

CS 4803-DL / 7643-A: LECTURE 21

DANFEI XU

Topics:

- Reinforcement Learning Part 2
 - **Policy Gradient**
 - **Actor-Critic**
 - **Advanced Policy Gradient Methods**
 - **Frontiers**

RL: Sequential decision making in an environment with evaluative feedback.

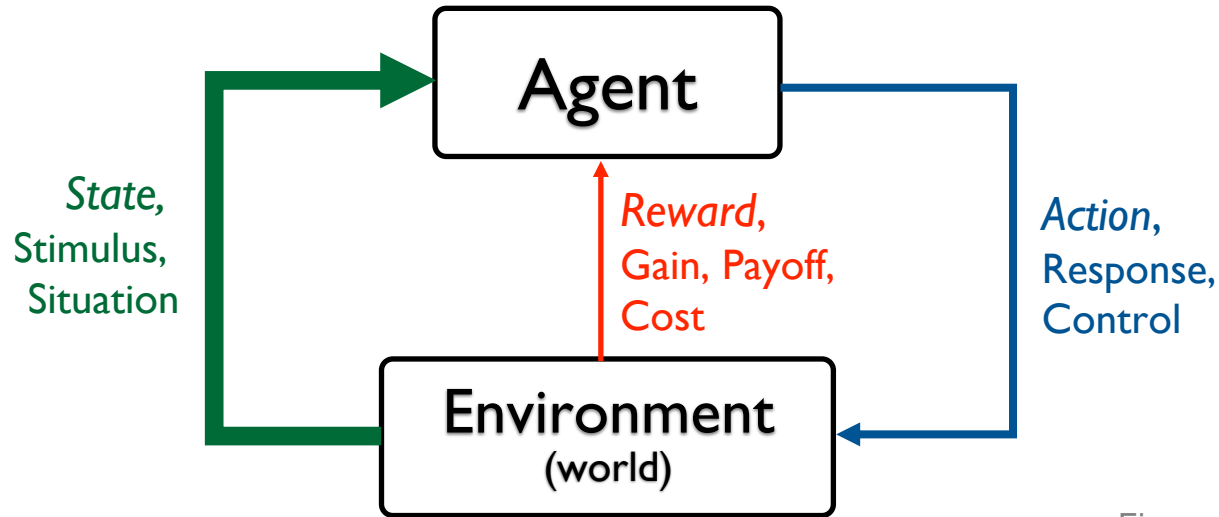


Figure Credit: Rich Sutton

- **Environment** may be unknown, non-linear, stochastic and complex.
- **Agent** learns a **policy** to map states of the environments to actions.
 - Seeking to maximize cumulative reward in the long run.

- **MDPs:** Theoretical framework underlying RL
- An MDP is defined as a tuple $(\mathcal{S}, \mathcal{A}, \mathcal{R}, \mathbb{T}, \gamma)$
 - \mathcal{S} : Set of possible states
 - \mathcal{A} : Set of possible actions
 - $\mathcal{R}(s, a, s')$: Distribution of reward
 - $\mathbb{T}(s, a, s')$: Transition probability distribution, also written as $p(s'|s, a)$
 - γ : Discount factor
- **Experience:** $\dots S_t, A_t, R_{t+1}, S_{t+1}, A_{t+1}, R_{t+2}, S_{t+2}, \dots$
- **Markov property:** Current state completely characterizes state of the environment
- **Assumption:** Most recent observation is a sufficient statistic of history

$$p(S_{t+1} = s' | S_t = s_t, A_t = a_t, S_{t-1} = s_{t-1}, \dots, S_0 = s_0) = p(S_{t+1} = s' | S_t = s_t, A_t = a_t)$$

Algorithm: Value Iteration

Initialize values of all states to arbitrary values, e.g., all 0's.

While not converged:

For each state:

$$V^{i+1}(s) \leftarrow \max_a \sum_{s'} p(s'|s, a) [r(s, a) + \gamma V^i(s')]$$

Repeat until convergence (no change in values)

$$V^0 \rightarrow V^1 \rightarrow V^2 \rightarrow \dots \rightarrow V^i \rightarrow \dots \rightarrow V^*$$

Time complexity per iteration $O(|\mathcal{S}|^2 |\mathcal{A}|)$

Q-Learning: a model-free method for RL

Idea: represent the Q value table as a parametric function $Q_\theta(s, a)$!

How do we learn the function?

$$\begin{aligned} Q'(s_t, a_t) &= (1 - \alpha)Q(s_t, a_t) + \alpha[r_t + \gamma \max_a Q(s_{t+1}, a)] \\ &= Q(s_t, a_t) + \alpha(r_t + \gamma \max_a Q(s_{t+1}, a) - Q(s_t, a_t)) \end{aligned}$$

Now, at optimum, $Q(s_t, a_t) = Q'(s_t, a_t) = Q^*(s_t, a_t)$; This gives us:

$$0 = 0 + \alpha(r_t + \gamma \max_a Q(s_{t+1}, a) - Q(s_t, a_t))$$

Learning problem:

$$\operatorname{argmin}_\theta \left\| \underbrace{r_t + \gamma \max_a Q_\theta(s_{t+1}, a)}_{\text{Target Q value}} - Q_\theta(s_t, a_t) \right\|$$

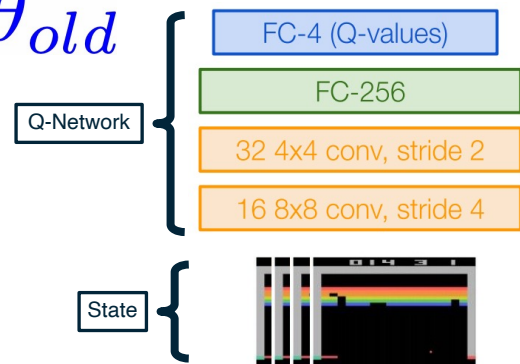
- Minibatch of $\{(s, a, s', r)_i\}_{i=1}^B$

