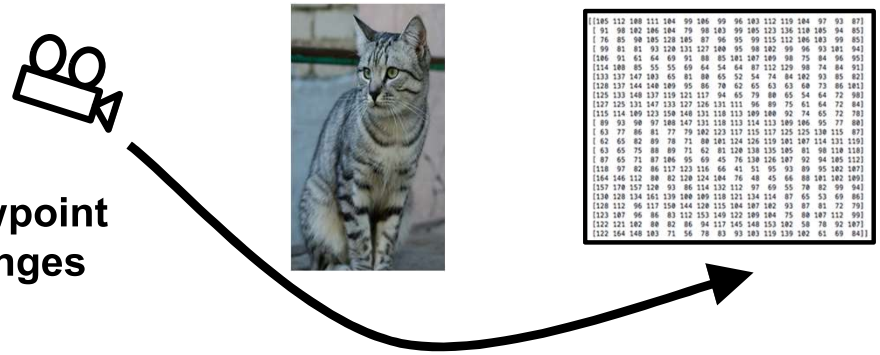


What the computer sees
What the computer sees

An image is just a big grid of numbers between [0, 255]:

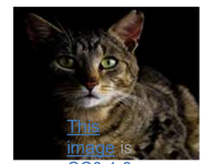
e.g. 800 x 600 x 3
(3 channels RGB)

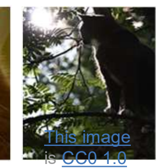
Viewpoint Changes



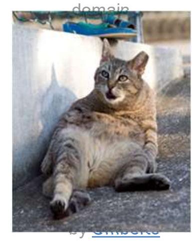
All pixels change when the camera moves!

Illumination





Deformation



Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

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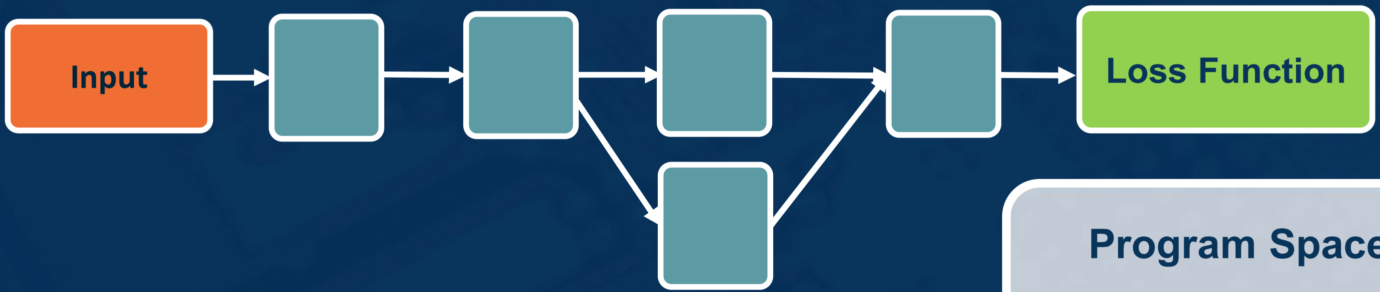
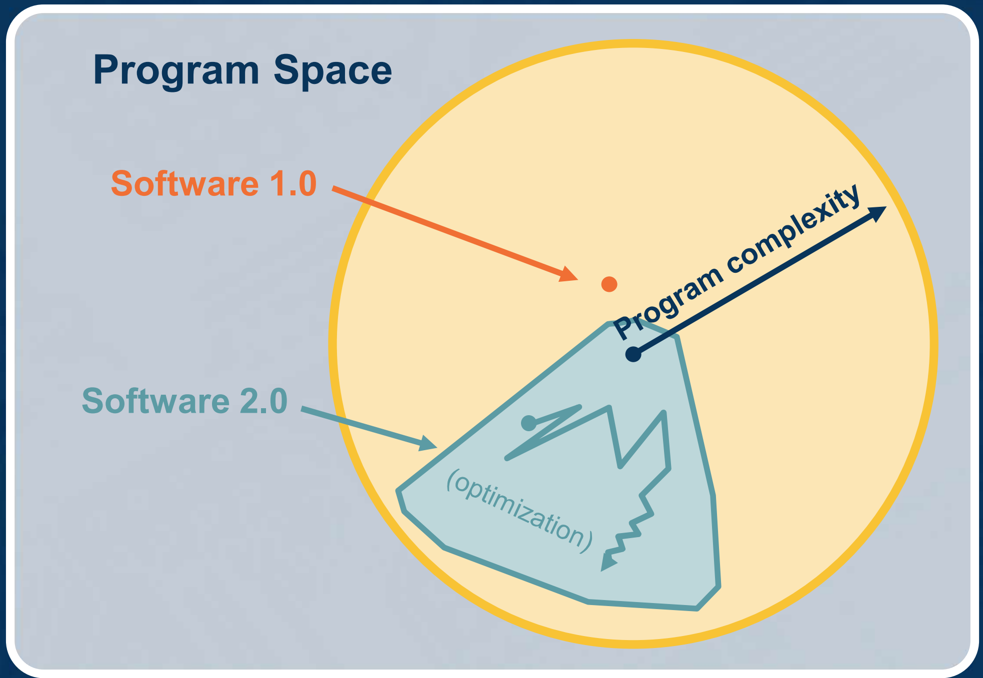
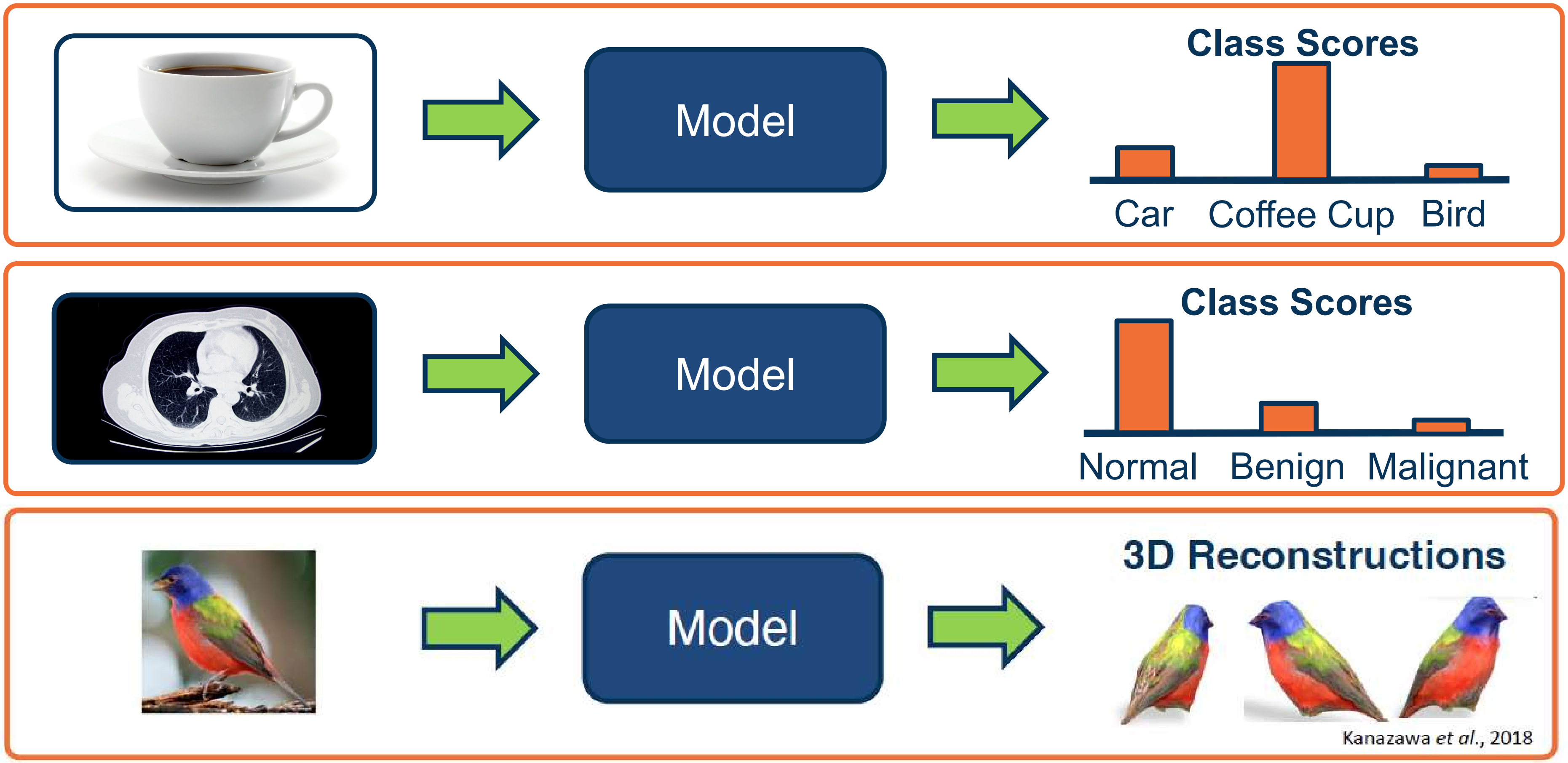
The Power of Deep Learning