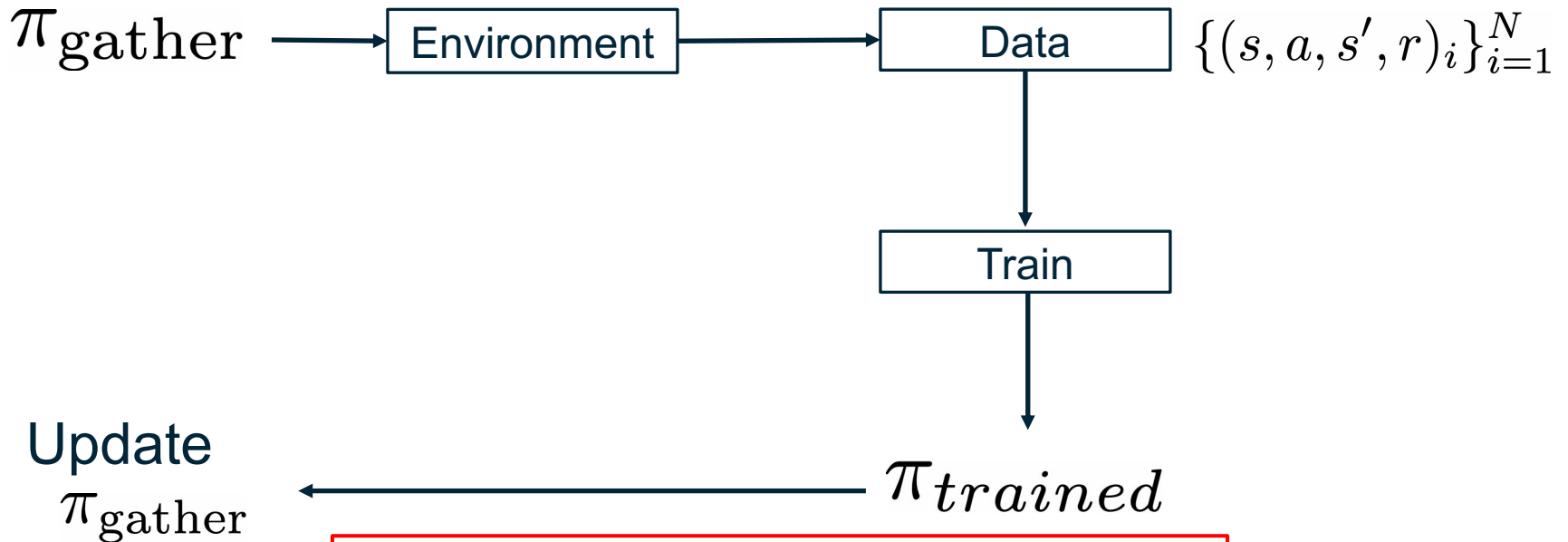


- Compute loss:

$$\left(\underbrace{Q_{new}(s, a)}_{\theta_{new}} - \left(r + \gamma \max_a \underbrace{Q_{old}(s', a)}_{\theta_{old}} \right) \right)^2$$

- Backward pass: $\frac{\partial Loss}{\partial \theta_{new}}$





Challenge 1: Exploration vs Exploitation

Challenge 2: Non iid, highly correlated data

How to gather experience?

- What should π_{gather} be?
 - Greedy? -> no exploration, always choose the most confident action
$$\arg \max_a Q(s, a; \theta)$$
- An exploration strategy:
 - ϵ -greedy

$$a_t = \begin{cases} \arg \max_a Q(s, a) & \text{with probability } 1 - \epsilon \\ \text{random action} & \text{with probability } \epsilon \end{cases}$$

- Correlated data: addressed by using experience replay
 - A replay buffer stores transitions (s, a, s', r)
 - Continually update replay buffer as game (experience) episodes are played, older samples discarded
 - Train Q-network on random minibatches of transitions from the replay memory, instead of consecutive samples
- Larger the buffer, lower the correlation

Algorithm 1 Deep Q-learning with Experience Replay

Initialize replay memory \mathcal{D} to capacity N

Initialize action-value function Q with random weights

Experience Replay

for episode = 1, M **do**

 Initialize sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$

for $t = 1, T$ **do**

 With probability ϵ select a random action a_t
 otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$

Epsilon-greedy

 Execute action a_t in emulator and observe reward r_t and image x_{t+1}

 Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$

 Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D}

 Sample random minibatch of transitions $(\phi_j, a_j, r_j, \phi_{j+1})$ from \mathcal{D}

 Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$

Q Update

 Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3

end for

end for

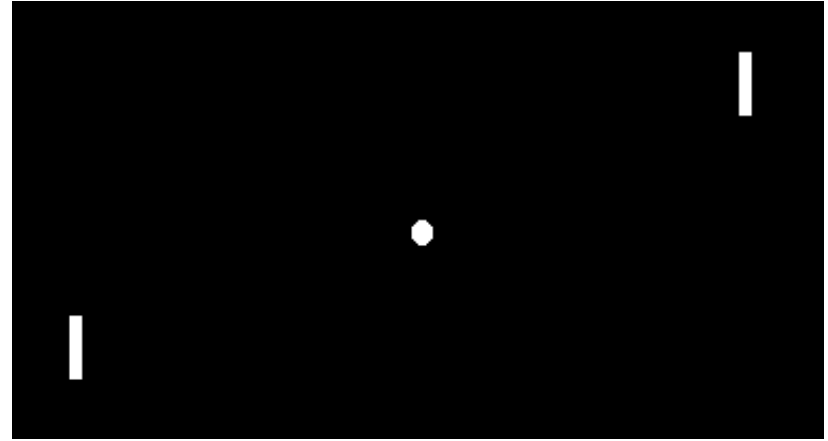
Atari Games



- ◆ **Objective:** Complete the game with the highest score
- ◆ **State:** Raw pixel inputs of the game state
- ◆ **Action:** Game controls e.g. Left, Right, Up, Down
- ◆ **Reward:** Score increase/decrease at each time step