Adapted from figure by Andrej Karpathy

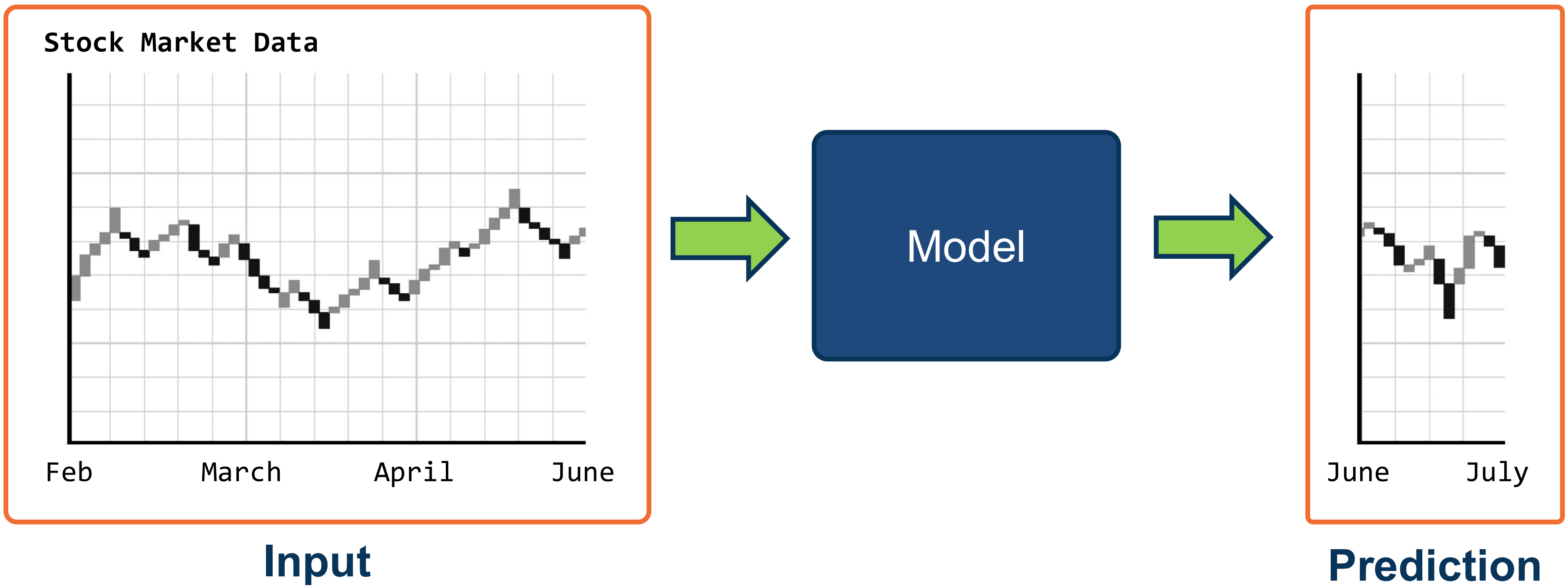
Application: Computer Vision



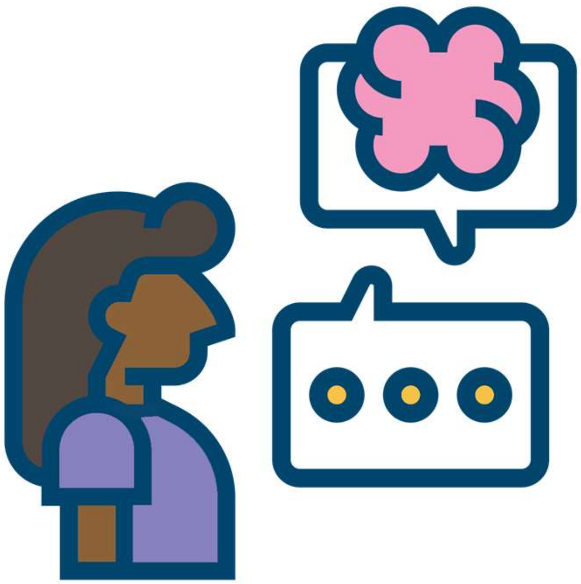
Example: Image Classification

Application: Time-Series Forecasting

Given a series of measurements, **output prediction for next time period**



Application: Natural Language Process (NLP)



Very large number of NLP sub-tasks:

- Syntax Parsing
- Translation
- Named entity recognition
- Summarization

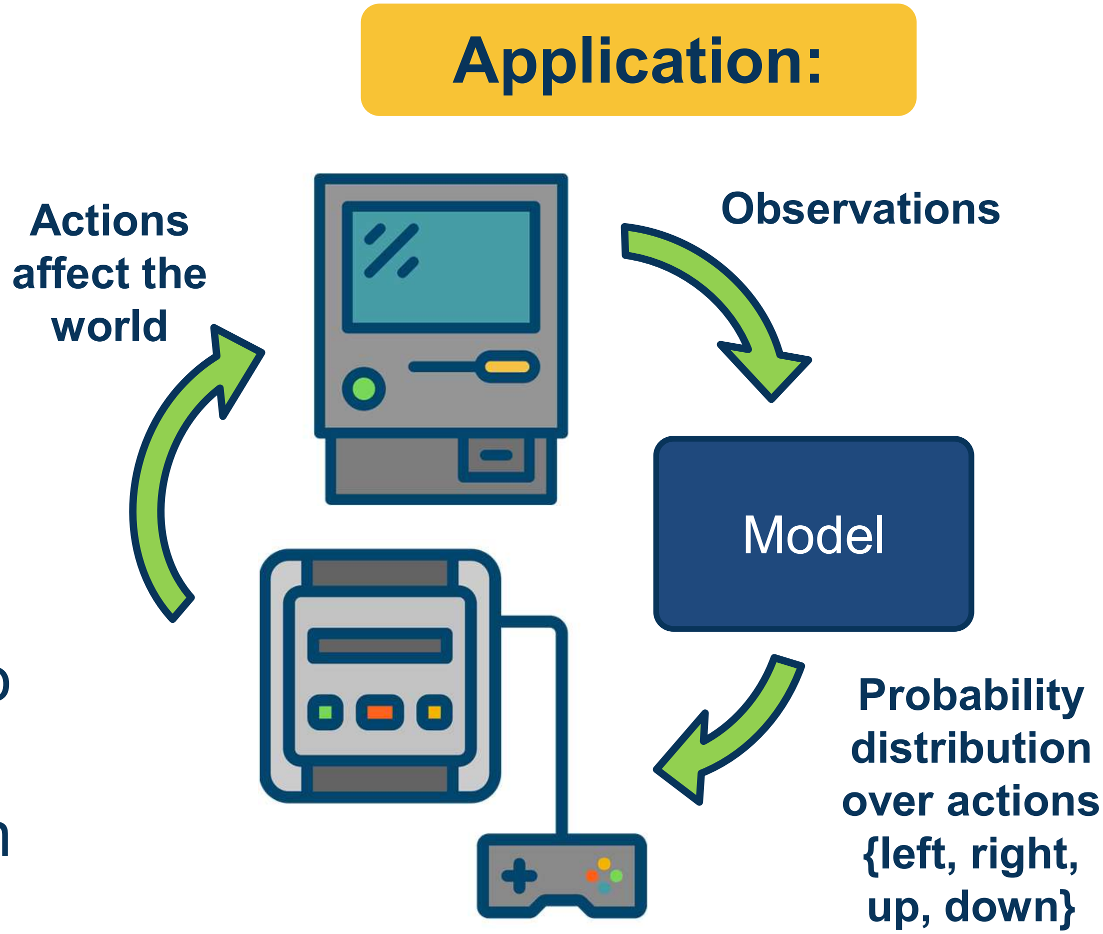
Sequence modeling: Variable length sequential inputs and/or outputs

Recent progress: Large-scale language models

Decision-making tasks

- Sequence of inputs/outputs
- Actions affect the environment

Examples: Chess / Go, Video Games, Recommendation Systems, Network Congestion Control, …



Robotics involves a **combination of AI/ML techniques**:

- **Sense:** Perception
- **Plan:** Planning
- **Act:** Controls/Decision-Making

Some things are **learned (perception)**, while others **programmed**

- Evolving landscape

Application:

Supervised Learning and Parametric Models

Supervised Learning

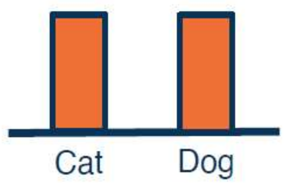
Unsupervised Learning

Reinforcement Learning

Supervised Learning

- Train Input: $\{X, Y\}$
- Learning output: $f : X \rightarrow Y$, e.g. a **distribution** $P(y|x)$

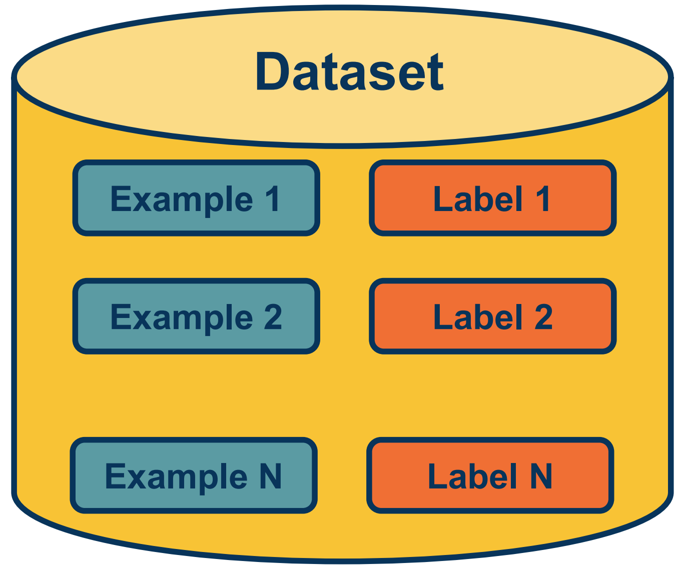
https://en.wikipedia.org/wiki/CatDog



Dataset

$X = \{x_1, x_2, \dots, x_N\}\ where\ x \in \mathbb{R}^d$ **Examples**

$Y = \{y_1, y_2, \dots, y_N\}\ where\ y \in \mathbb{R}^c$ **Labels**



Supervised Learning

- Train Input: $\{X, Y\}$
- Learning output: $f : X \rightarrow Y$, e.g. $P(y|x)$

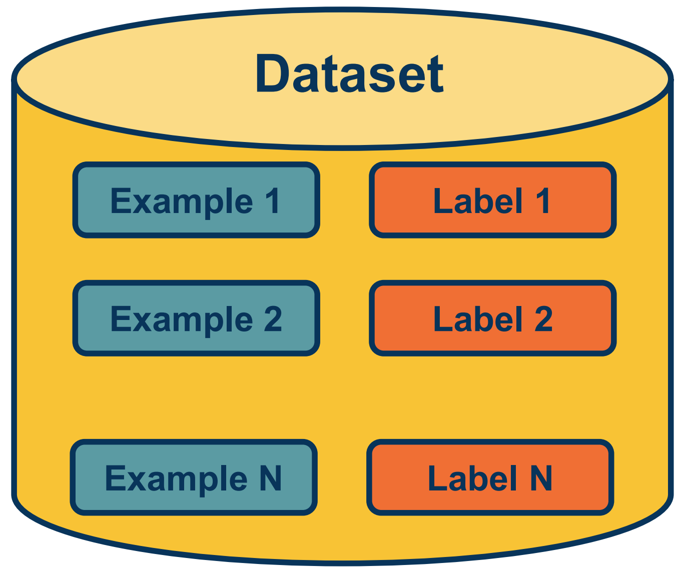
Terminology:

- Model / Hypothesis Class
  - $H: \{h: X \rightarrow Y\}$
  - Learning is search in hypothesis space
- Note **inputs $\boldsymbol{x_i}$ and $\boldsymbol{y_i}$** are each represented as **vectors**

Dataset

$X = \{x_1, x_2, \dots, x_N\}\ where\ x \in \mathbb{R}^d$ **Examples**

$Y = \{y_1, y_2, \dots, y_N\}\ where\ y \in \mathbb{R}^c$ **Labels**

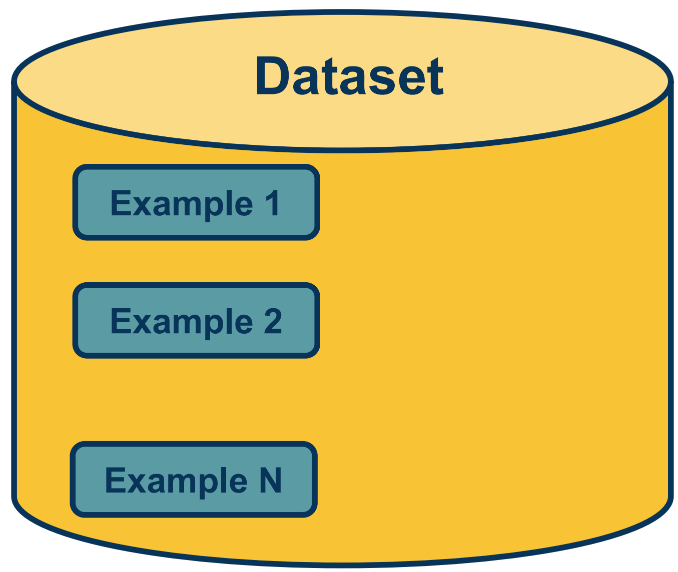


Dataset

$X = \{x_1, x_2, \ldots, x_N\}\ where\ x \in \mathbb{R}^d$ **Examples**

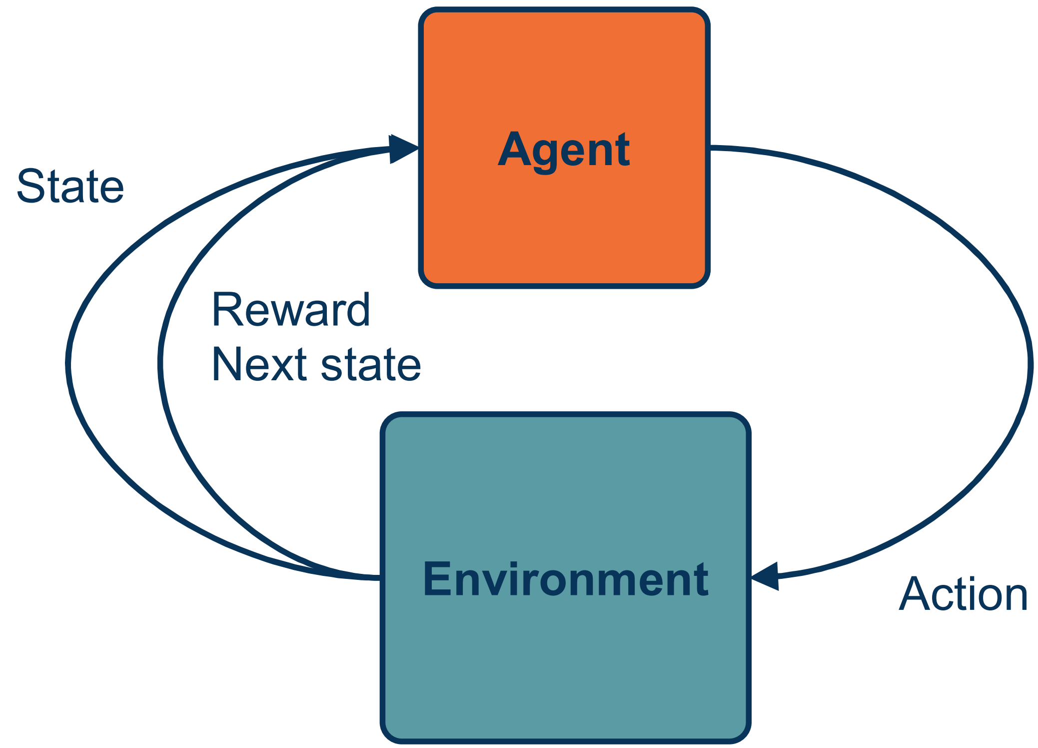
Unsupervised Learning

- Input: $\{X\}$
- Learning output: $P_{data}(x)$
- How likely is x under P_{data}?
- Can we sample from P_{data}?
- Example: Clustering, density estimation, generative modeling, etc.



Reinforcement Learning

- Supervision in form of **reward**
- No supervision on what action to take



Adapted from: http://cs231n.stanford.edu/slides/2020/lecture_17.pdf

Supervised Learning

- Train Input: $\{X, Y\}$
- Learning output: $f : X \rightarrow Y$, e.g. $P(y|x)$

Unsupervised Learning

- Input: $\{X\}$
- Learning output: $P(x)$
- Example: Clustering, density estimation, etc.

Reinforcement Learning

- Supervision in form of **reward**
- No supervision on what action to take

Very often combined, sometimes within the same model!