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Atari Games



<https://www.youtube.com/watch?v=V1eYniJORnk>

Different RL Paradigms

- ◆ **Value-based RL**

- ◆ (Deep) Q-Learning, approximating $Q^*(s, a)$ with a deep Q-network

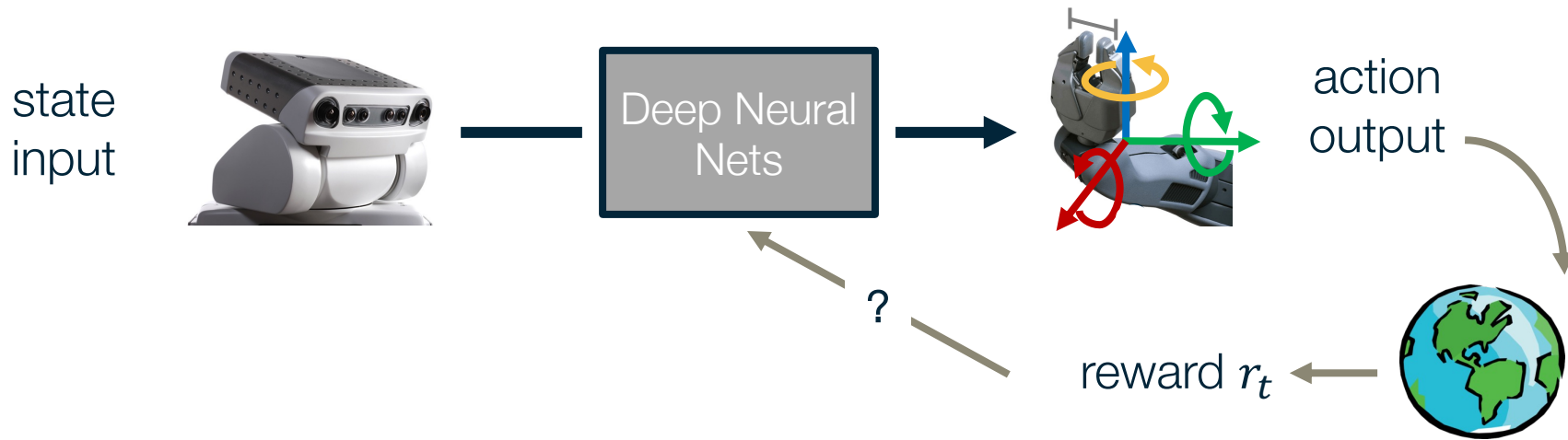
- ◆ **Policy-based RL**

- ◆ Directly approximate optimal policy π^* with a parametrized policy π_θ^*

- ◆ **Model-based RL**

- ◆ Approximate transition function $T(s', a, s)$ and reward function $\mathcal{R}(s, a)$
- ◆ Plan by looking ahead in the (approx.) future!

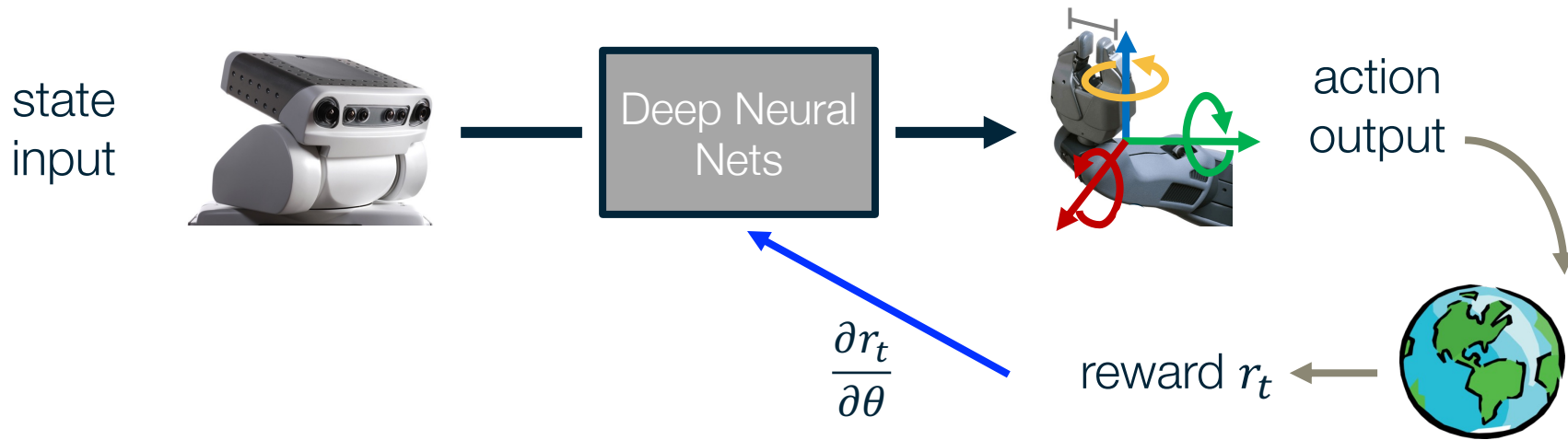
Deep Learning for Decision Making



Problem: we don't know the correct action label to supervise the output!

All we know is the step-wise task reward

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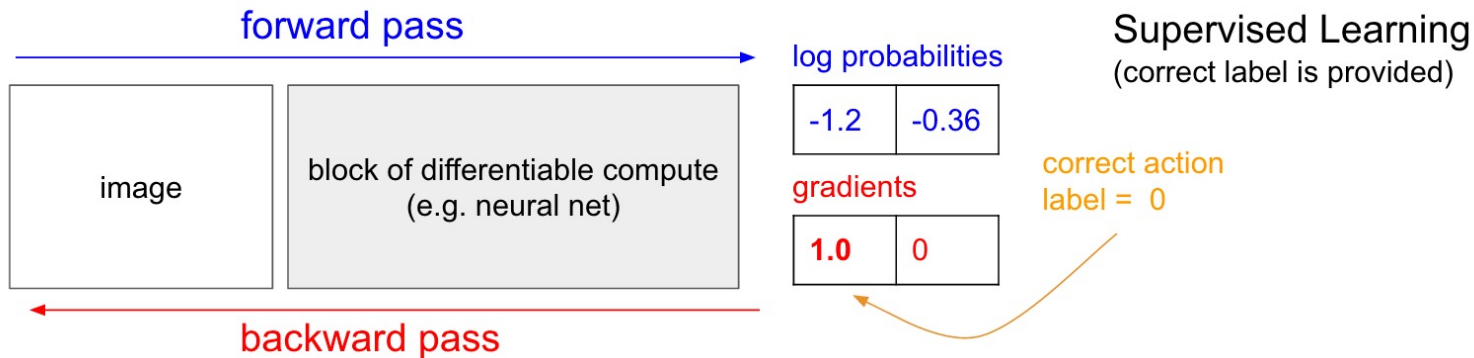


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Can we directly backprop reward???

Policy Gradient: Just backprop from reward (sort of)!