Types of Machine Learning

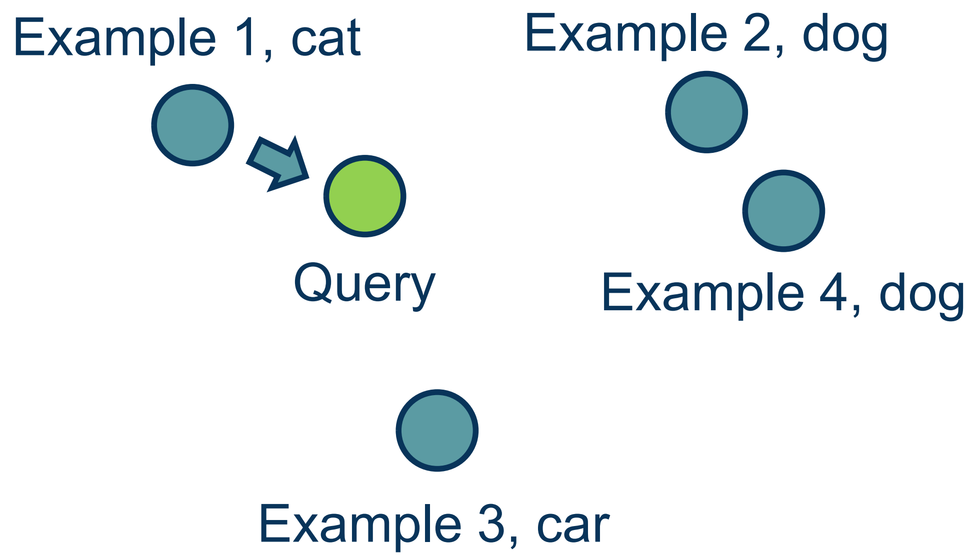
Non-Parametric Model

No explicit model for the function, **examples**:

- **Nearest neighbor classifier**
- Decision tree

Capacity (size of hypothesis class) grow with size of training data!

Non-Parametric – Nearest Neighbor

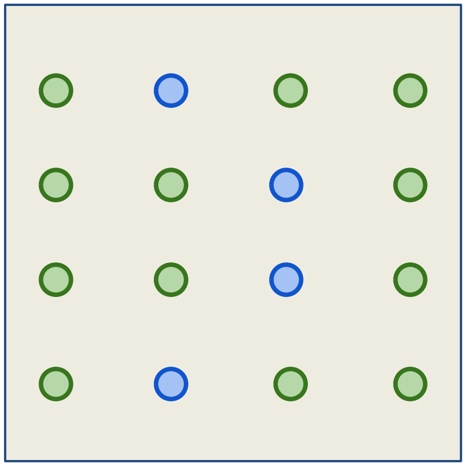


Procedure: Take label of nearest example k-Nearest Neighbor on images almost **never used.**

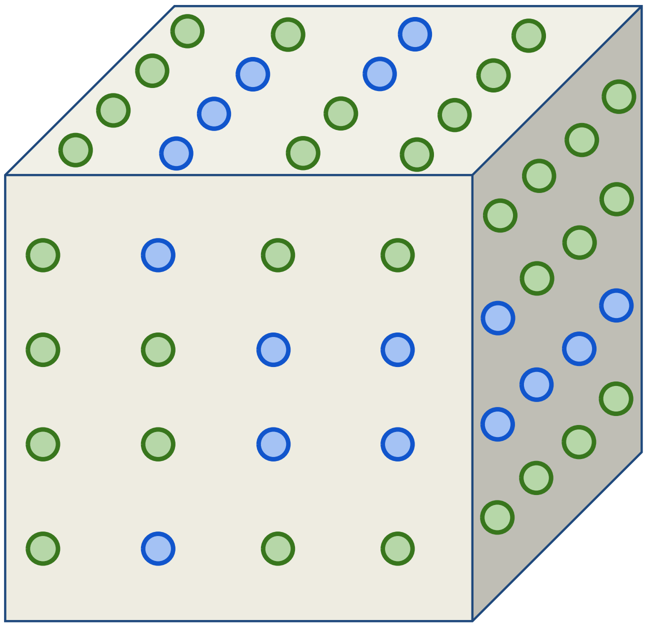
- Curse of dimensionality
  - Lots of weird behavior in high-dimensional spaces, e.g. orthogonality of random vectors, percentage of points around shell, etc.

Dimensions = 1
Points = 4

Dimensions = 2
Points = 4^2



Dimensions = 3
Points = 4^3



Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

- **Curse of Dimensionality**
  - Distances become meaningless in high dimensions
- **Doesn’t work well when large number of irrelevant features**
  - Distances overwhelmed by noisy features
- **Expensive**
  - No Learning: most real work done during testing
  - For every test sample, must search through all dataset – very slow!
  - Must use tricks like approximate nearest neighbor search

Problems with Instance-Based Learning

Parametric Model

Explicitly model the function $f : X \rightarrow Y$ in the form of a parametrized function $f(x, W) = y$, **examples**:

- Logistic regression/classification
- Neural networks

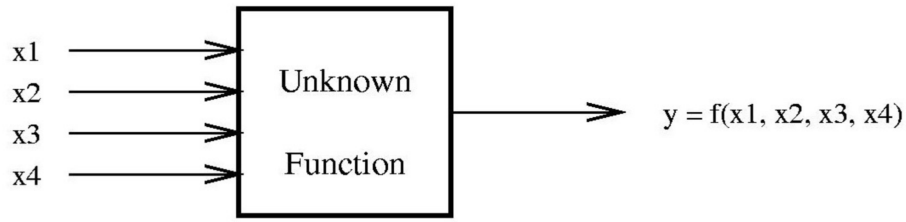
Capacity (size of hypothesis class) **does not** grow with size of training data!

Learning is **search**

Parametric – Linear Classifier

$$f(x, W) = Wx + b$$

A Learning Problem



Example	x_1	x_2	x_3	x_4	y
1	0	0	1	0	0
2	0	1	0	0	0
3	0	0	1	1	1
4	1	0	0	1	1
5	0	1	1	0	0
6	1	1	0	0	0
7	0	1	0	1	0

No Assumptions means no learning

Training Stage:

Training Data { (x_i,y_i) } → h (Learning)

Testing Stage

Test Data x → h(x) (Apply function, Evaluate error)

Procedural View of ML

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Probabilities to rescue:

X and Y are *random variables*

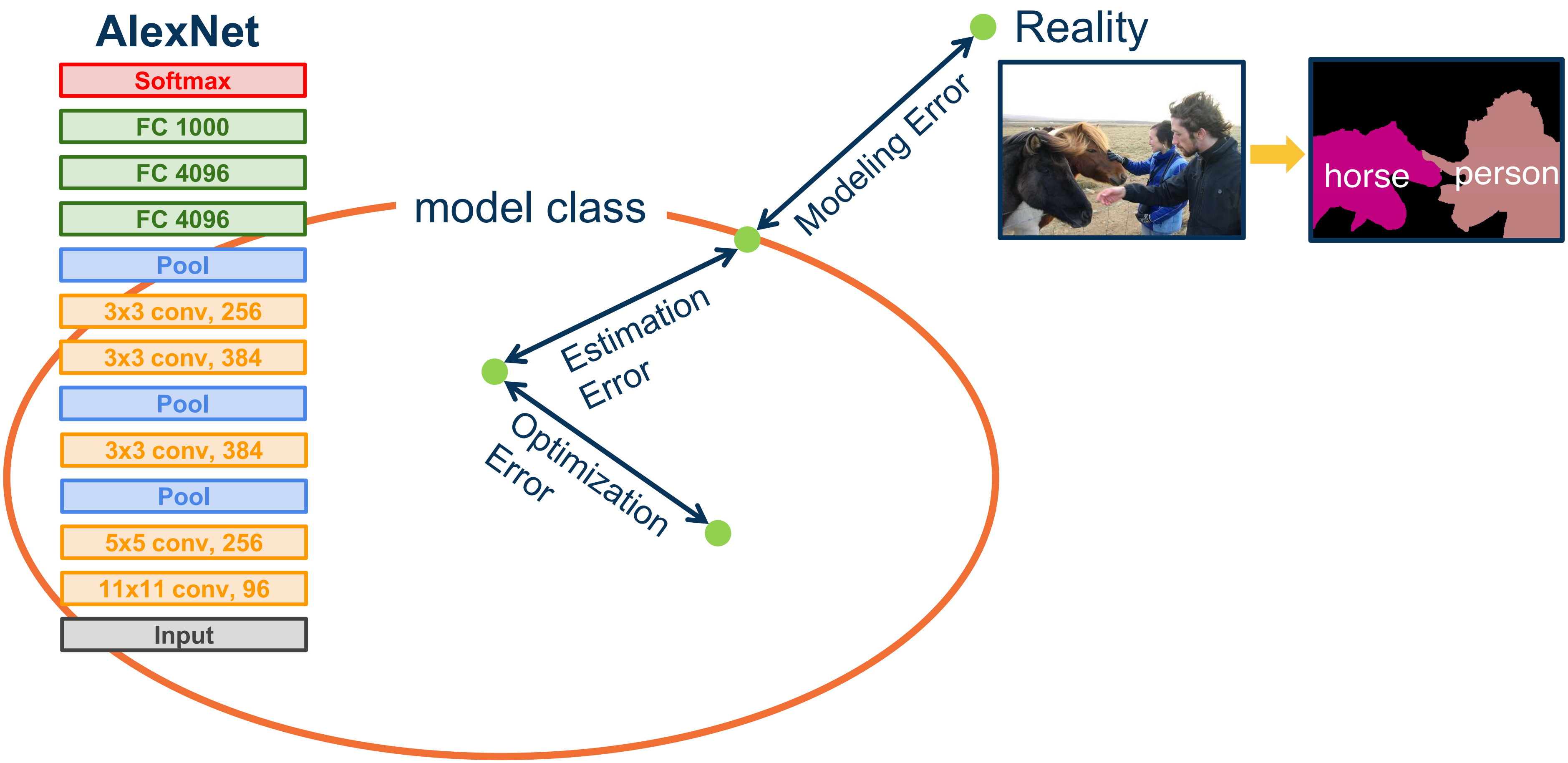
$D = (x_1,y_1), (x_2,y_2), \ldots, (x_N,y_N) \quad \sim P(X,Y)$