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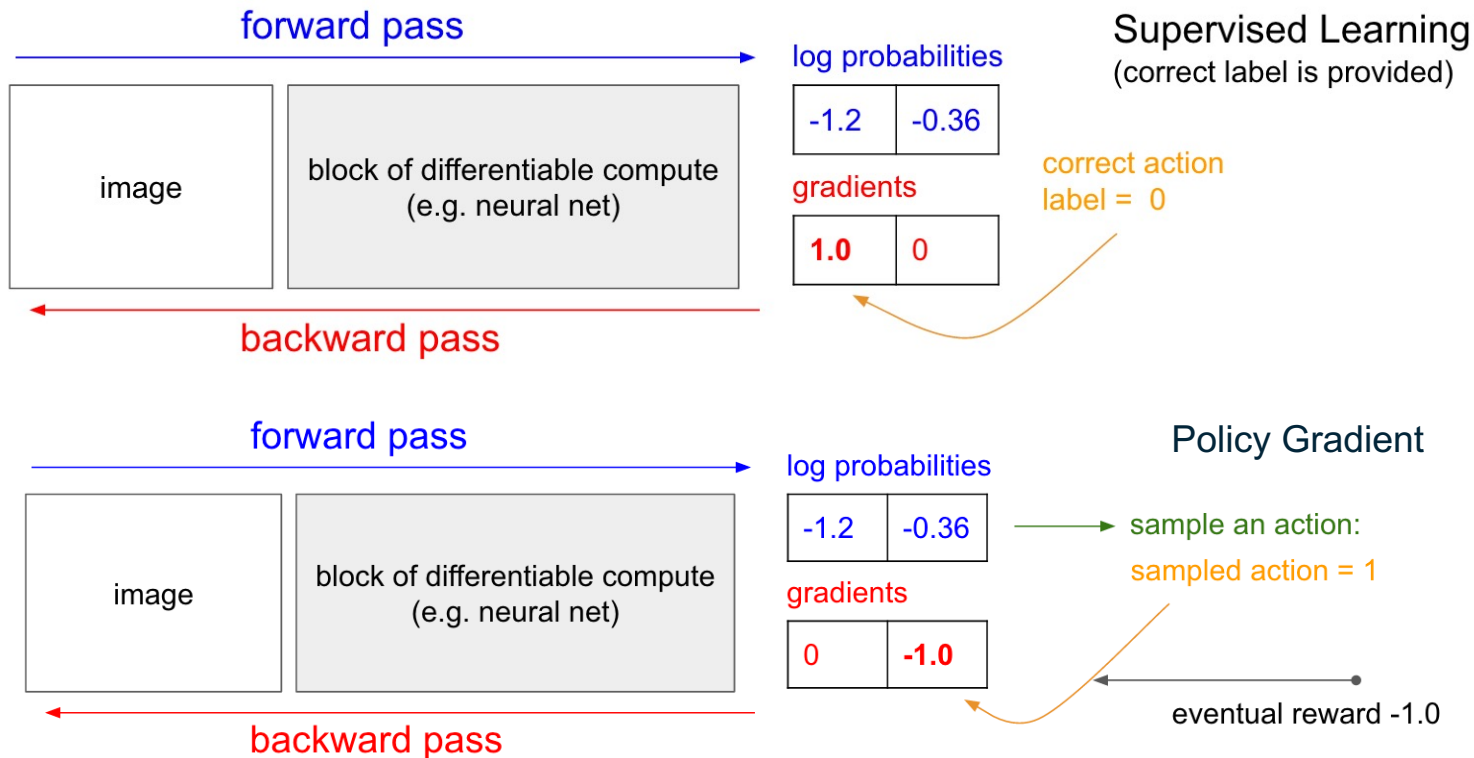


Image Source: <http://karpathy.github.io/2016/05/31/rl/>

Brief derivation of policy gradient (REINFORCE)

Let $\tau = (s_0, a_0, \dots, s_T, a_T)$ denote a trajectory

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Let $\tau = (s_0, a_0, \dots, s_T, a_T)$ denote a trajectory

- ◆ Distribution of trajectories given a policy parameterized by θ is:

$$\begin{aligned} p_{\theta}(\tau) &= p_{\theta}(s_0, a_0, \dots, s_T, a_T) \\ &= p(s_0) \prod_{t=0}^{T-1} p_{\theta}(a_t | s_t) \cdot p(s_{t+1} | s_t, a_t) \end{aligned}$$

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◆ What we need (policy gradient):

$$\nabla_{\theta} J(\theta) = \nabla_{\theta} \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\mathcal{R}(\tau)]$$

Brief derivation of policy gradient (REINFORCE)

$$\begin{aligned}\nabla_{\theta} J(\theta) &= \nabla_{\theta} \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\mathcal{R}(\tau)] \\ &= \nabla_{\theta} \int \pi_{\theta}(\tau) \mathcal{R}(\tau) d\tau \\ &= \int \nabla_{\theta} \pi_{\theta}(\tau) \mathcal{R}(\tau) d\tau \\ &= \int \nabla_{\theta} \pi_{\theta}(\tau) \cdot \frac{\pi_{\theta}(\tau)}{\pi_{\theta}(\tau)} \cdot \mathcal{R}(\tau) d\tau \\ &= \int \pi_{\theta}(\tau) \nabla_{\theta} \log \pi_{\theta}(\tau) \mathcal{R}(\tau) d\tau \\ &= \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\nabla_{\theta} \log \pi_{\theta}(\tau) \mathcal{R}(\tau)]\end{aligned}$$

Expectation as integral

Exchange integral and gradient

Log derivative rule: $\frac{d \log f(x)}{dx} = \frac{f'(x)}{f(x)}$

$$\nabla_{\theta} \log \pi(\tau) = \frac{\nabla_{\theta} \pi(\tau)}{\pi(\tau)}$$

Brief derivation of policy gradient (REINFORCE)

$$\pi_{\theta}(\tau) = p(s_0) \prod_{t=0}^{T-1} p_{\theta}(a_t | s_t) \cdot p(s_{t+1} | s_t, a_t)$$

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\underbrace{\nabla_{\theta} \log \pi_{\theta}(\tau)}_{\text{Gradient of log-probability}} \mathcal{R}(\tau) \right]$$

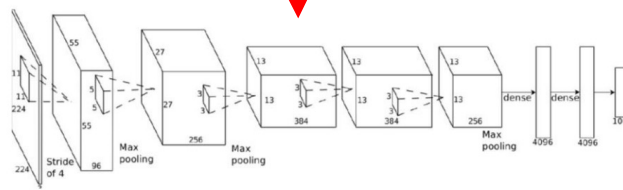
$$\nabla_{\theta} \left[\cancel{\log p(s_0)} + \sum_{t=1}^T \log \pi_{\theta}(a_t | s_t) + \sum_{t=1}^T \cancel{\log p(s_{t+1} | s_t, a_t)} \right]$$

Doesn't depend on
Transition probabilities!