IID: Independent Identically Distributed

Both training & testing data sampled IID from P(X,Y)

Learn on training set

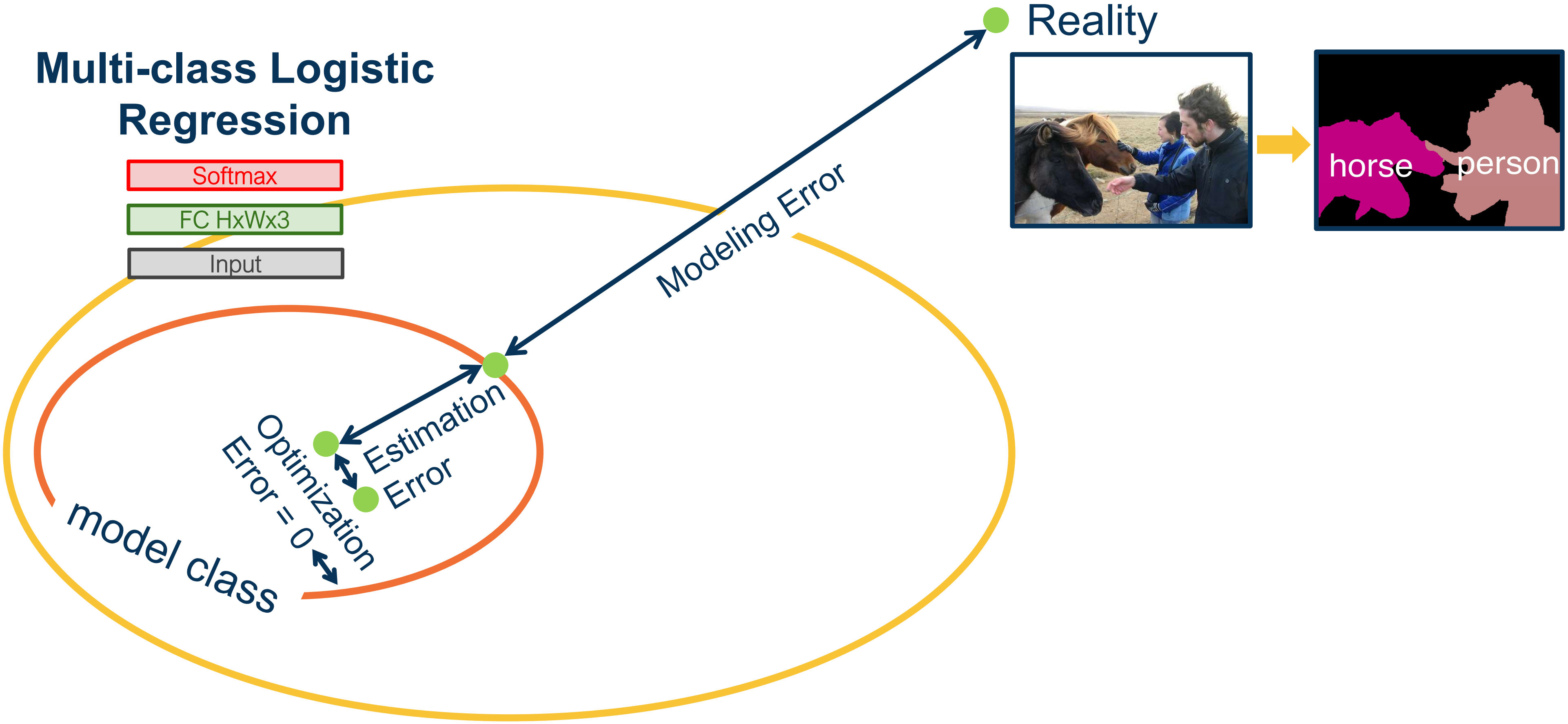
Have some hope of *generalizing* to test set



From: slides by Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

Generalization

Multi-class Logistic Regression



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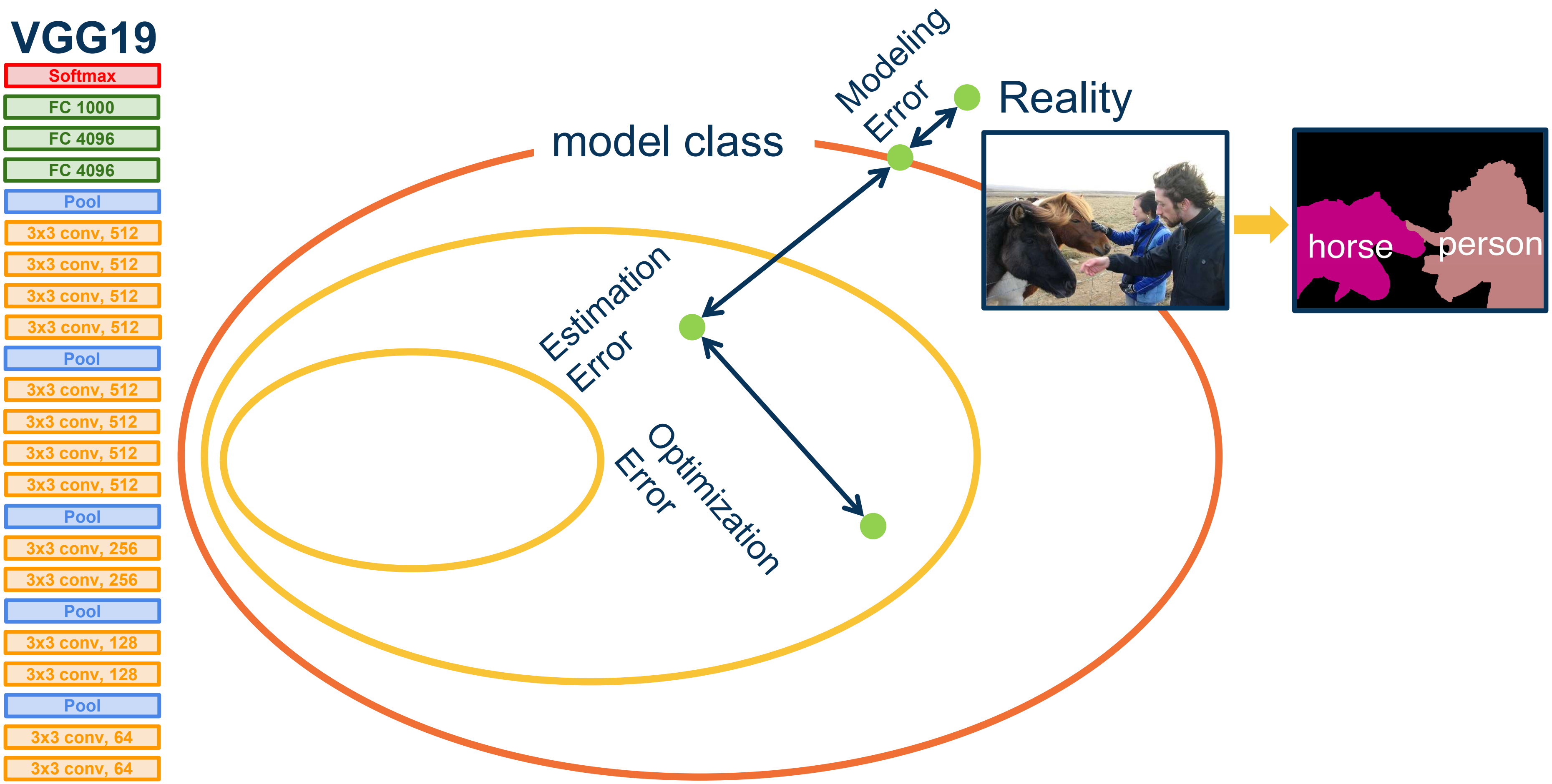
Generalization



From: slides by Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

Generalization

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20 years of research in Learning Theory oversimplified:

If you have:

Enough training data D

and H is not too complex

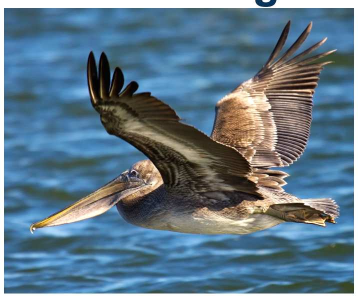
then *probably* we can generalize to unseen test data

Caveats: A number of recent empirical results question our intuitions built from this clean separation.

Zhang et al., Understanding deep learning requires rethinking generalization

Guarantees

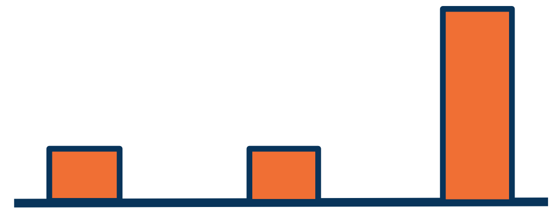
Data: Image



Model

$f(x, W) = Wx + b$

Class Scores



Input $\{X, Y\}$ where:

- X is an image
- Y is a **ground truth label** annotated by an expert (human)
- $f(x, W) = Wx + b$ is our model, chosen to be a linear function in this case
- W and b are the parameters (**weights**) of our model that must be learned

Example: Image Classification

Input image is **high-dimensional**

- For example n=512 so 512x512 image = **262,144** pixels
- Learning a classifier with high-dimensional inputs is hard

Before deep learning, it was typical to perform **feature engineering**

- Hand-design algorithms for converting raw input into a lower-dimensional set of features

Input Image

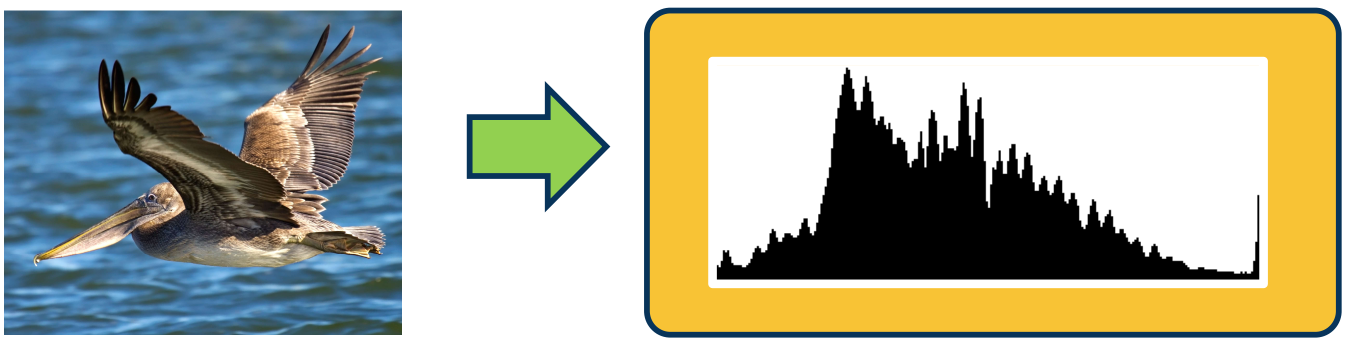
$$x = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1n} \\ x_{21} & x_{22} & \cdots & x_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nn} \end{bmatrix}$$

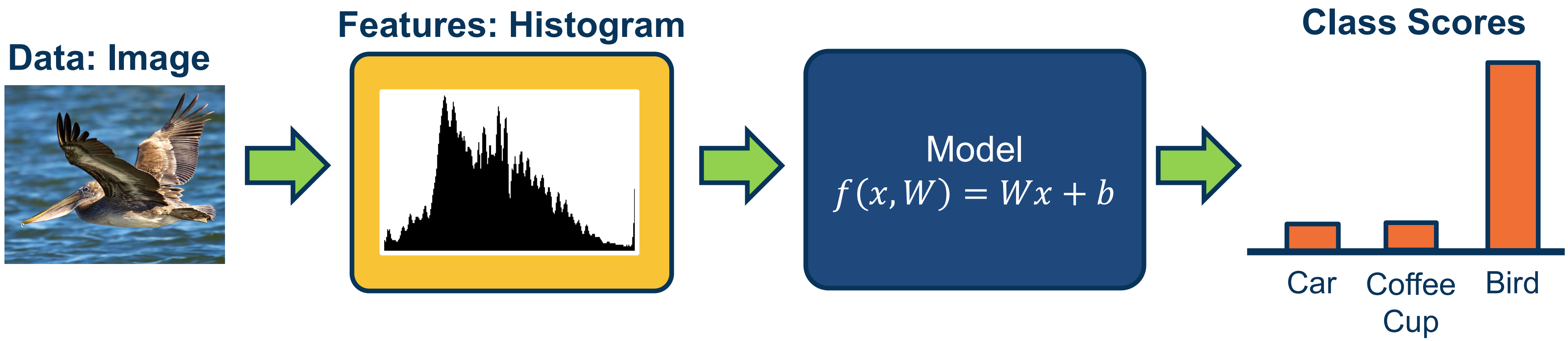
Input Representation: Feature Engineering

Example: Color histogram

- Vector of numbers representing number of pixels fitting within each bin
- We will later see that learning the feature representation itself is much more effective

Data: Image **Features: Histogram**





Input $\{X, Y\}$ where:

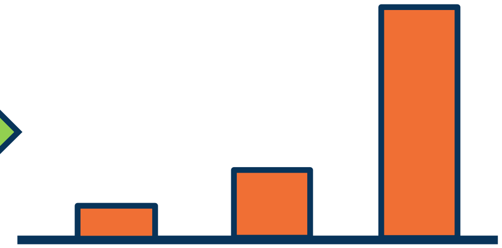
- X is an **image histogram**
- Y is a **ground truth label represented a probability distribution**
- $f(x, W) = Wx + b$ is our model, chosen to be a linear function in this case
- W and b are the **weights** of our model that must be learned

Example: Image Classification

Data: Text

Model
$f(x, W) = W_x + b$

Class Scores



Input $\{X, Y\}$ where:

- X is a sentence
- Y is a **ground truth label** annotated by an expert (human)
- $f(x, W) = Wx + b$ is our model, chosen to be a linear function in this case
- W and b are the **weights** of our model that must be learned

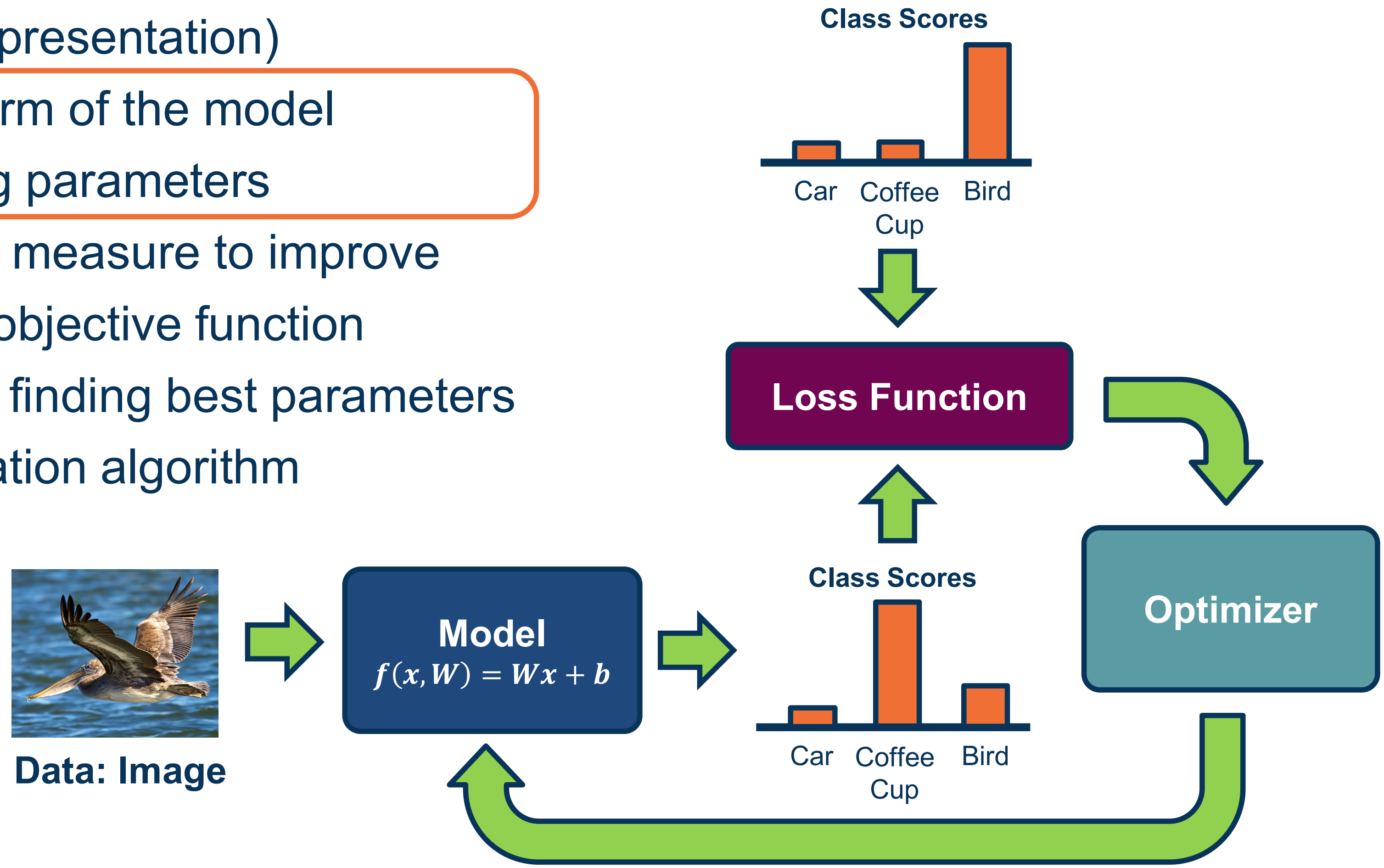
Word Histogram

Word	Count
this	1
that	0
is	2
...	
extremely	1
hello	0
onomatopoeia	0
...	