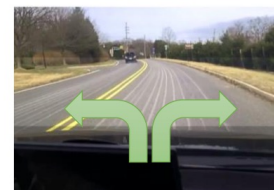
$$= \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) \cdot \sum_{t=1}^T \mathcal{R}(s_t, a_t) \right]$$



s_t



$\pi_{\theta}(a_t | s_t)$



a_t

Can use continuous action space!

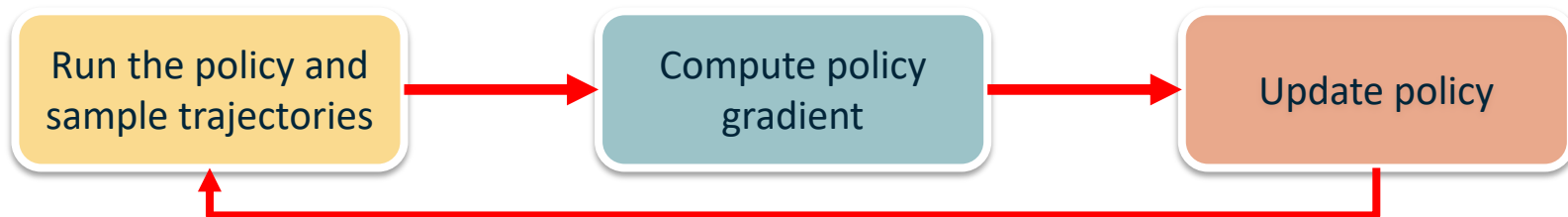
Policy gradient: algorithm sketch

- Sample trajectories $\tau_i = \{s_1, a_1, \dots, s_T, a_T\}_i$ by acting according to π_θ

- Compute policy gradient as

$$\nabla_\theta J(\theta) \approx \frac{1}{N} \sum_i \left[\sum_{t=1}^T \nabla_\theta \log \pi_\theta (a_t^i | s_t^i) \cdot \sum_{t=1}^T \mathcal{R} (s_t^i | a_t^i) \right]$$

- Update policy parameters: $\theta \leftarrow \theta + \alpha \nabla_\theta J(\theta)$



Policy gradient intuition

$\log \pi_{\theta}(a|s)$

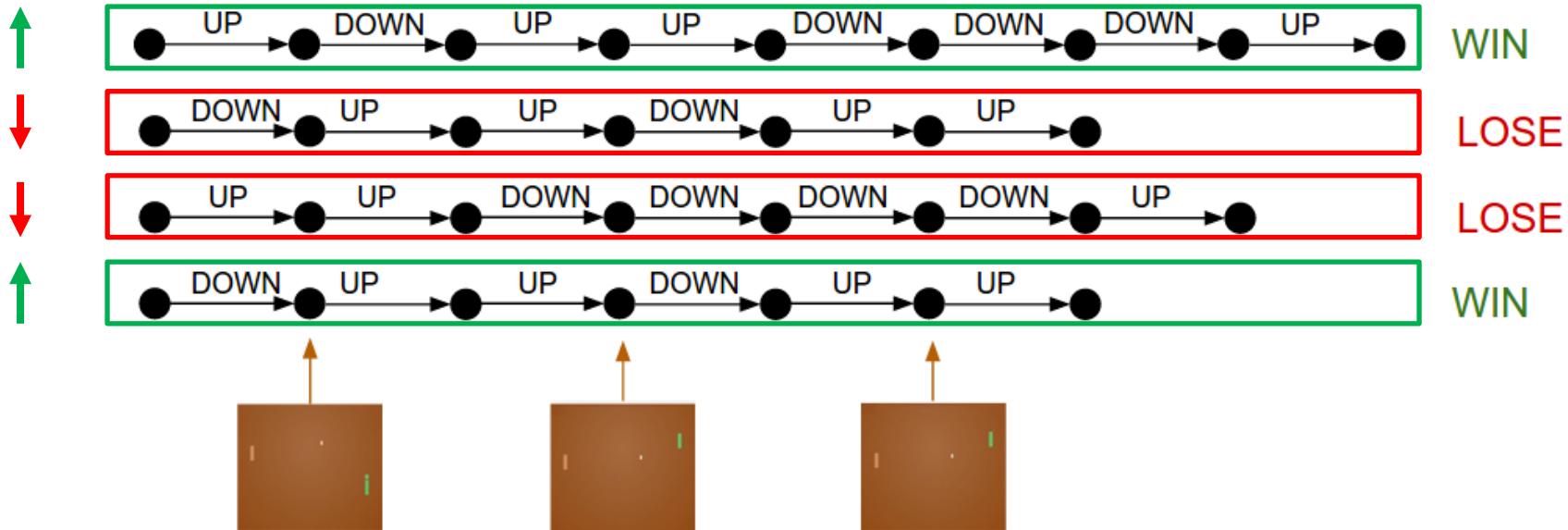


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Issues with Policy Gradients

- **Credit assignment is hard!**
 - Which specific action led to increase in reward
 - Suffers from high variance → leading to unstable training

Can we do better?

What if instead of just reward per episode, we know the expected future return of taking an action? (This should remind you of something ...)

Q value function $Q(s, a)$!

Actor-Critic

- Learn both policy and Q function
 - Use the “actor” to sample trajectories
 - Use the Q function to “evaluate” or “critic” the policy

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- REINFORCE: $\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) \mathcal{R}(s, a)]$
- Actor-critic: $\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) Q^{\pi_{\theta}}(s, a)]$

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- Update “critic”:
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Note the difference to DQN: $\left(Q_{new}(s, a) - (r + \gamma \max_a Q_{old}(s', a)) \right)^2$

Actor-Critic

$$\text{Actor-critic: } \nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) Q_{\beta}(s, a)]$$

Actor-Critic

Actor-critic Policy Gradient: $\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) Q_{\beta}(s, a)]$

Consider a situation where $Q_{\beta}(s, a_1) = 10.1$ and $Q_{\beta}(s, a_2) = 10.5$

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- $V(s)$: How much better is taking action a over the average value at state s

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- $V(s)$: How much better is taking action a over the average value at state s
- Say $V(s) = 10.0$, we have $A(s, a_1) = 0.1$ and $A(s, a_2) = 0.5$

Advantage Actor-Critic (A2C)

Advantage Actor-critic Gradient: $\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) A(s, a)]$

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Problem: need to learn both Q and V to calculate A

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Problem: need to learn both Q and V to calculate A

Idea: use state value of experience sample to approximate Q :

$$A(s, a) = Q(s, a) - V(s) \cong r + V(s') - V(s)$$

Policy Gradient Methods

- REINFORCE: $\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) R(s, a)]$
- Actor-critic (AC): $\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) Q(s, a)]$
- Advantage Actor-critic (A2C): $\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) A(s, a)]$

Advanced policy gradient methods

Trust Region Policy Gradient (TRPO, Schulman 2017)

Advanced policy gradient methods

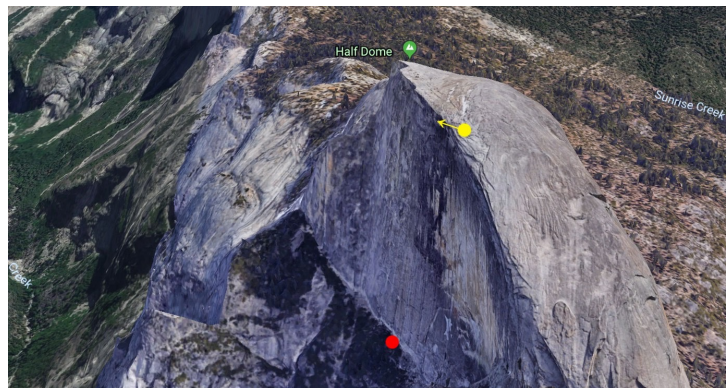
Trust Region Policy Gradient (TRPO, Schulman 2017)

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- Idea: constrain the update to a *trust region* using off-policy policy gradient

$$J(\theta) = \mathbb{E}_{s \sim \rho^{\pi_{\theta_{\text{old}}}}, a \sim \pi_{\theta_{\text{old}}}} \left[\frac{\pi_{\theta}(a|s)}{\pi_{\theta_{\text{old}}}(a|s)} \hat{A}_{\theta_{\text{old}}}(s, a) \right]$$

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Subject to:

$$\mathbb{E}_{s \sim \rho^{\pi_{\theta_{\text{old}}}}} [D_{\text{KL}}(\pi_{\theta_{\text{old}}}(\cdot | s) \| \pi_{\theta}(\cdot | s))] \leq \delta$$

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Optimizing this objective requires calculating Hessian
(second-order optimization)!

Advanced policy gradient methods

Proximal Policy Optimization (PPO, Schulman 2017)

Issue with TRPO: objective too complicated! Requires second-order optimization (calculating Hessian).

Advanced policy gradient methods

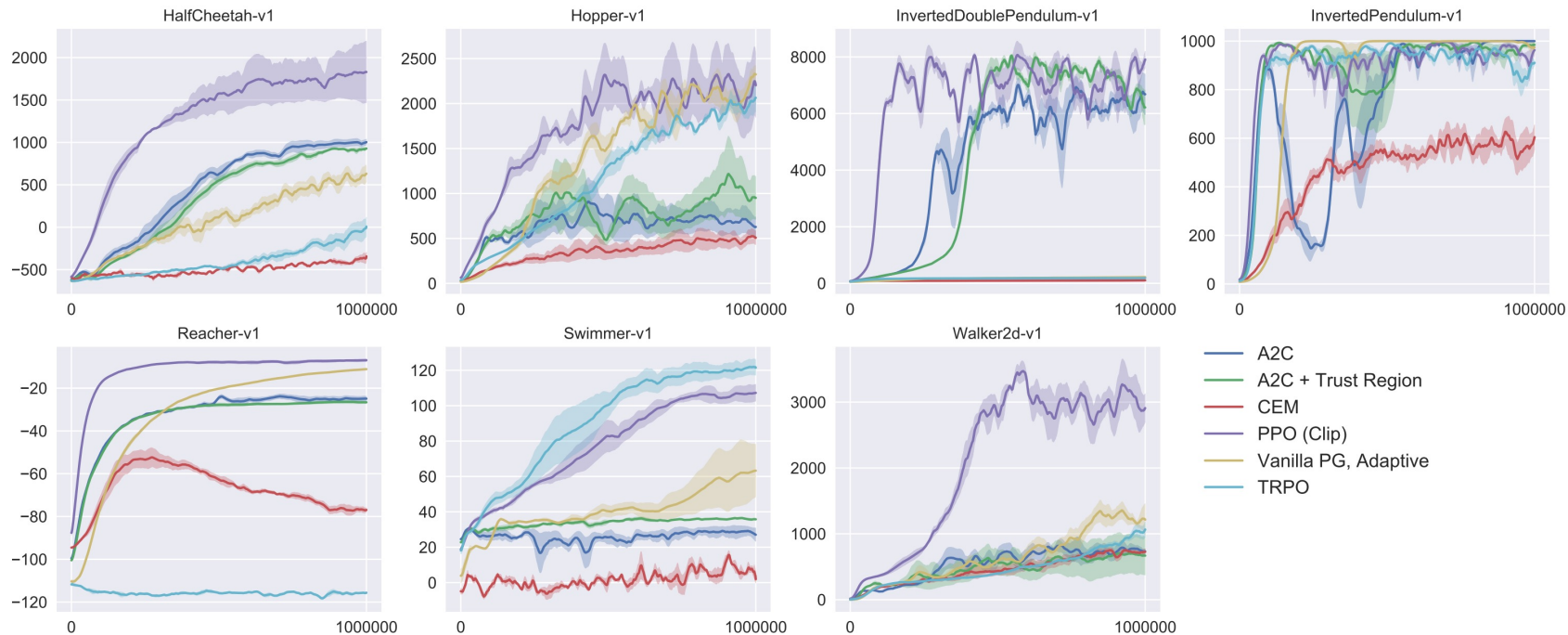
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Idea: Approximate trust-region constraint with a penalty term

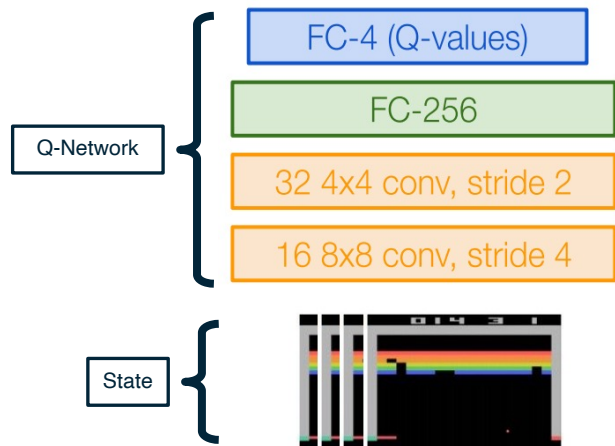
$$\underset{\theta}{\text{maximize}} \quad \hat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(a_t | s_t)}{\pi_{\theta_{\text{old}}}(a_t | s_t)} \hat{A}_t \right] - \beta \hat{\mathbb{E}}_t [\text{KL}[\pi_{\theta_{\text{old}}}(\cdot | s_t), \pi_{\theta}(\cdot | s_t)]]$$