Example: Image Classification

Components of a Parametric Learning Algorithm

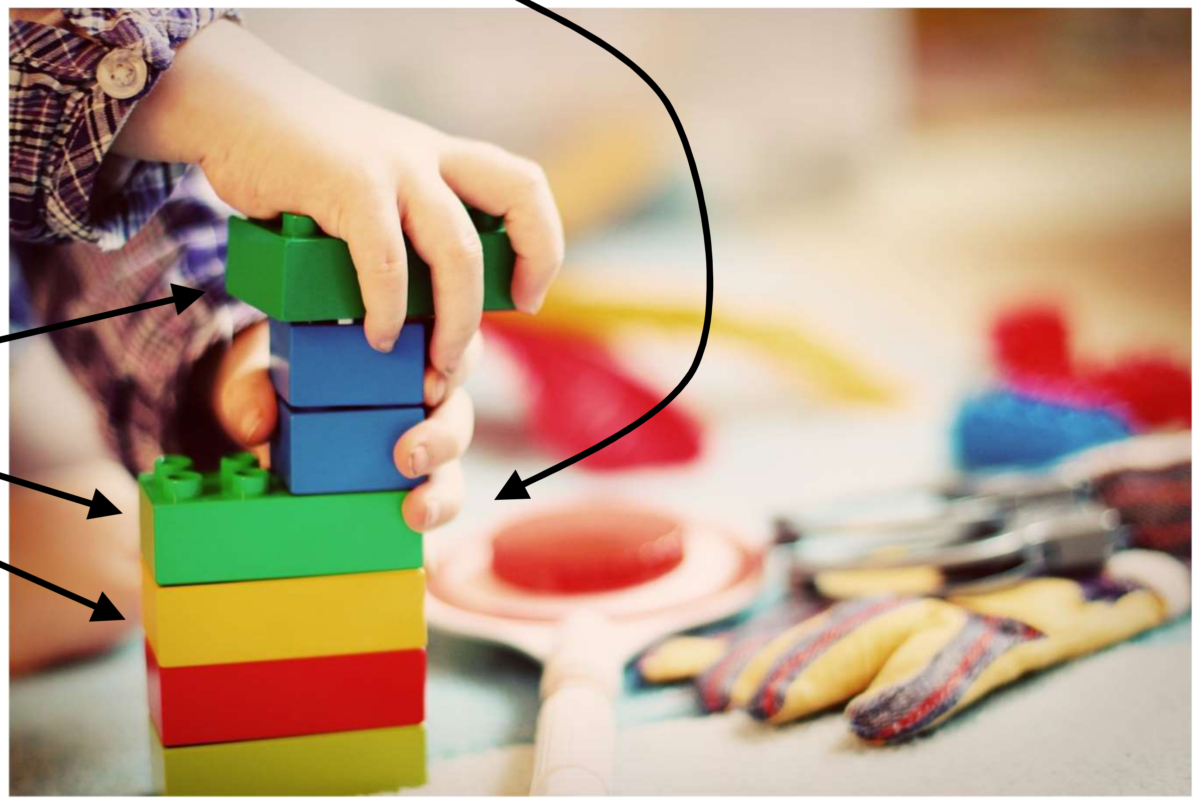
- Input (and representation)
- Functional form of the model
  - Including parameters
- Performance measure to improve
  - Loss or objective function
- Algorithm for finding best parameters
  - Optimization algorithm



Components of a Parametric Model

Neural Network

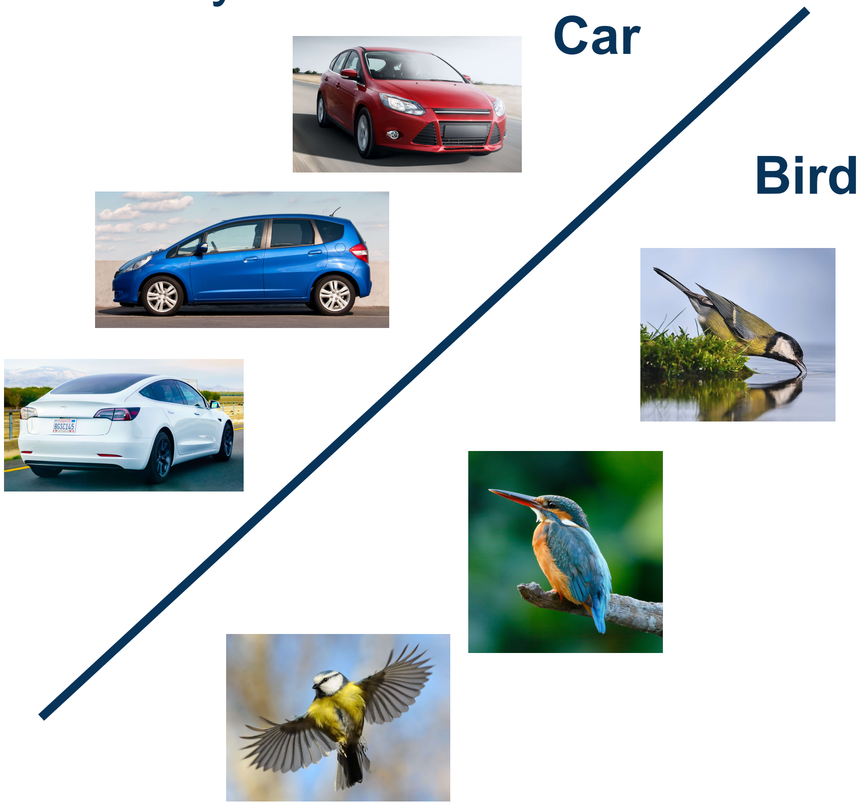
Linear
classifiers



Slide Credit: Fei-Fei Li, Justin Johnson, Serena Yeung, CS 231n

Deep Learning as Legos

What is the **simplest function** you can think of?



Our model is:

$$f(x, w) = w \cdot x + b$$

Classifier Result — $f(x, w)$

Weights — w

Input — x

Bias (scalar) — b

(Note if $\boldsymbol{w}$ and $\mathbf{x}$ are column vectors we often show this as $\boldsymbol{w}^T\boldsymbol{x}$)

Simple Function

Linear Classification and Regression

Simple linear classifier:

- Calculate score:
  $$\boldsymbol{f(x, w) = w \cdot x + b}$$
- Binary classification rule ($\boldsymbol{w}$ is a vector):
  $$\boldsymbol{y} = \begin{cases} \mathbf{1} & \textbf{if } \boldsymbol{f(x, w) >= 0} \\ \mathbf{0} & \textbf{otherwise} \end{cases}$$
- For multi-class classifier take class with highest (max) score
  $$\boldsymbol{f(x, W) = Wx + b}$$

Input Dimensionality

Data: Image

Model

$$f(x, W) = Wx + b$$

Class Scores

$$x = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1n} \\ x_{21} & x_{22} & \cdots & x_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nn} \end{bmatrix}$$

Flatten

$$x = \begin{bmatrix} x_{11} \\ x_{12} \\ \vdots \\ x_{21} \\ x_{22} \\ \vdots \\ x_{n1} \\ \vdots \\ x_{nn} \end{bmatrix}$$

To simplify notation we will refer to inputs as $x_1 \cdots x_m$ where $m = n \times n$

Model
$$f(x, W) = Wx + b$$

Classifier for class 1
Classifier for class 2
Classifier for class 3

$$\begin{bmatrix} w_{11} & w_{12} & \cdots & w_{1m} \\ w_{21} & w_{22} & \cdots & w_{2m} \\ w_{31} & w_{32} & \cdots & w_{3m} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_m \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

$\boldsymbol{W}$ $\boldsymbol{x}$ $\boldsymbol{b}$

(Note that in practice, implementations can use xW instead, assuming a different shape for W. That is just a different convention and is equivalent.)

Weights

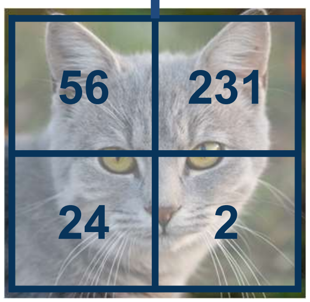
- We can move the bias term into the weight matrix, and a “1” at the end of the input
- Results in **one matrix-vector multiplication**!

Model
$$f(x, W) = Wx + b$$

$$\underbrace{\begin{bmatrix} w_{11} & w_{12} & \cdots & w_{1m} & b_1 \\ w_{21} & w_{22} & \cdots & w_{2m} & b_2 \\ w_{31} & w_{32} & \cdots & w_{3m} & b_3 \end{bmatrix}}_{\boldsymbol{W}} \underbrace{\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_m \\ 1 \end{bmatrix}}_{\boldsymbol{x}}$$

Example with an image with **4 pixels**, and **3 classes** (cat/dog/ship)

Stretch pixels into column



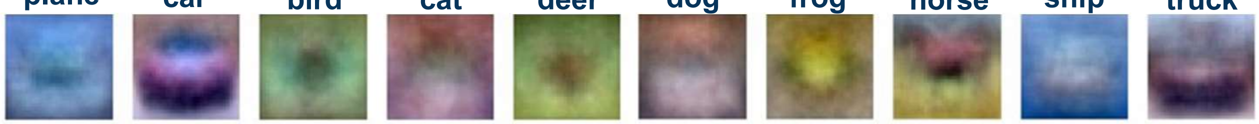
Input image

$$\underbrace{\begin{bmatrix} 0.2 & -0.5 & 0.1 & 2.0 \\ 1.5 & 1.3 & 2.1 & 0.0 \\ 0 & 0.25 & 0.2 & -0.3 \end{bmatrix}}_{W} \begin{bmatrix} 56 \\ 231 \\ 24 \\ 2 \end{bmatrix} + \underbrace{\begin{bmatrix} 1.1 \\ 3.2 \\ -1.2 \end{bmatrix}}_{b} = \begin{bmatrix} -96.8 \\ 437.9 \\ 61.95 \end{bmatrix} \begin{array}{l} \text{Cat score} \\ \text{Dog score} \\ \text{Ship score} \end{array}$$

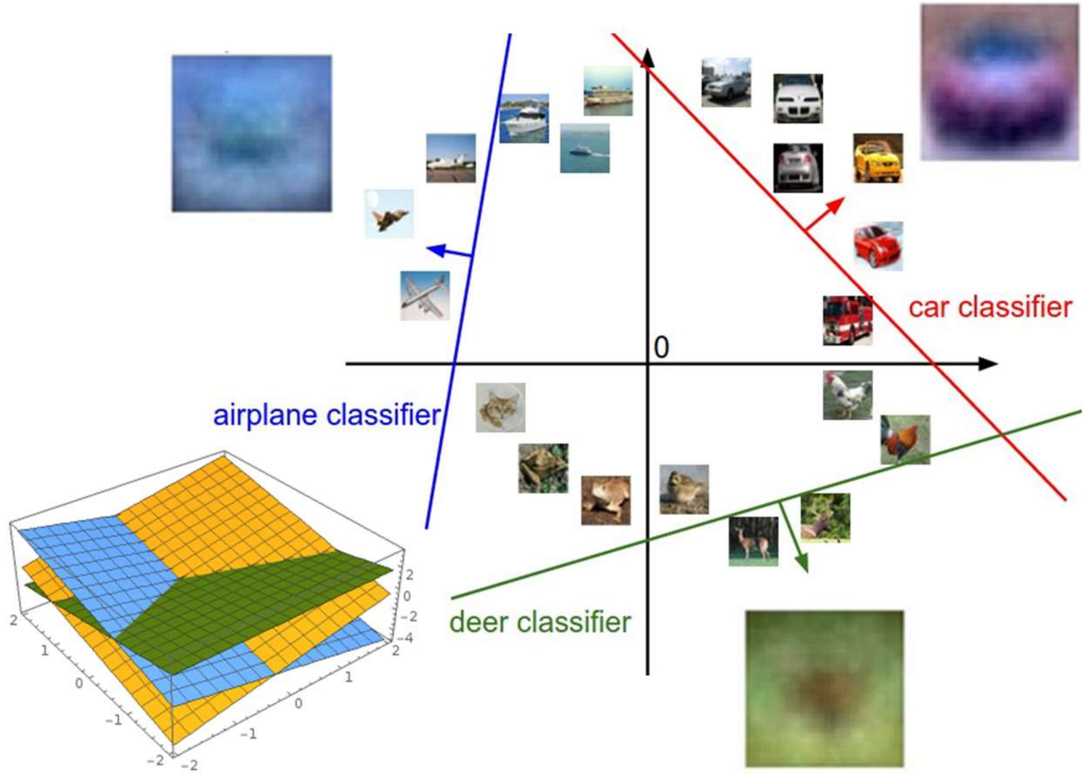
Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

Visual Viewpoint

We can convert the weight vector back into the shape of the image and visualize



Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n



Plot created using Wolfram Cloud

Geometric Viewpoint

$$f(x, W) = Wx + b$$

Array of **32x32x3** numbers
(3072 numbers total)

Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

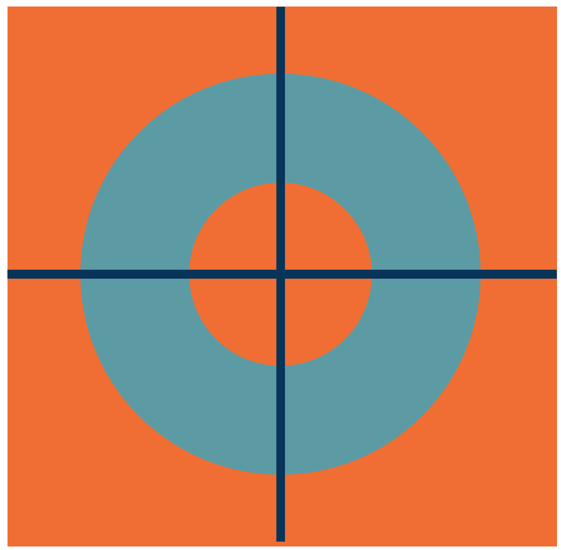
Hard Cases for a Linear Classifier

Class 1:
number of pixels > 0 odd

Class 2:
number of pixels > 0 even

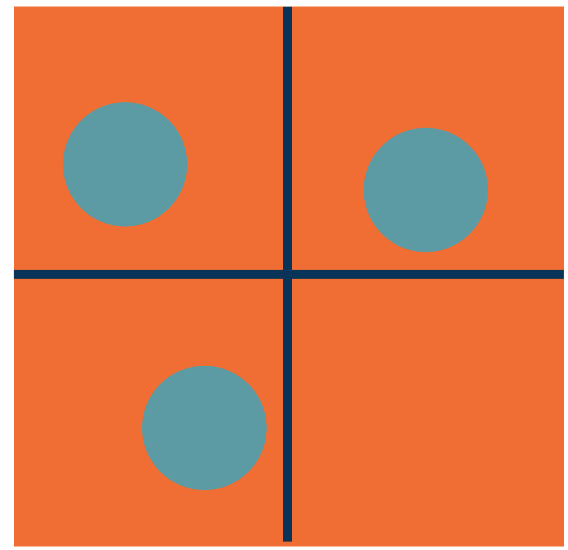
Class 1:
1 < = L2 norm < = 2

Class 2:
Everything else



Class 1:
Three modes

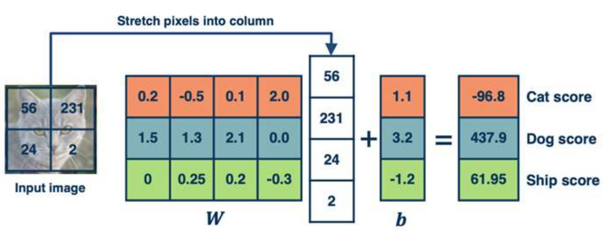
Class 2:
Everything else



Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

Algebraic Viewpoint

$$f(x, W) = Wx$$

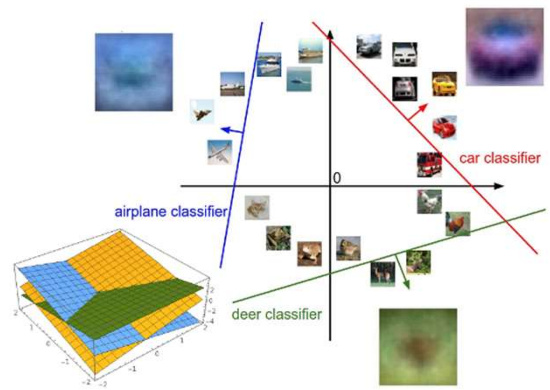


Visual Viewpoint

One template per class

Geometric Viewpoint

Hyperplanes cutting up space



Adapted from slides by Fei-Fei Li, Justin Johnson, Serena Yeung, from CS 231n

- We will learn complex, parameterized functions
  - Start w/ simple building blocks such as linear classifiers

- Key is to learn parameters, but learning is hard
  - Sources of generalization error
  - Add bias/assumptions via architecture, loss, optimizer

- Components of parametric classifiers:
  - Input/Output, Model (function), Loss function, Optimizer
  - Example: Image/Label, Linear Classifier, Hinge Loss, ?

Summary