Advanced policy gradient methods



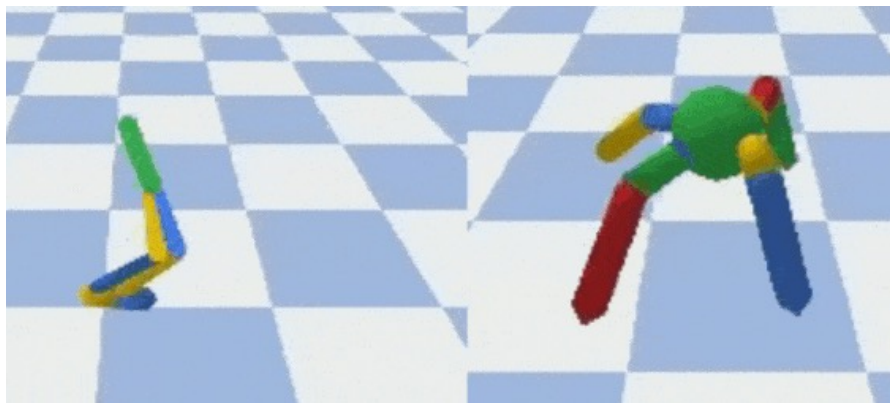
Welcome to continuous control!

DQN: limited to discrete action space

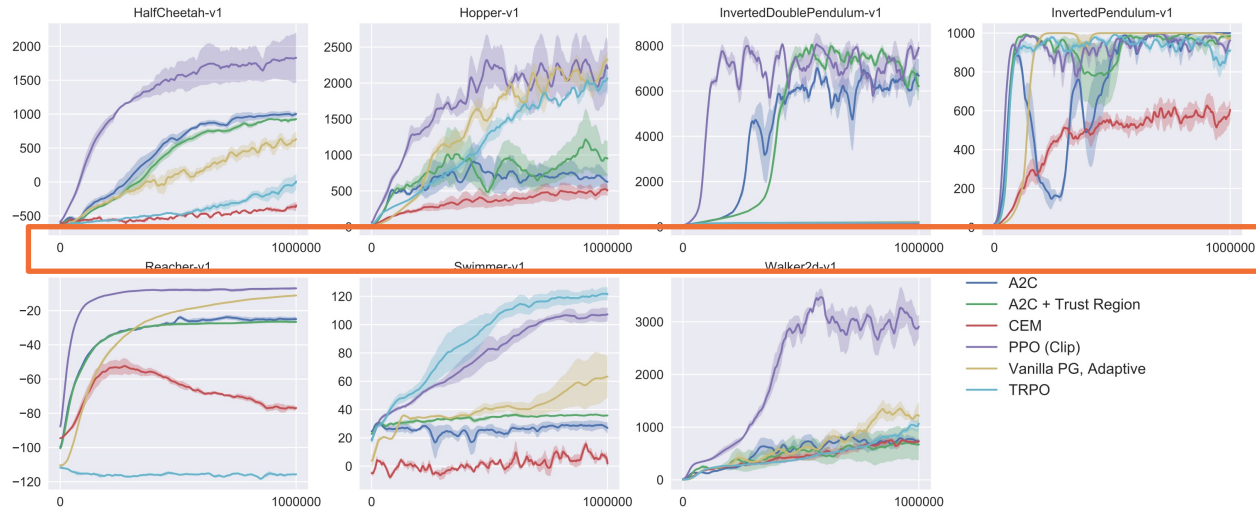


$$\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{a \sim \pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(a|s) A(s, a)]$$

Policy net can output anything!



But Deep RL is still pretty expensive to train ...



Idea: transfer policy trained in simulation (cheap) directly to the real world (expensive)!

Simulation to Real World Transfer (Sim2Real)

Issue: simulators is a *very crude* approximation of the real world!

Simulation to Real World Transfer (Sim2Real)

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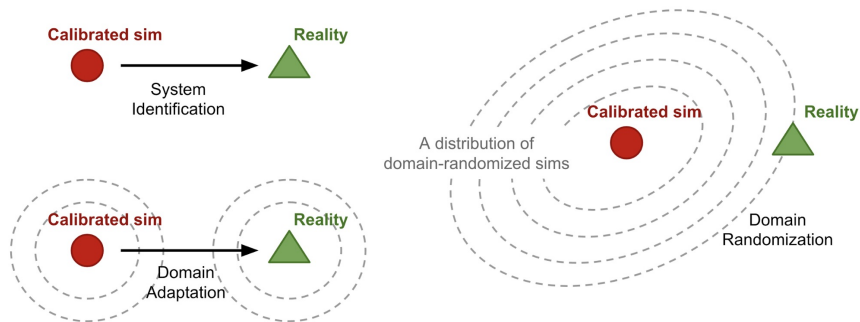
Potential gaps (not an exhaustive list):

- Position, shape, and color of objects,
- Material texture,
- Lighting condition,
- Other measurement noise
- Position, orientation, and field of view of the camera in the simulator.
- Mass and dimensions of objects,
- Mass and dimensions of robot bodies,
- Damping, k_p , friction of the joints,
- Gains for the PID controller (P term),
- Joint limit,
- Action delay,
- Observation noise.

Simulation to Real World Transfer (Sim2Real)

Issue: simulators is a *very crude* approximation of the real world!

Idea: domain randomization

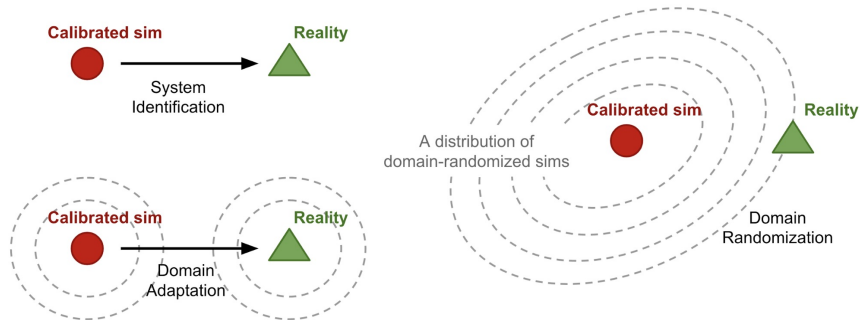


<https://lilianweng.github.io/posts/2019-05-05-domain-randomization/>

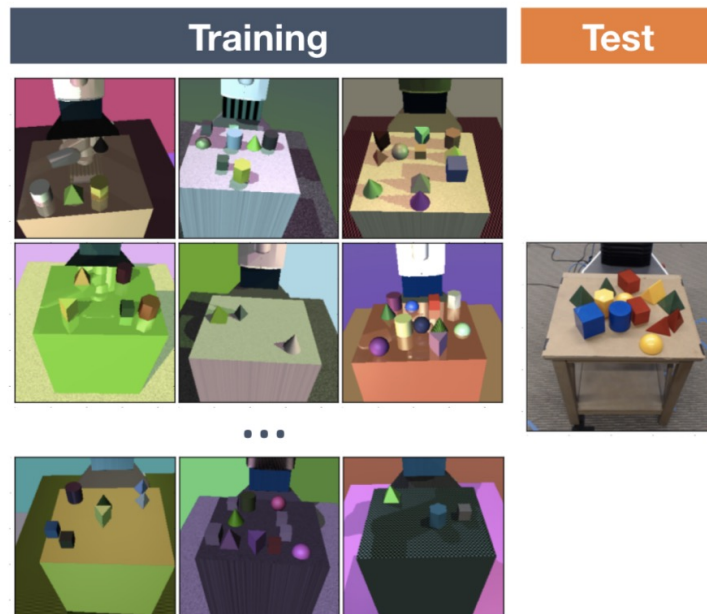
Simulation to Real World Transfer (Sim2Real)

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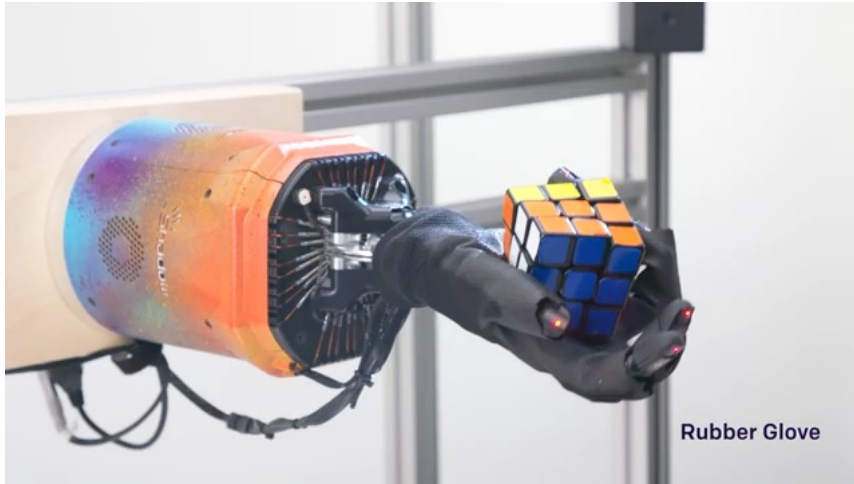
Idea: domain randomization



<https://lilianweng.github.io/posts/2019-05-05-domain-randomization/>



Deep RL for Robotics

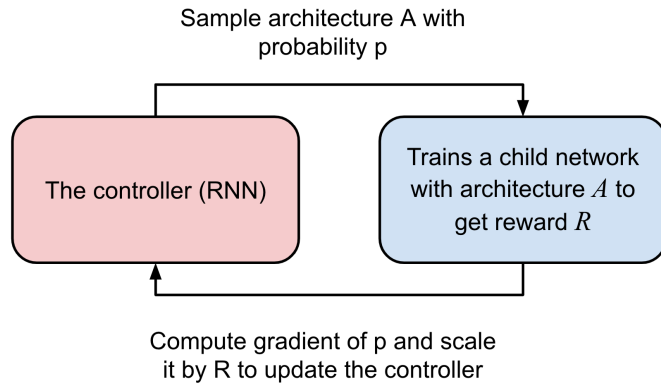


Source: OpenAI

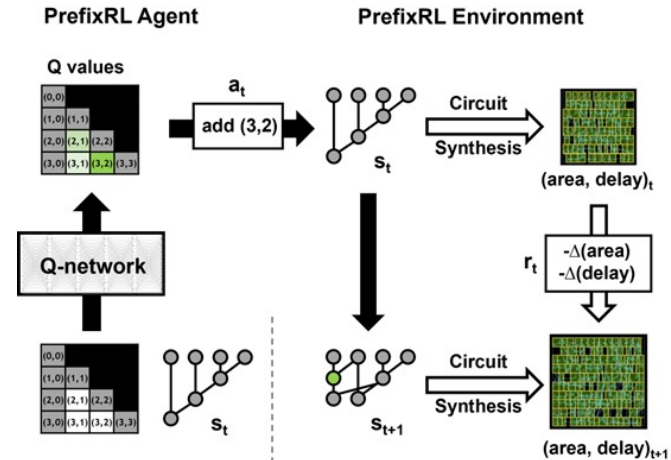


Source: ETH Zurich

Deep RL beyond robotics / games ...



Neural Architecture Search
Zoph and Le, 2016

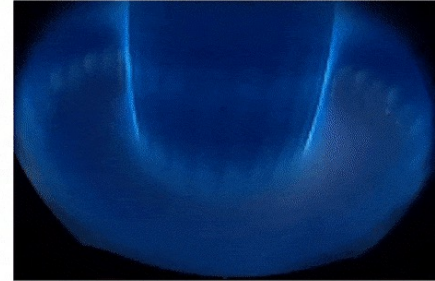


Chip Design
Roy, 2022

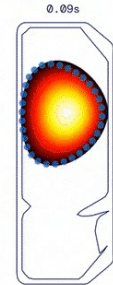
Deep RL beyond robotics / games ...



Data Center Cooling
Lazic, 2018



View from inside the tokamak



Plasma state reconstruction

Plasma Control (nuclear fusion)
Degraeve, 2022

Summary

- It turns out we can directly backprop from reward (sort of)!
- Naïve policy gradient (REINFORCE) has high variance due to the use of episodic reward. Credit assignment is hard.
- Use Action Value Function (Q) instead!
 - Actor-Critic: learn Q value function jointly with policy
 - Advantage Actor-Critic: estimate advantage A using V value function
- Advanced policy gradient methods: TRPO, PPO
- Still pretty expensive to train! Mostly used in simulation.